



VUV and X-ray Free-Electron Lasers

Electron Bunch Compression, CSR, μ Bi, Laser Heater & Machine Layout

Dinh C. Nguyen,¹ Petr Anisimov,² Nicole Neveu¹

¹ SLAC National Accelerator Laboratory

² Los Alamos National Laboratory



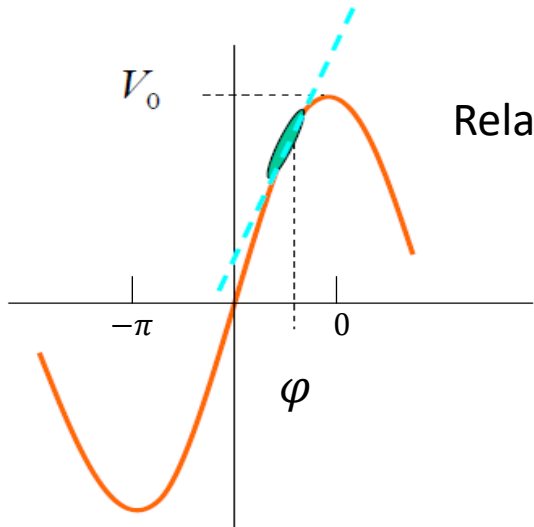
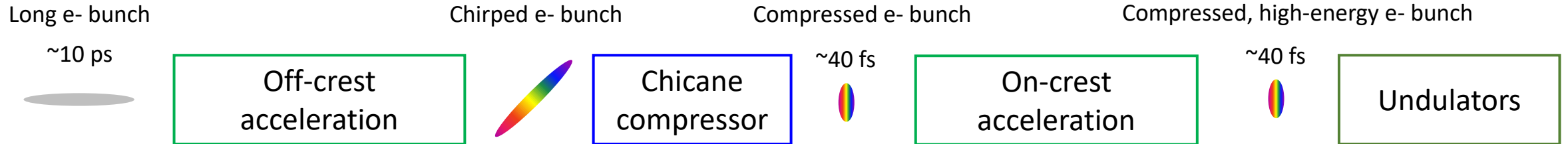
Thursday (February 4) Lecture Outline

Time

- Electron Bunch Compression 10:00 – 10:40
- Coherent Synchrotron Radiation (CSR) 10:40 – 11:00
- Break 11:00 – 11:10
- Microbunching Instabilities & Laser Heaters 11:10 – 11:30
- Machine Layout 11:30 – Noon

Bunch Compression Overview

Photoinjectors produce electron bunches with ~10 ps bunch length and ~10 A peak current. To obtain kA peak current at the undulators, we compress the bunch by imposing a “chirp” (a linear energy-z correlation) via off-crest acceleration, followed by a chicane compressor to rotate the “chirped” bunch into an upright ellipse, i.e., a compressed bunch.



Relative energy deviation vs. z

$$\delta(z) = \kappa z + O(z^2)$$

First-order pathlength change in chicane

$$\Delta z \approx R_{56} \delta$$

First-order momentum compaction of chicane

$$R_{56} = -\left(\frac{4}{3}L + 2D\right) \theta^2$$

Creating an Energy Chirp in RF Cavities

Energy versus z , coordinate along the bunch

$$E(z) = E_0 + eV_0 \cos(kz + \varphi)$$

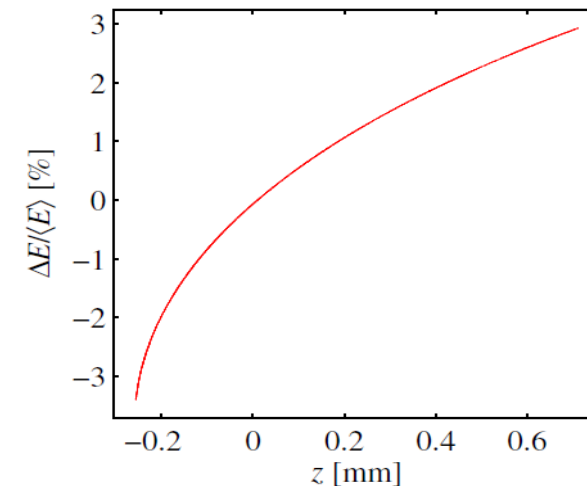
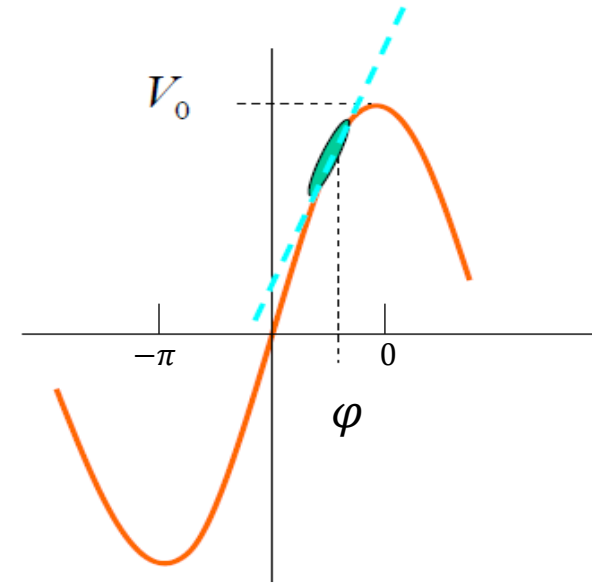
Relative energy deviation, δ versus z

$$\delta(z) = \frac{eV_0(\cos(kz + \varphi) - \cos\varphi)}{E_0 + eV_0 \cos\varphi}$$

$$\delta(z) = \kappa z + O(z^2)$$

Energy chirp

$$\kappa = \frac{d\delta}{dz} = -\frac{keV_0 \sin\varphi}{E_0 + eV_0 \cos\varphi}$$



Chirper Cavity R Matrix

$$\begin{bmatrix} x \\ x' \\ y \\ y' \\ z \\ \delta \end{bmatrix}_1 = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ R_{21} & R_{22} & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & R_{43} & R_{44} & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & R_{65} & R_{66} \end{bmatrix} \begin{bmatrix} x \\ x' \\ y \\ y' \\ z \\ \delta \end{bmatrix}_0$$

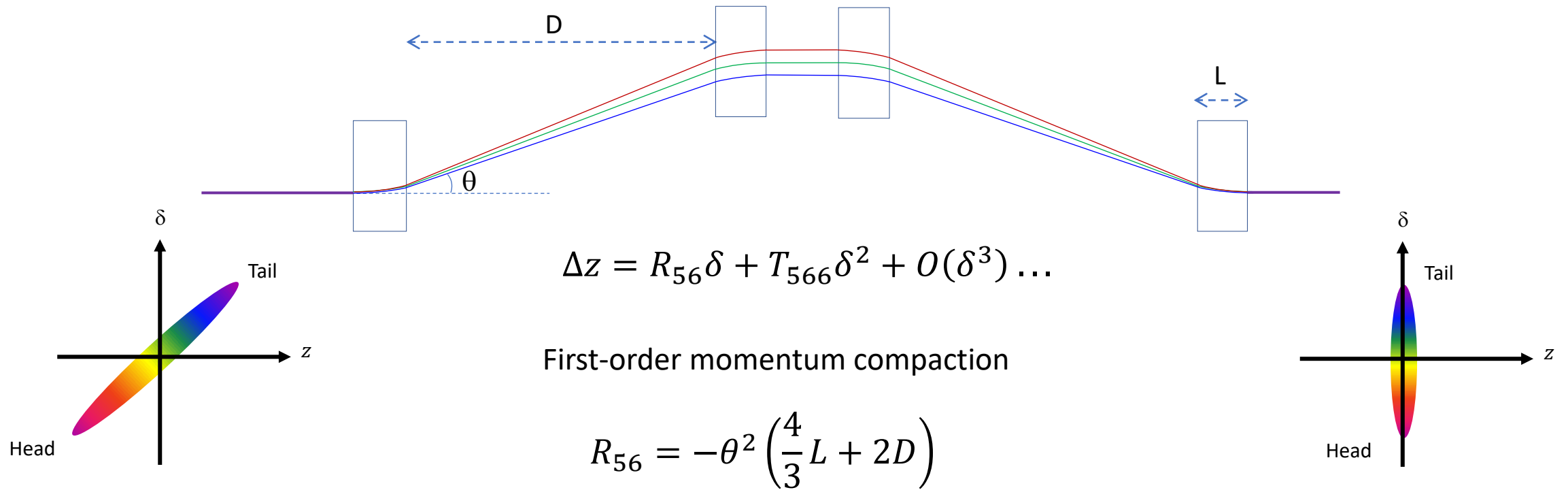
Exit centroid energy

$$E_{1c} = E_0 + eV_0 \cos\varphi$$

$$R_{65} = \kappa = -\frac{eV_0 k}{E_{1c}} \sin\varphi$$

$$R_{66} = \frac{E_0}{E_{1c}}$$

Chicane as a Non-linear Bunch Compressor



$$\Delta z = R_{56} \delta + T_{566} \delta^2 + O(\delta^3) \dots$$

First-order momentum compaction

$$R_{56} = -\theta^2 \left(\frac{4}{3} L + 2D \right)$$

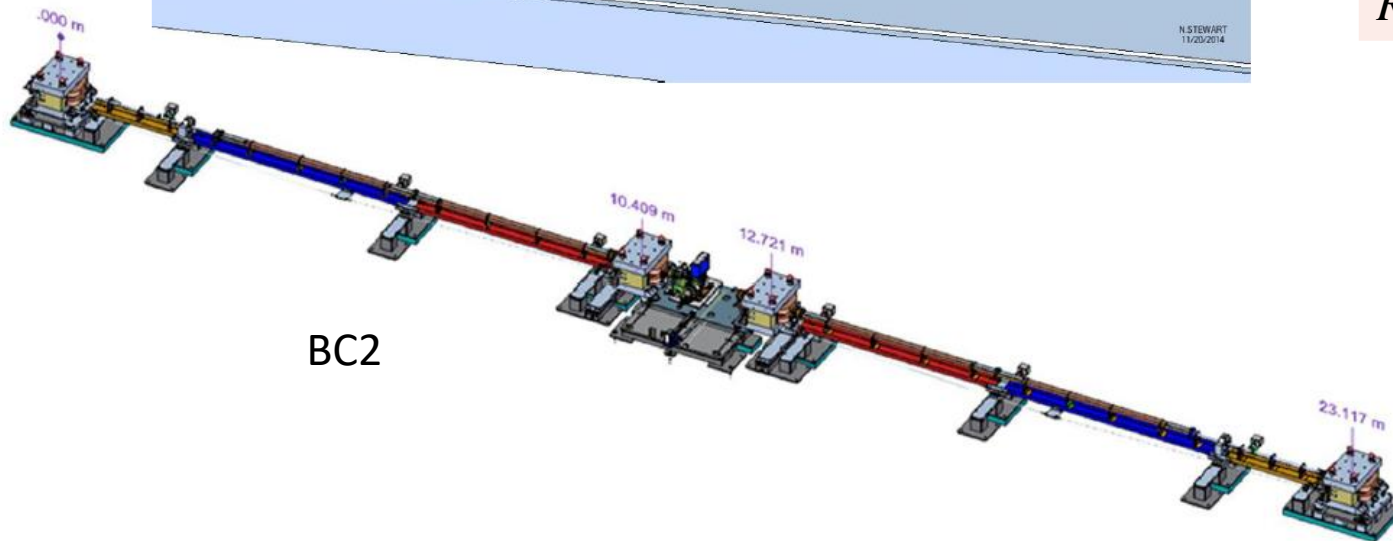
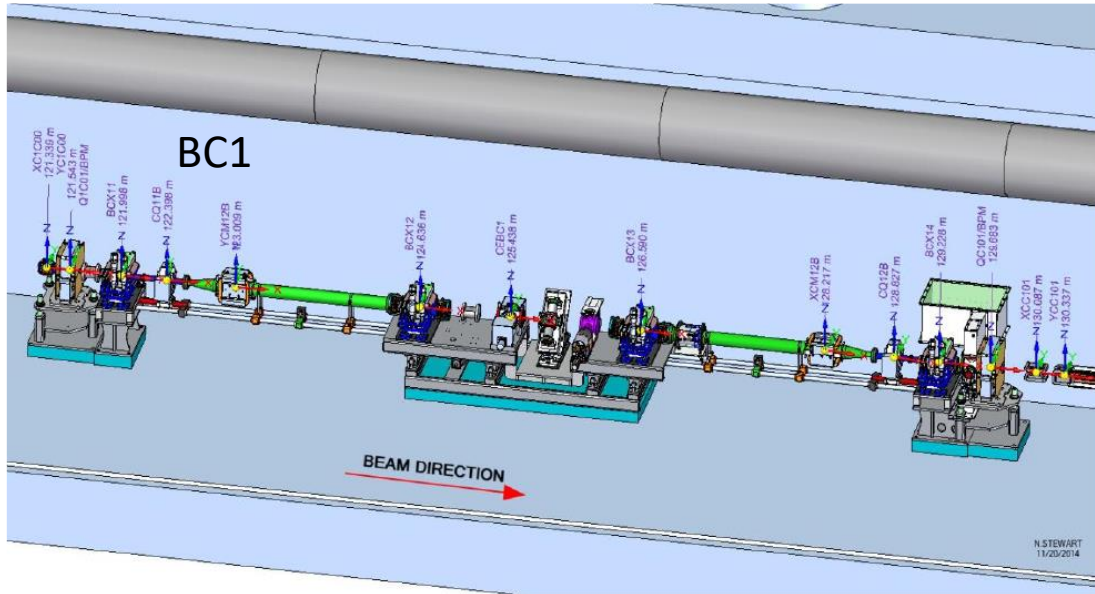
Second-order momentum compaction

$$T_{566} \approx -\frac{3}{2} R_{56}$$

Chirped electron bunch

Compressed electron bunch

Physical Dimensions of LCLS-II Chicanes



	BC1	BC2
Dipole L	0.2 m	0.54 m
Distance D	3 m	10.41 m
Total length	6.3 m	23.7 m
Angle θ	0.087 rad	0.05 rad
Beam energy E_b	250 MeV	1.6 GeV
R_{56}	-39 mm	-54 mm

Approximate value of R_{56} for $D \gg L$

$$R_{56} \approx -2\theta^2 D$$

Vary R_{56} by adjusting the dipole magnetic field, thus changing θ

Combined Chirper-Chicane Transfer Matrix

Transfer matrix of the RF chirper cavity

$$\begin{pmatrix} z_1 \\ \delta_1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ \kappa & \frac{E_0}{E_{1c}} \end{pmatrix} \cdot \begin{pmatrix} z_0 \\ \delta_0 \end{pmatrix}$$

Transfer matrix of the chicane

$$\begin{pmatrix} z_2 \\ \delta_2 \end{pmatrix} = \begin{pmatrix} 1 & R_{56} \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} z_1 \\ \delta_1 \end{pmatrix}$$

Multiply these two matrices together, we obtain the combined chirper cavity-chicane transfer matrix

$$\begin{pmatrix} z_2 \\ \delta_2 \end{pmatrix} = \begin{pmatrix} 1 + \kappa R_{56} & R_{56} \frac{E_0}{E_{1c}} \\ \kappa & \frac{E_0}{E_{1c}} \end{pmatrix} \cdot \begin{pmatrix} z_0 \\ \delta_0 \end{pmatrix}$$

Particle position at the end of the chicane

$$z_2 = (1 + \kappa R_{56})z_0 + \left(\frac{E_0}{E_{1c}}\right) R_{56} \delta_0$$

Final Compressed Bunch Length

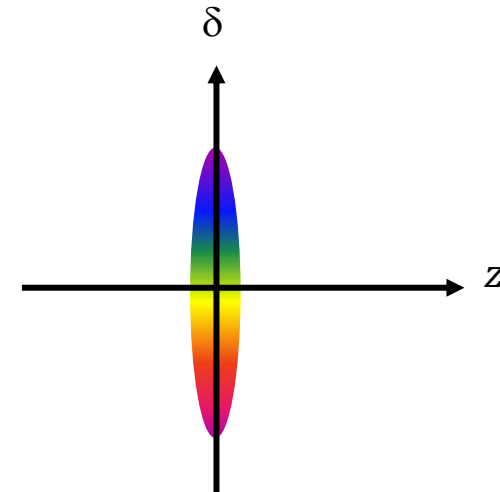
Final rms bunch length

$$\sigma_{z,f} = \sqrt{(1 + \kappa R_{56})^2 \sigma_{z,i}^2 + \left(\frac{E_{ic}}{E_{fc}}\right)^2 R_{56}^2 \sigma_{\delta,i}^2}$$

Minimum compressed bunch length is achieved with the final ellipse in upright position

$$R_{56} = -\frac{1}{\kappa} = -\frac{1}{R_{65}}$$

$$\sigma_{z,f} = \left(\frac{E_{ic}}{E_{fc}}\right) R_{56} \sigma_{\delta,i}$$



Compressed electron bunch

Nonlinear Bunch Compression

Particle energy as a function of bunch coordinate

$$\delta(z) = \kappa z + \mu z^2 + \dots$$

Linear chirp

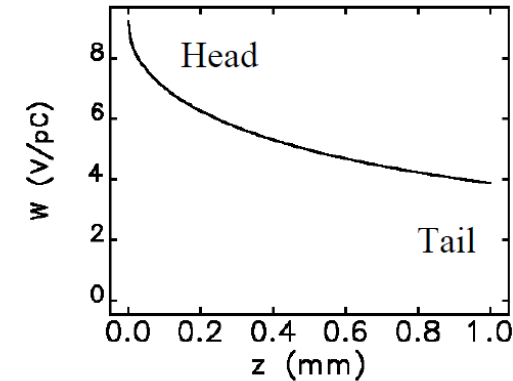
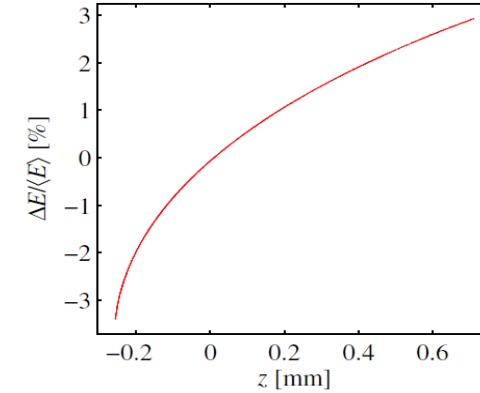


Second order curvature

$$\mu = -\frac{k^2 e V_0}{2 E_{c,f}} \cos \varphi$$

Position change in the chicane with first and second-order momentum compactions

$$\Delta z = R_{56} \delta + T_{566} \delta^2$$



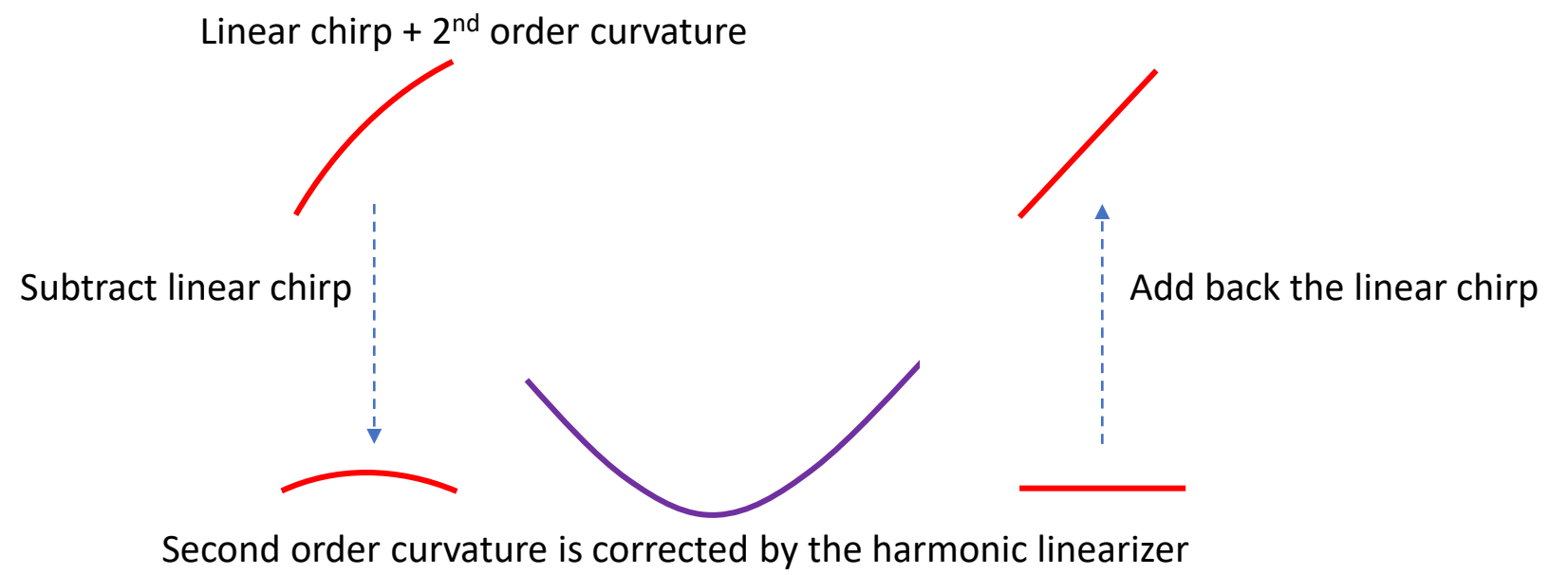
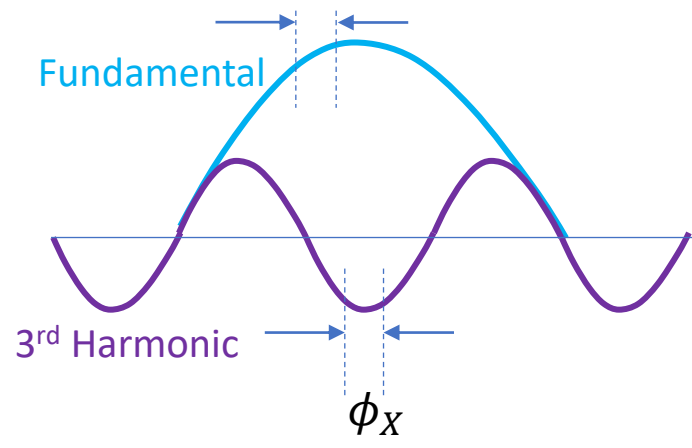
Short-range wake field in LCLS S-band linac is used to “dechirp” the final compressed bunch, i.e. remove both the linear energy chirp and 2nd order curvature.

Harmonic Linearizer

Harmonic linearizer curvature

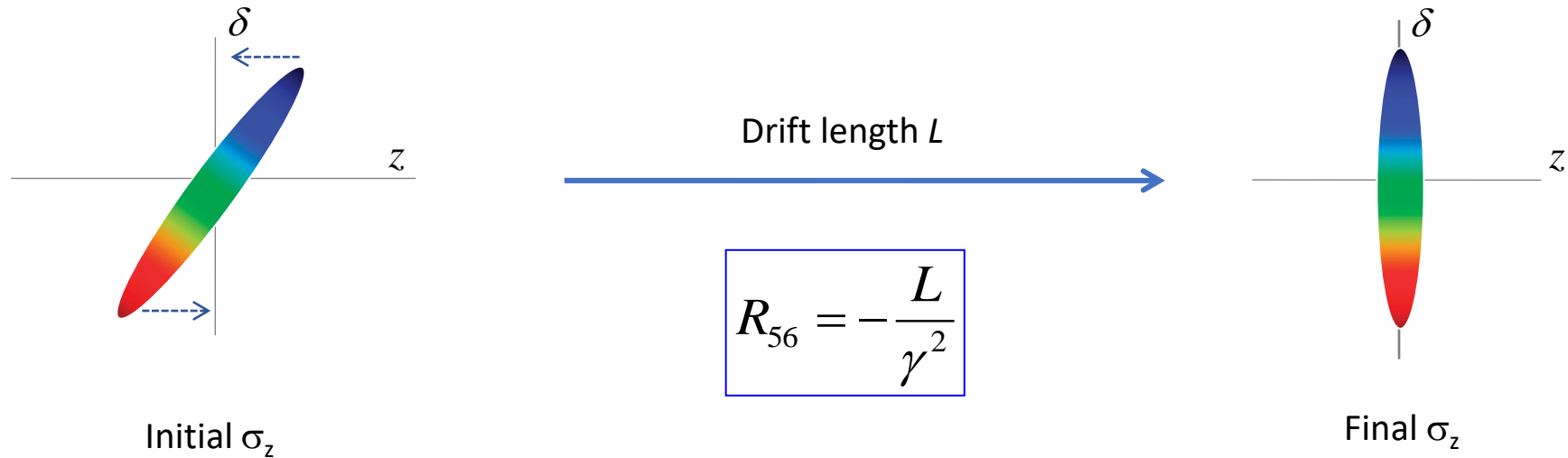
$$E_X = -k_X e V_X \cos \phi_X$$

$$\phi_X \approx -\pi$$



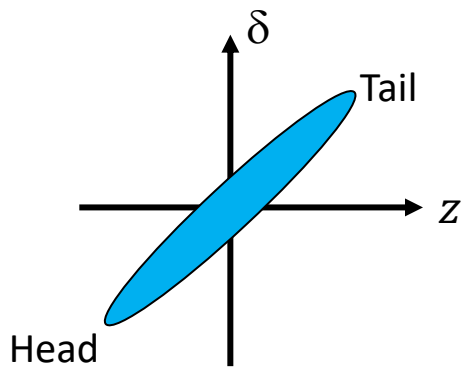
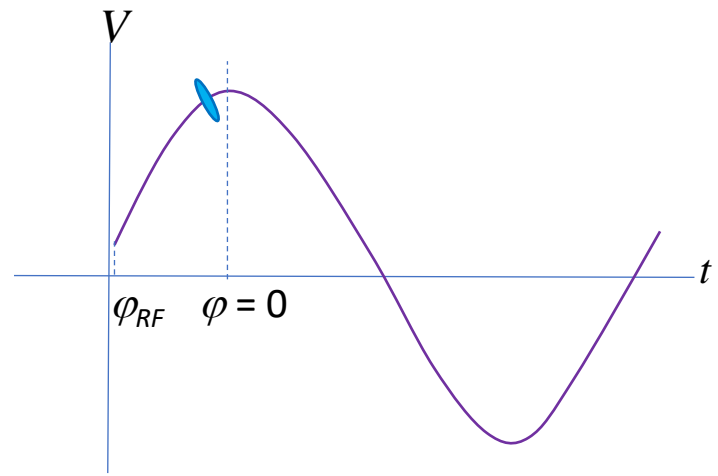
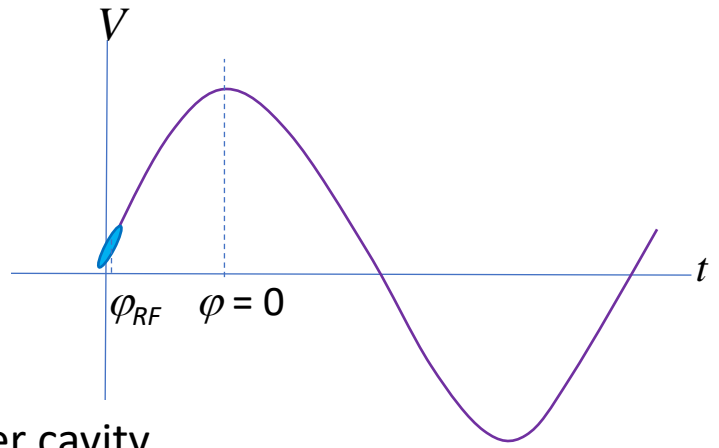
Ballistic Compression

Ballistic compression is usually applied to electron beams at relatively low energy (<2 MeV). As the chirped electron bunch propagates in the drift, the slow electrons at the head move back with respect to the center and fast electrons at the tail catch up with the center.

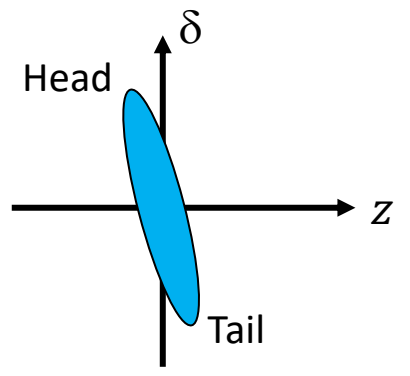


Ballistic compression is negligible at high energy as the magnitude of R_{56} of the drift decreases with the electron beam energy ($1/\gamma^2$).

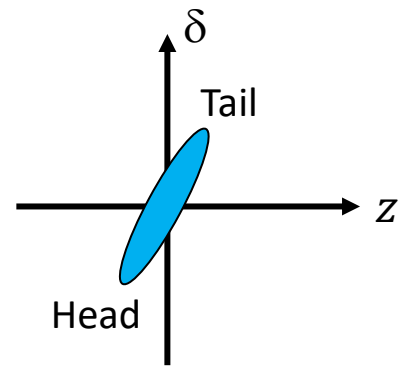
Longitudinal Phase-space Manipulation



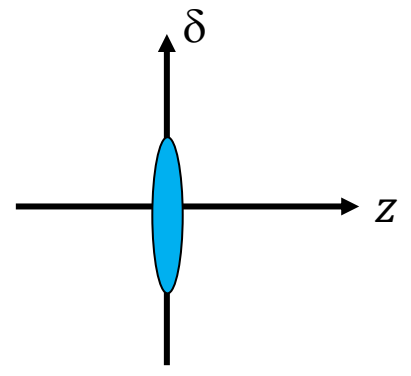
Exit of buncher cavity



Over-compression



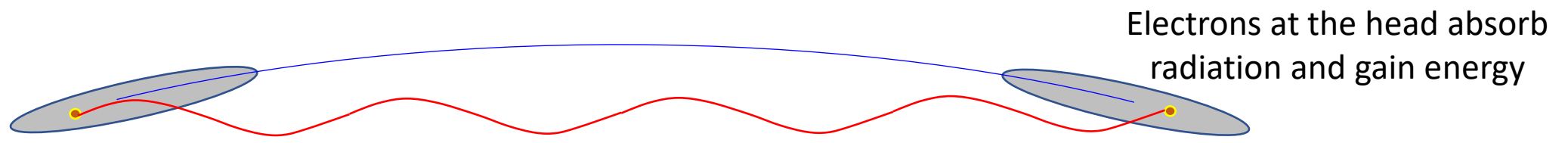
Exit of linac



After compression

Coherent Synchrotron Radiation

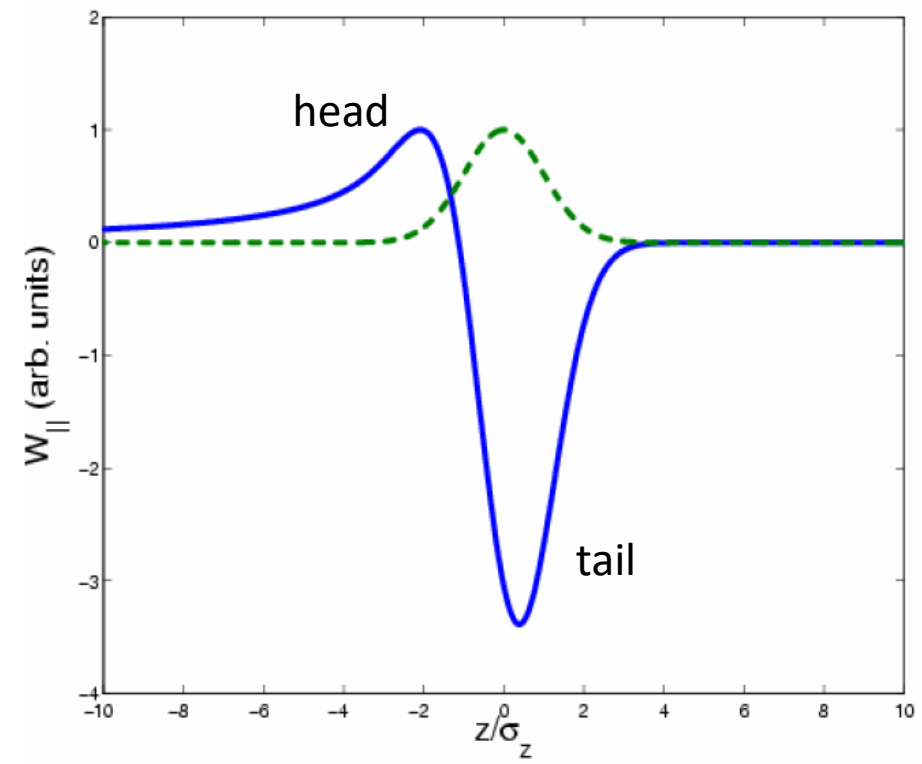
Coherent Synchrotron Radiation



Electrons in the back of the bunch emit radiation and lose energy

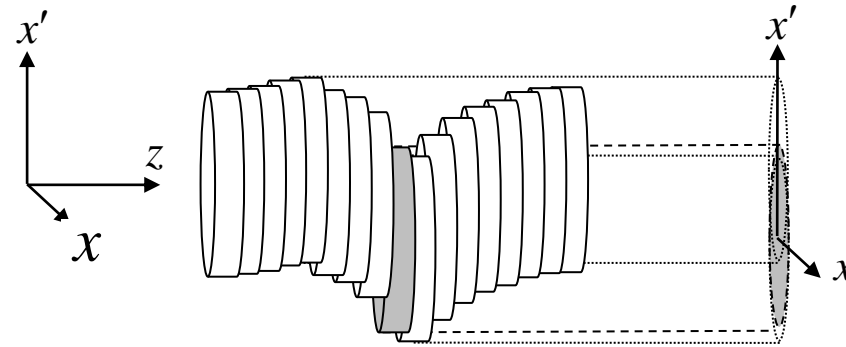
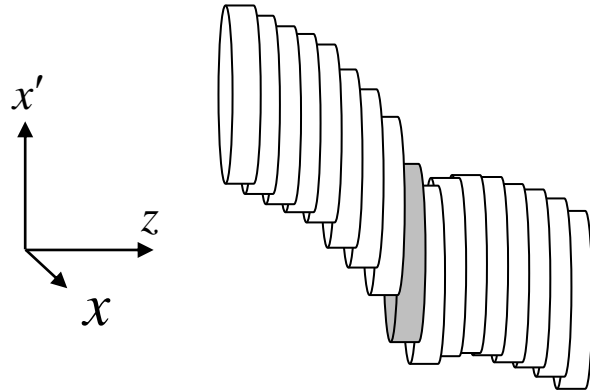
For electron bunches with Gaussian distribution and bunch length longer than the critical wavelength of the synchrotron radiation, the total energy loss can be expressed as

$$\left(\frac{\Delta E}{E}\right)_{CSR} \approx \left\{ \frac{5 Q R^{1/3} \theta}{\sigma_z^{4/3} E_c} \right\} \text{Int} \left(\frac{s}{\sigma_z} \right)$$



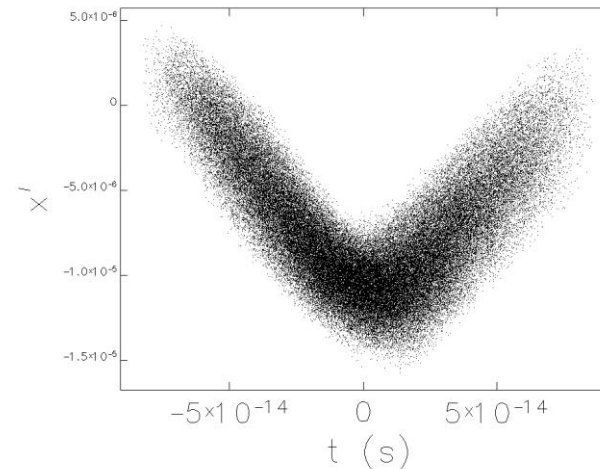
Emittance Growth

CSR wake and dispersion cause the trace space of different slices to spread out in x' - x space



$$\Delta x = R_{16} \left(\frac{\Delta \gamma}{\gamma} \right)_{CSR}$$

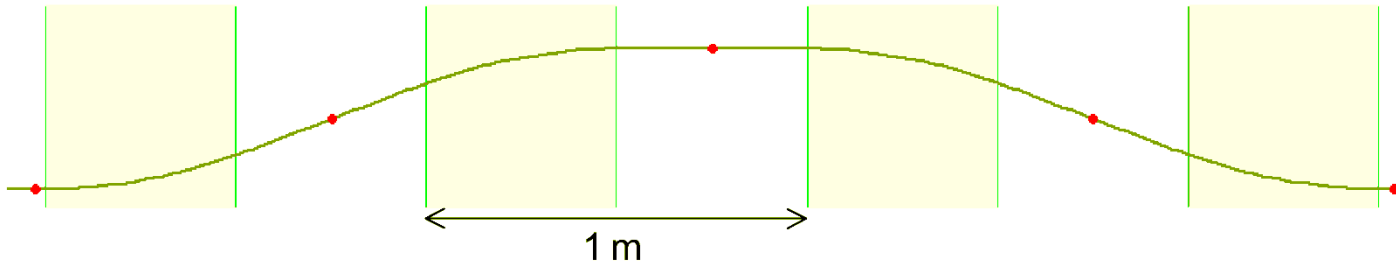
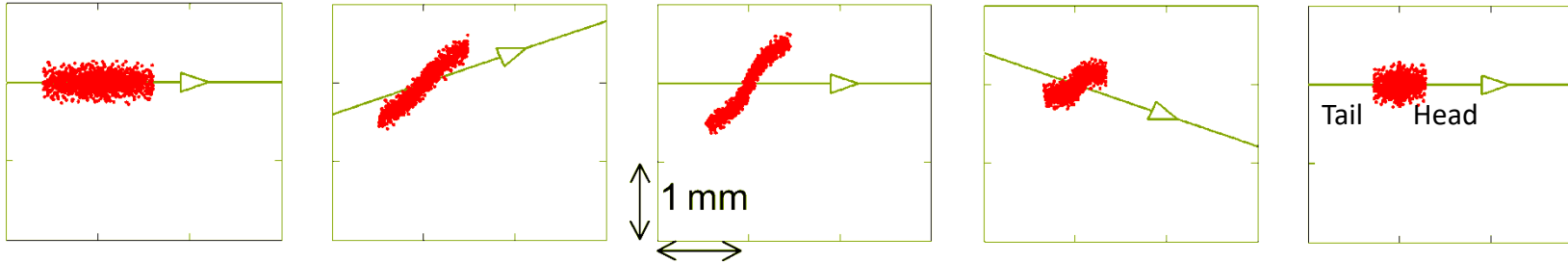
$$\Delta x' = R_{26} \left(\frac{\Delta \gamma}{\gamma} \right)_{CSR}$$



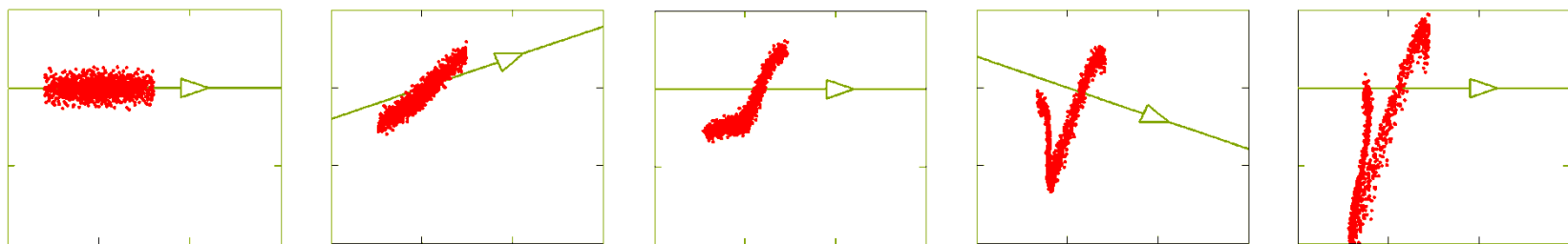
output phase space--input: L01BC.ele lattice: L01BC.lte

Compression with no CSR and with CSR

without self-interaction

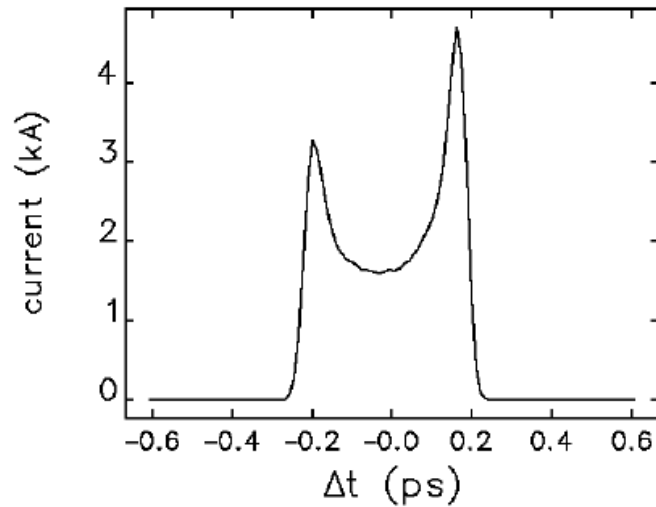
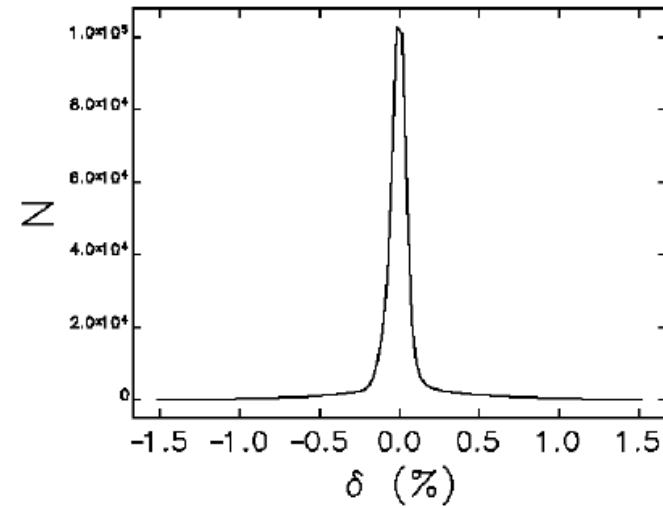
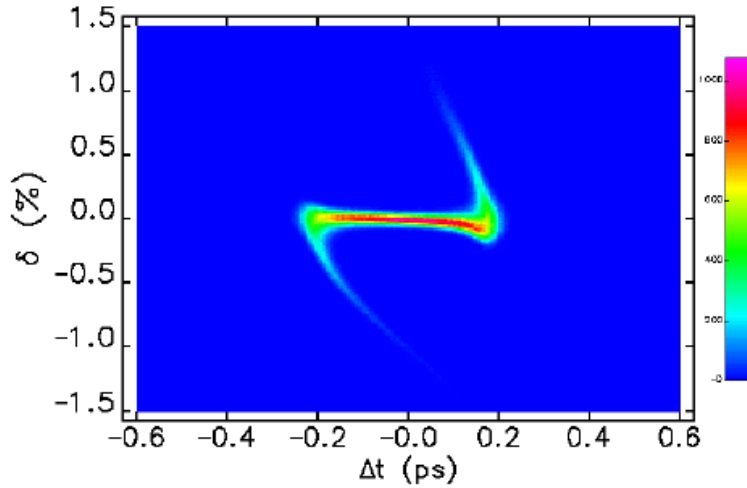


with self-interaction

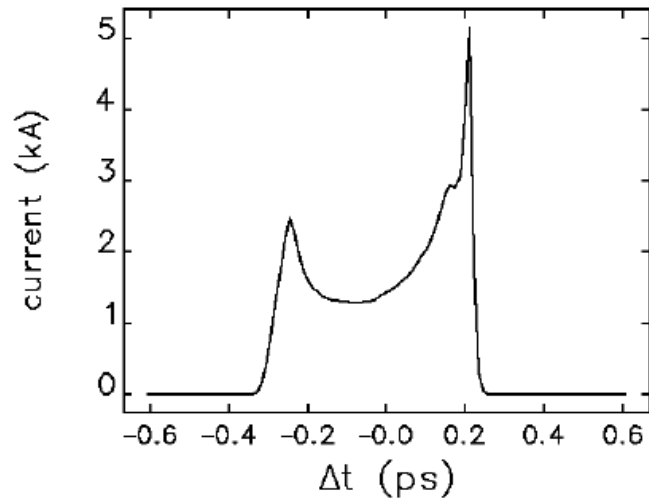
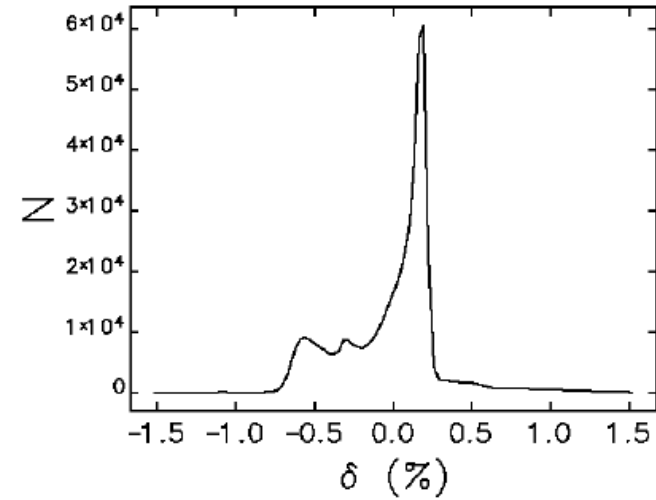
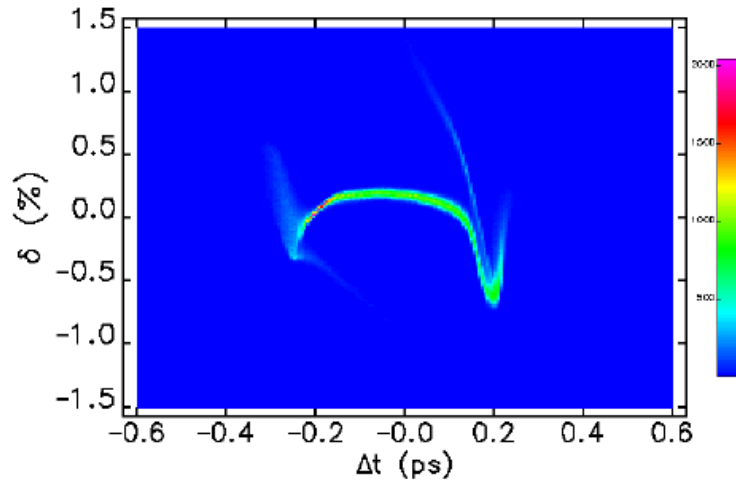


Center & tail lose energy

Bunch Compression without CSR

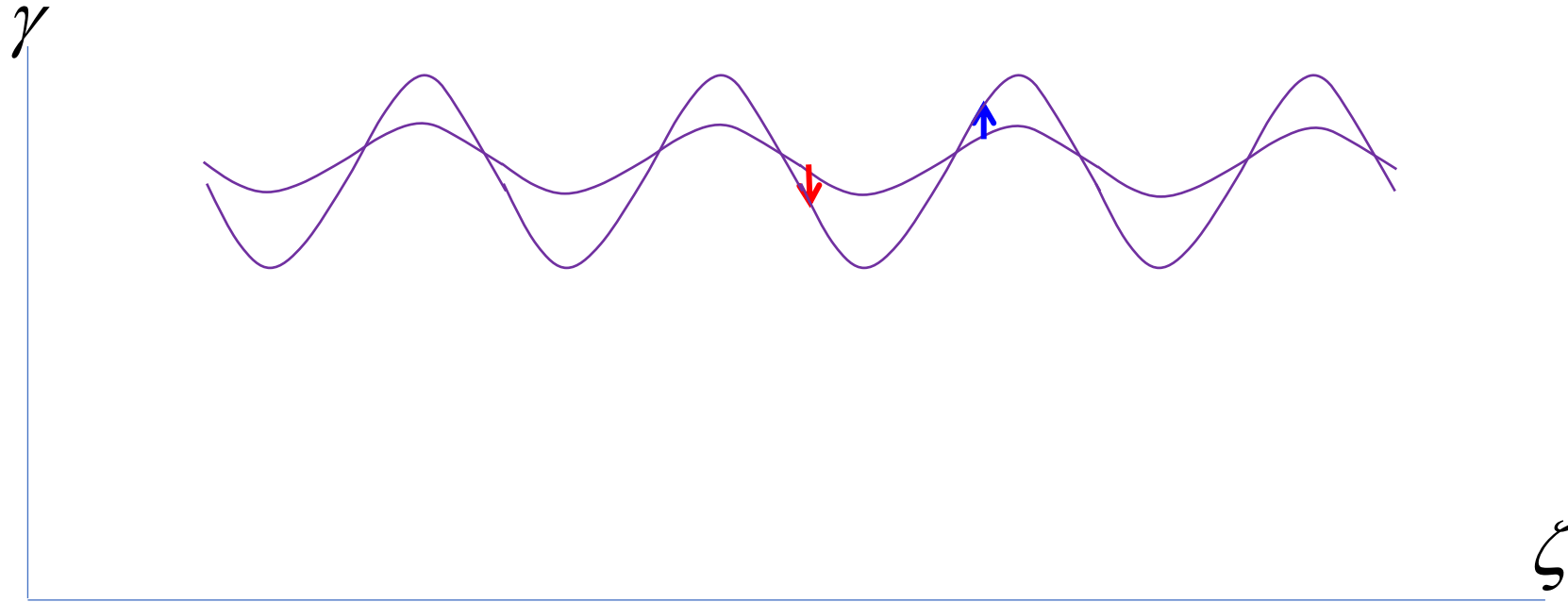


Bunch Compression with CSR



Microbunching Instabilities & Laser Heaters

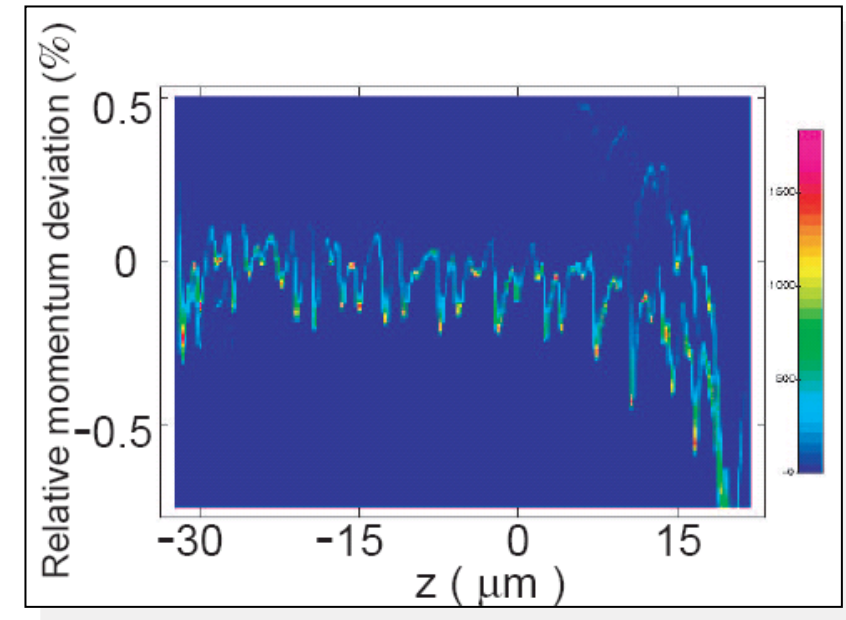
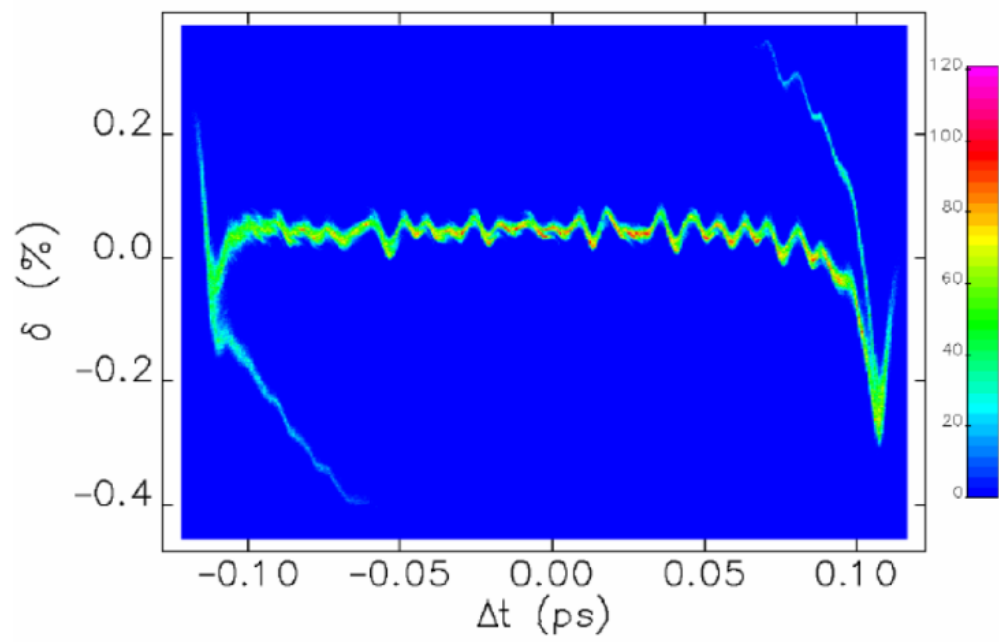
Longitudinal Space Charge



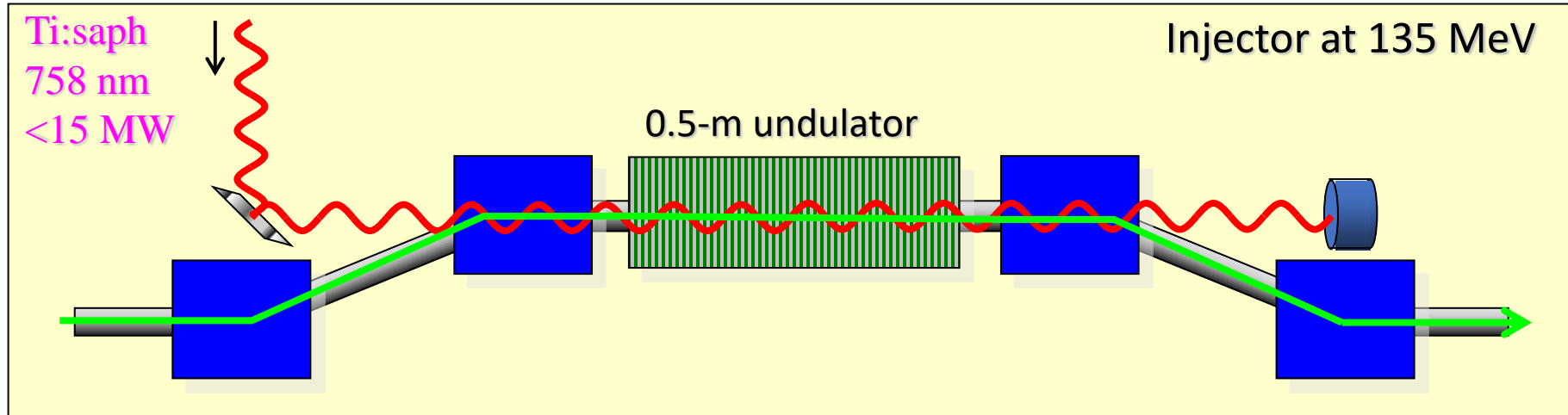
Longitudinal space charge increases the initial small energy modulations which grow with time.

Chicanes convert energy modulations into density modulations and thus magnify the microbunching instabilities.

Microbunching Instabilities

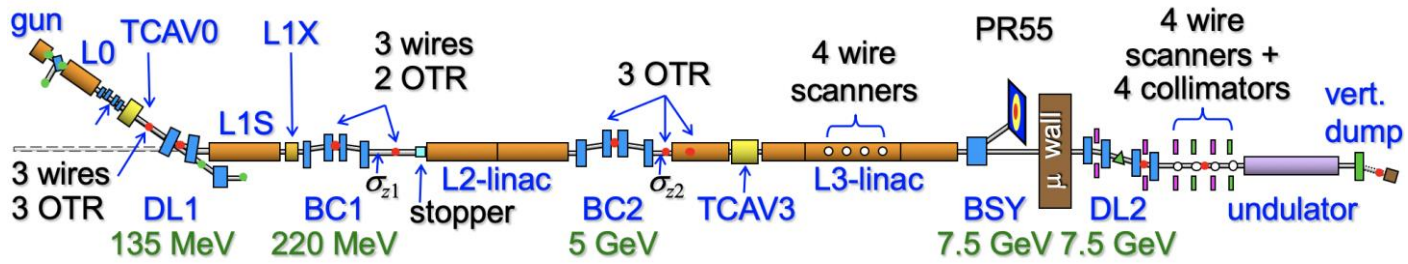
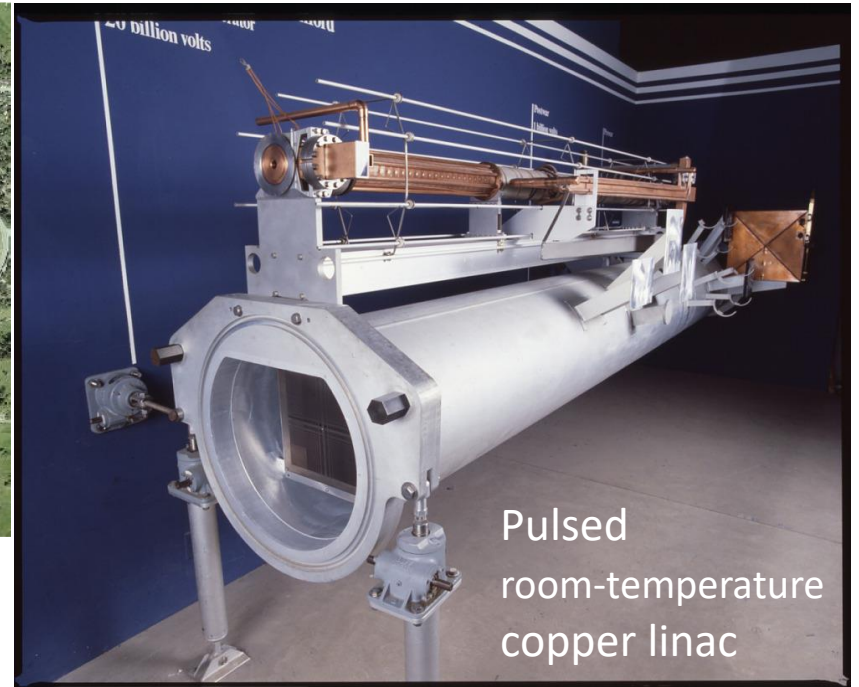
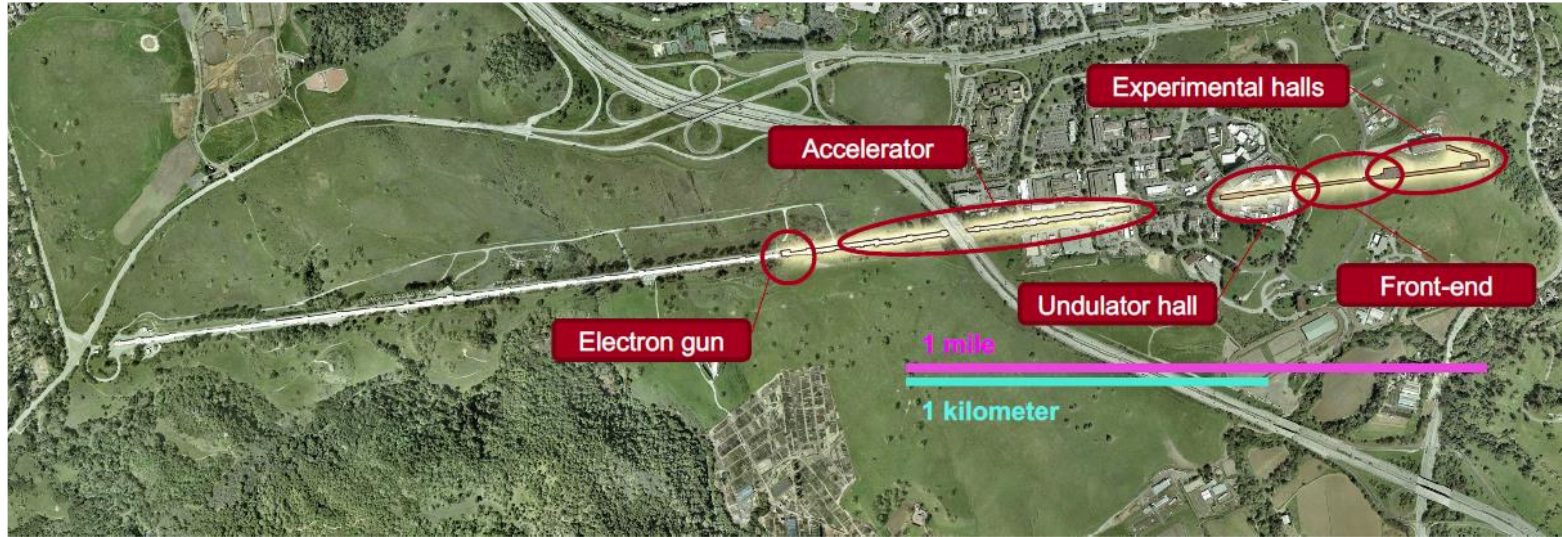


LCLS Laser Heater



Machine Layout

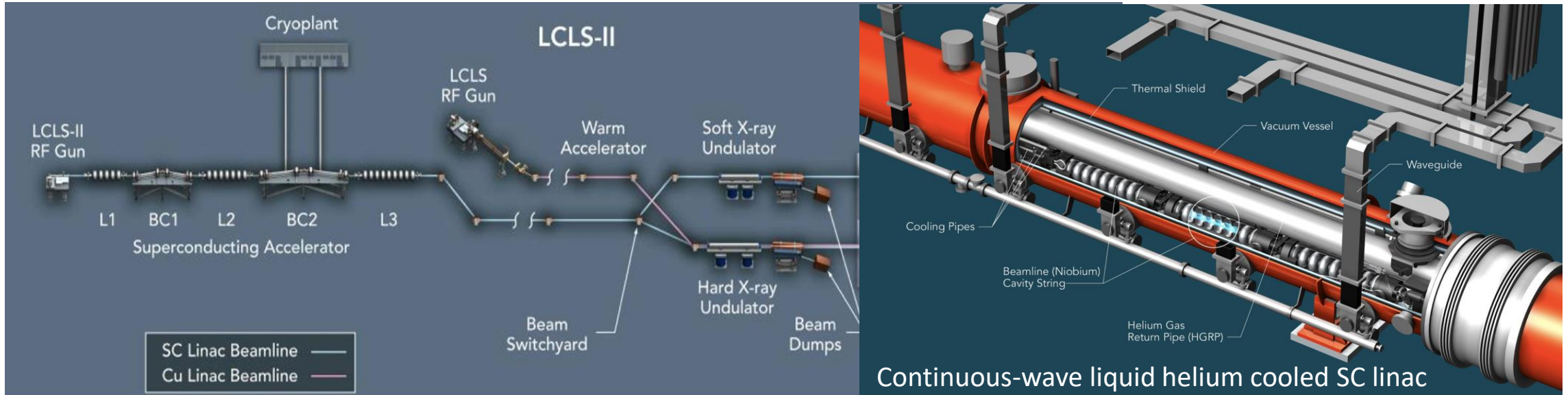
LCLS Copper Linac X-ray FEL at SLAC



120-Hz X-ray pulse repetition rate

Photoinjector	Injector Linac	Laser Heater	Linac 1	BC1	Linac 2	BC2	Linac 3	Undulators
1.6-cell NC Cu 2.856 GHz	NC Cu S-band 2.856 GHz	760 nm	NC Cu S-band X-band linearizer	$R_{56} = -45.5\text{mm}$	NC Cu 2.856 GHz	$R_{56} = -24.7\text{mm}$	NC Cu 2.856 GHz	Hybrid PMU HXR (v) SXR (h)
6 MeV	135 MeV	135 MeV	250 MeV	250 MeV	5 GeV	5 GeV	15 GeV	25 keV

LCLS-II and LCLS-II-HE at SLAC



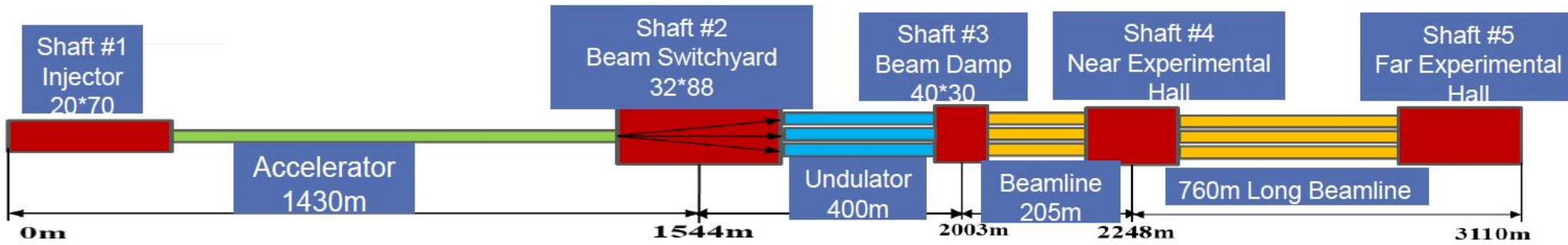
Continuous-wave liquid helium cooled SC linac

	SC Linac	Beam energy
LCLS-II	Injector, L1, L2, L3	4 GeV
LCLS-II-HE	Additional CM in L3, L4	8 GeV

High-repetition-rate (<1 MHz) X-ray pulses

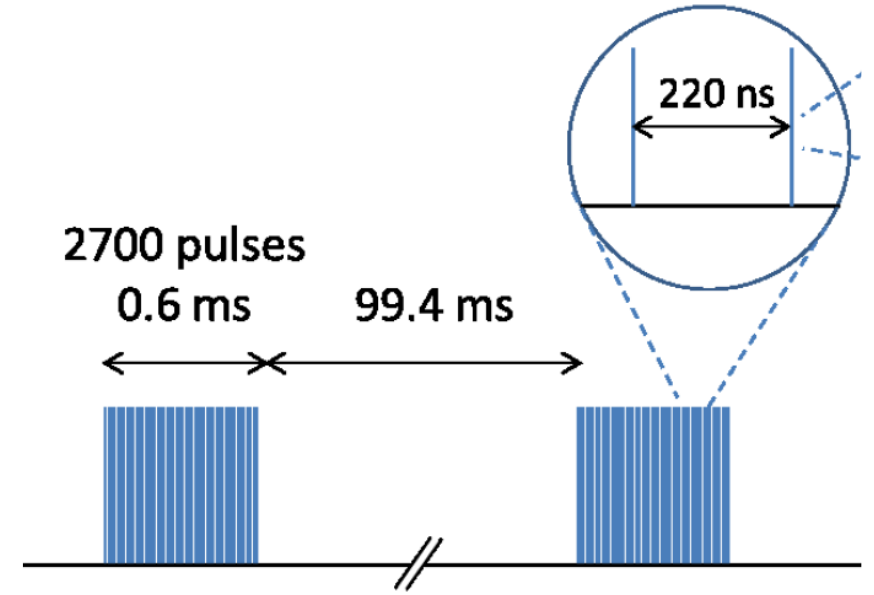
Photoinjector	Injector Linac	Laser Heater	Linac 1	BC1	Linac 2	BC2	Linac 3 & Linac 4	Undulators
186-MHz gun + NC 1.3-GHz bunchers	SC Linac 1.3 GHz	$R_{56} = -3.5\text{mm}$	SC 1.3 GHz 3.9-GHz linearizer	$R_{56} = -55\text{mm}$	SC 1.3 GHz	$R_{56} = -37\text{mm}$	SC 1.3 GHz	Hybrid PMU HXR (v) SXR (h)
0.75 MeV	100 MeV	100 MeV	250 MeV	250 MeV	1.6 GeV	1.6 GeV	8 GeV	0.2 - 20 keV

SHINE XFEL at SINAP



Photoinjector	Injector Linac	Laser Heater	Linac 1	BC1	Linac 2	BC2	Linac 3 & Linac 4	Undulators
217-MHz gun + NC 1.3-GHz bunchers	SC Linac 1.3 GHz	1030 nm	SC 1.3 GHz 3.9-GHz linearizer	$R_{56} = -55\text{mm}$	SC 1.3 GHz	$R_{56} = -37\text{mm}$	SC 1.3 GHz	2 PMU lines 1 SCU line
0.75 MeV/2.4 MeV	100 MeV	100 MeV	270 MeV	270 MeV	1.5 GeV	1.5 GeV	8.6 GeV	0.4 - 25 keV

European X-ray FEL at DESY



SASE 1 has the XFEL highest photon energy

10-Hz macropulse repetition rate
4.5-MHz micropulse repetition rate

Photoinjector	Injector Linac	Laser Heater	BC0	Linac 1	BC1	Linac 2	BC2	Linac 3 & 4	Undulators
1.5-cell NC Cu 1.3 GHz	SC 1.3 GHz 3.9-GHz linearizer	1030 nm	$R_{56} = -150$ to -30mm	SC 1.3 GHz	$R_{56} = -120$ to -50mm	SC 1.3 GHz	$R_{56} = -80$ to -20mm	SC 1.3 GHz	SASE 1-3 HPMU
6 MeV	130 MeV	130 MeV	130 MeV	600 MeV	600 MeV	2.4 GeV	2.4 GeV	17.5 GeV	30 keV

Summary

- X-ray FELs use multi-stage compression to shorten the ps electron bunches from the photoinjector to produce femtosecond bunches with kA peak current.
- Bunch compression is routinely performed with a chirper cavity and a chicane, sometimes in multiple stages through the linac, with counteracting effects of the non-linearities in the cavity (RF curvature), wake field and harmonic linearizer.
- CSR introduces emittance growth and energy spread in the compressed bunch.
- Microbunching instabilities can be mitigated by using a laser heater to increase the energy spread of the low-energy beam to reduce longitudinal space charge.