

# Neutrino oscillation phenomenology at long-baseline experiments

Pilar Coloma



FNAL theory seminar

Feb 16<sup>th</sup>, 2014

# Current status in neutrino oscillations

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Atmospheric
Reactor/Interference
Solar

$$\theta_{12} \sim 33^\circ$$

$$\theta_{23} \sim 45^\circ$$

$$\theta_{13} \sim 8.5^\circ$$

$$\Delta m_{21}^2 \sim 7.5 \times 10^{-5} \text{eV}^2$$

$$\Delta m_{31}^2 \sim \pm 2.45 \times 10^{-3} \text{eV}^2$$

Gonzalez-Garcia, Maltoni, Schwetz, 1409.5439 [hep-ph]

(see also Capozzi et al 1312.2878 [hep-ph] and Forero et al, 1405.7540[hep-ph])

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$$\theta_{12} \sim 33^\circ \pm 3^\circ$$

$$\theta_{23} \sim 45^\circ \pm 8^\circ$$

$$\theta_{13} \sim 8.5^\circ \pm 1^\circ$$

$$\Delta m_{21}^2 \sim (7.5 \pm 0.5) \times 10^{-5} \text{eV}^2$$

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Unknowns:

$\delta$  ?

Octant of  $\theta_{23}$  ?

Mass ordering ?

New Physics ?

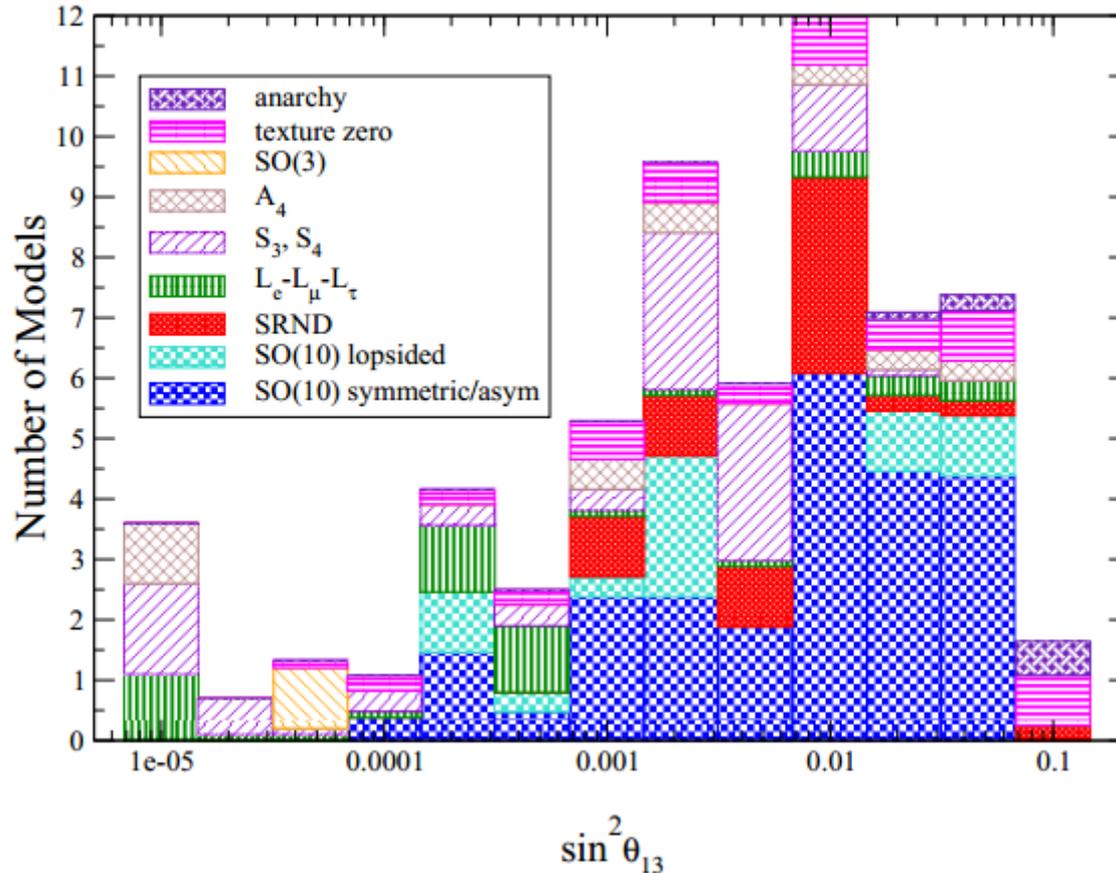
Majorana/Dirac ?

Gonzalez-Garcia, Maltoni, Schwetz, 1409.5439 [hep-ph]

(see also Capozzi et al 1312.2878 [hep-ph] and Forero et al, 1405.7540[hep-ph])

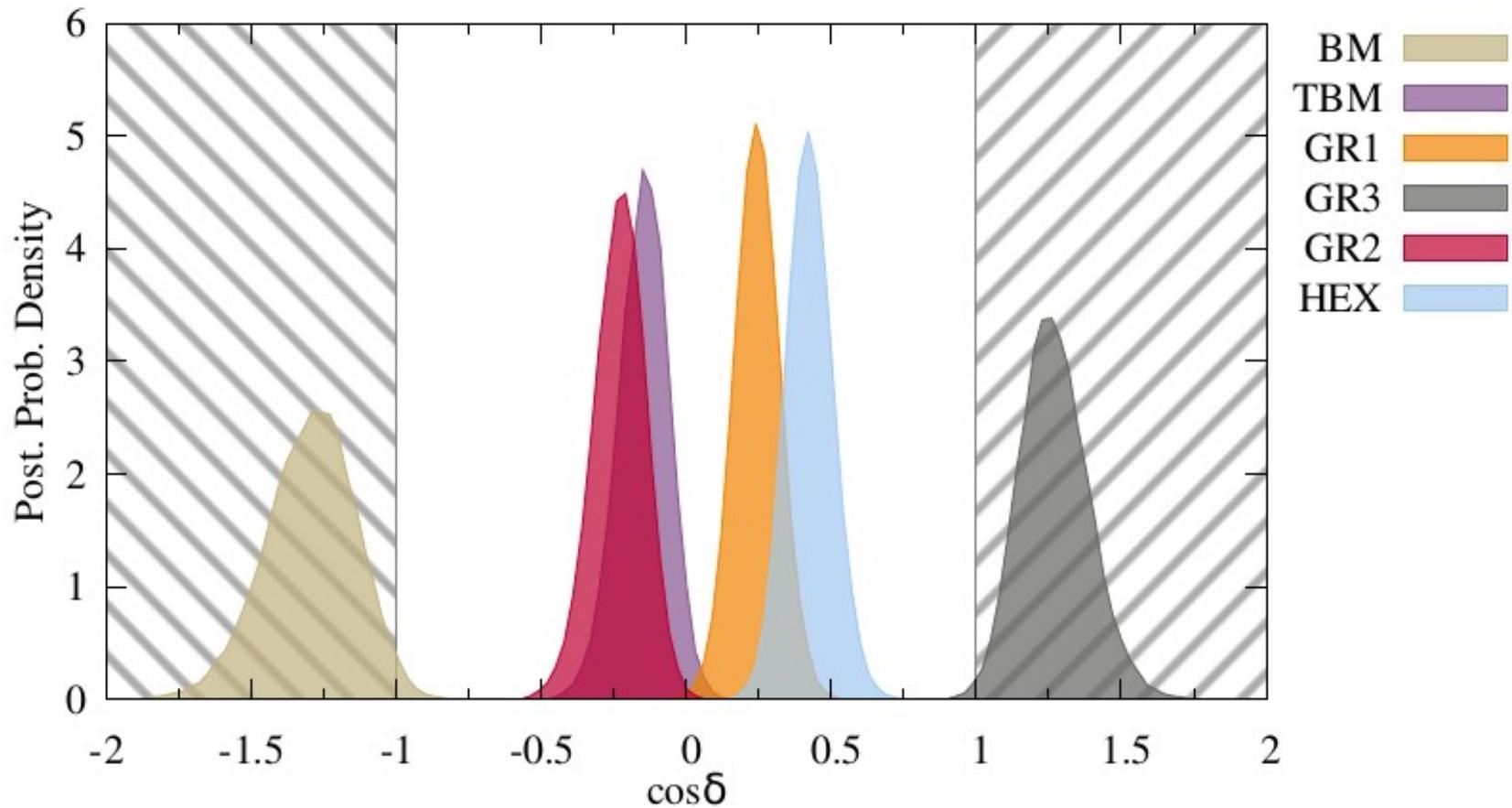
# Why precision?

Predictions of All 63 Models



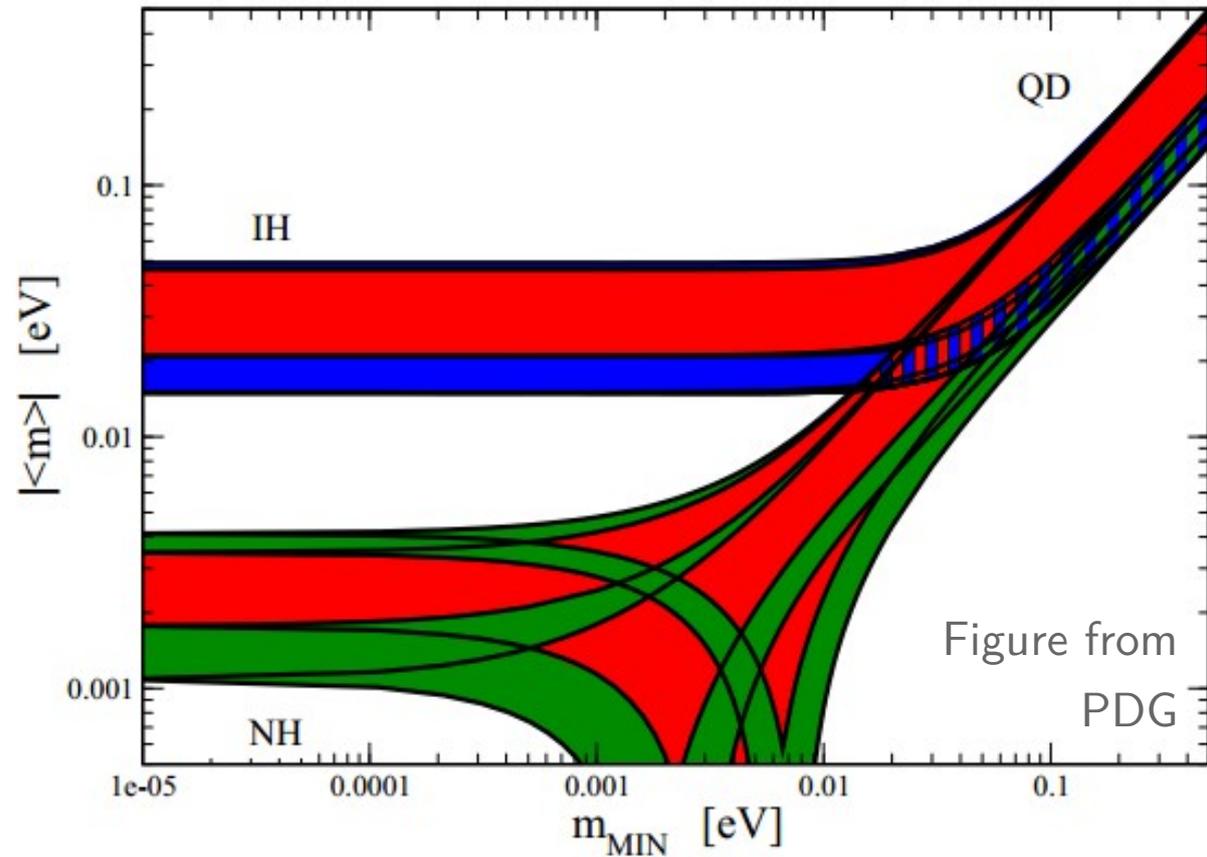
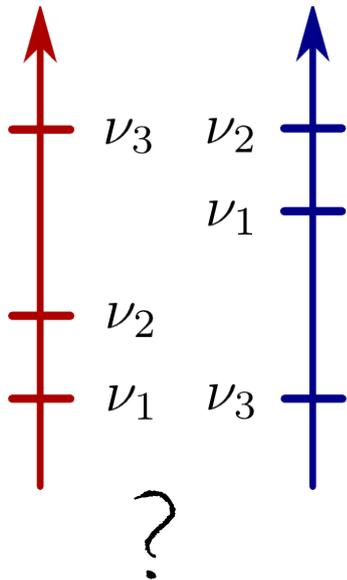
Albright and Chen, hep-ph/0608137, and Albright, 0911.2437  
 (see also, e.g., Albright, Dueck and Rodejohann, 1004.2798)

# Why precision?

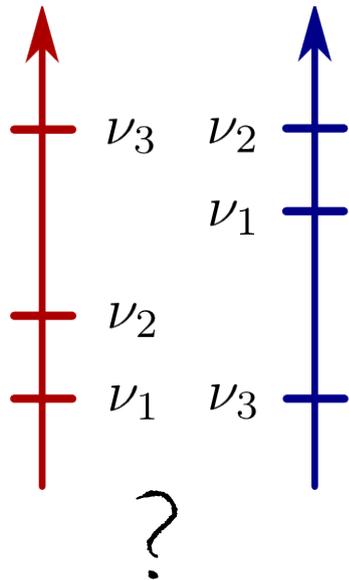


Ballett, King, Luhn, Pascoli, Schmidt, 1410.7573 [hep-ph]  
(see also, e.g., Girardi et al, 1410.8056, Meloni, 1308.4578)

# Importance of mass ordering



# Importance of mass ordering



## Normal $3\nu$ Spectrum

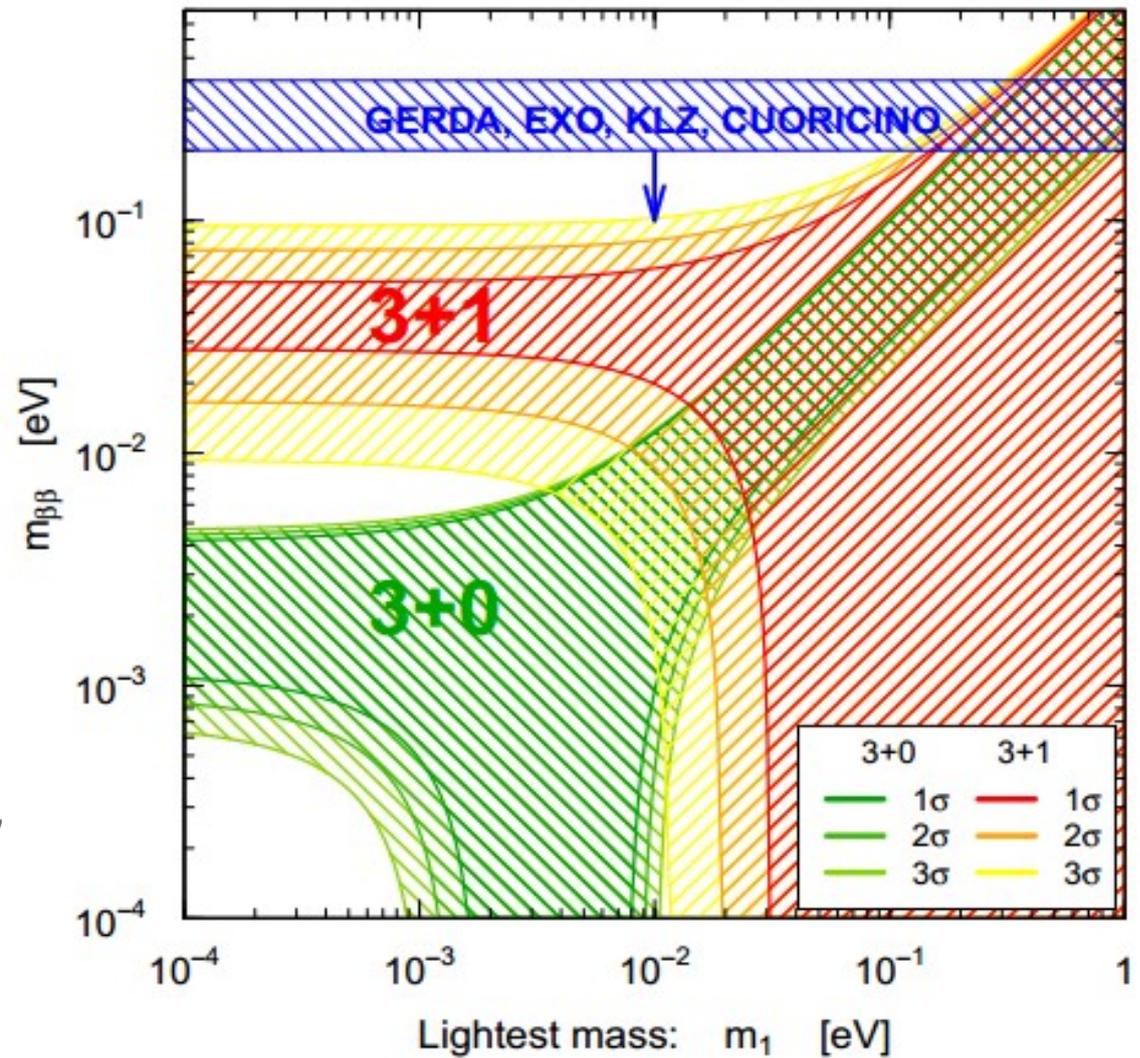
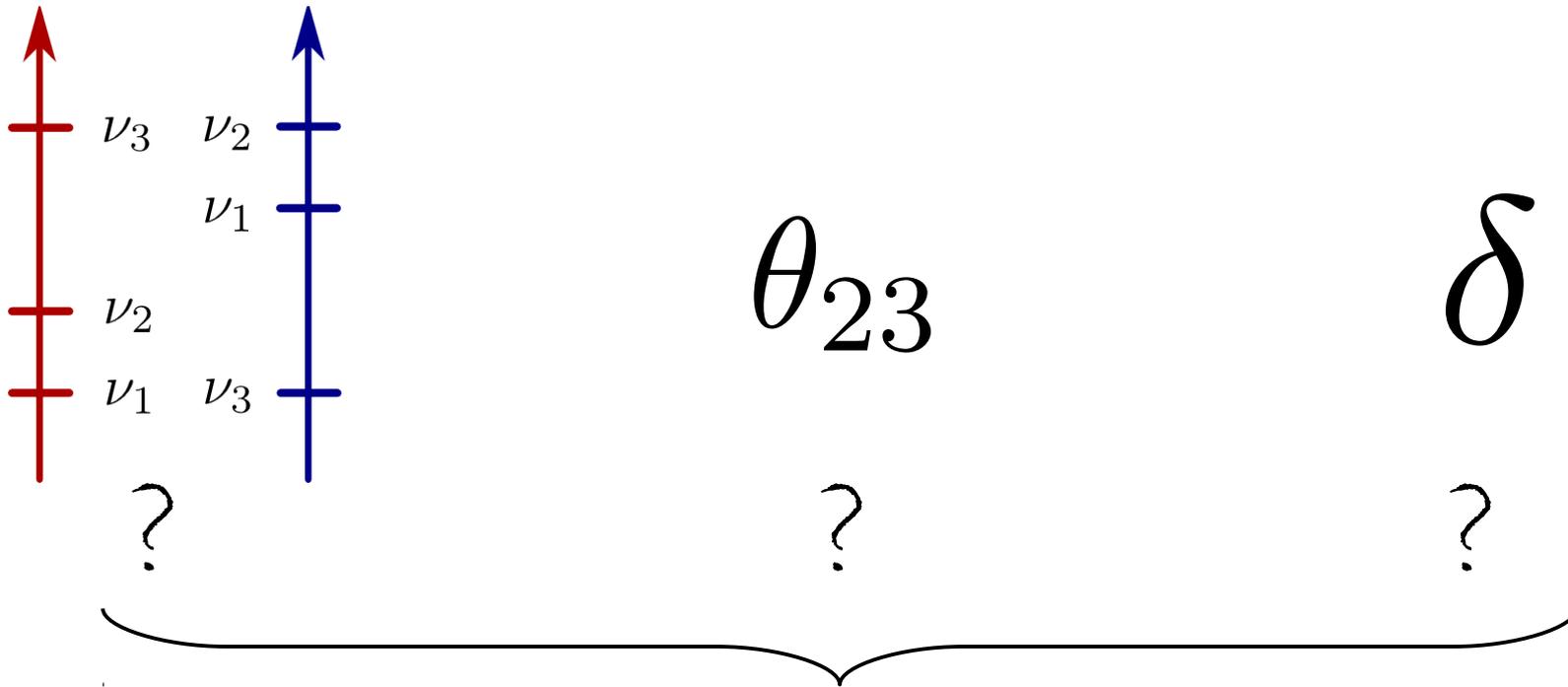


Figure taken from  
 Giunti's talk at NuPhys 2014  
 (see also Bilenky et al, hep-ph/0104218,  
 or Blennow et al, 1005.3240, among  
 others)

# Degeneracies



$$P(\nu_\mu \rightarrow \nu_e)$$

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$$

# Outline

- Introduction to long-baseline experiments
- CP violation searches and delta
- Precise determination of  $\theta_{23}$
- Determination of mass ordering
- Challenges for the future
- Summary

# The very basics

$$\pi^+ \rightarrow \mu^+ \nu_\mu \quad \left\{ \begin{array}{l} \nu_\mu \longrightarrow \nu_e \\ \nu_\mu \longrightarrow \nu_\mu \end{array} \right.$$

Problems:

$$\pi^- \rightarrow \mu^- \bar{\nu}_\mu$$

$$K^+ \rightarrow e^+ \nu_e$$

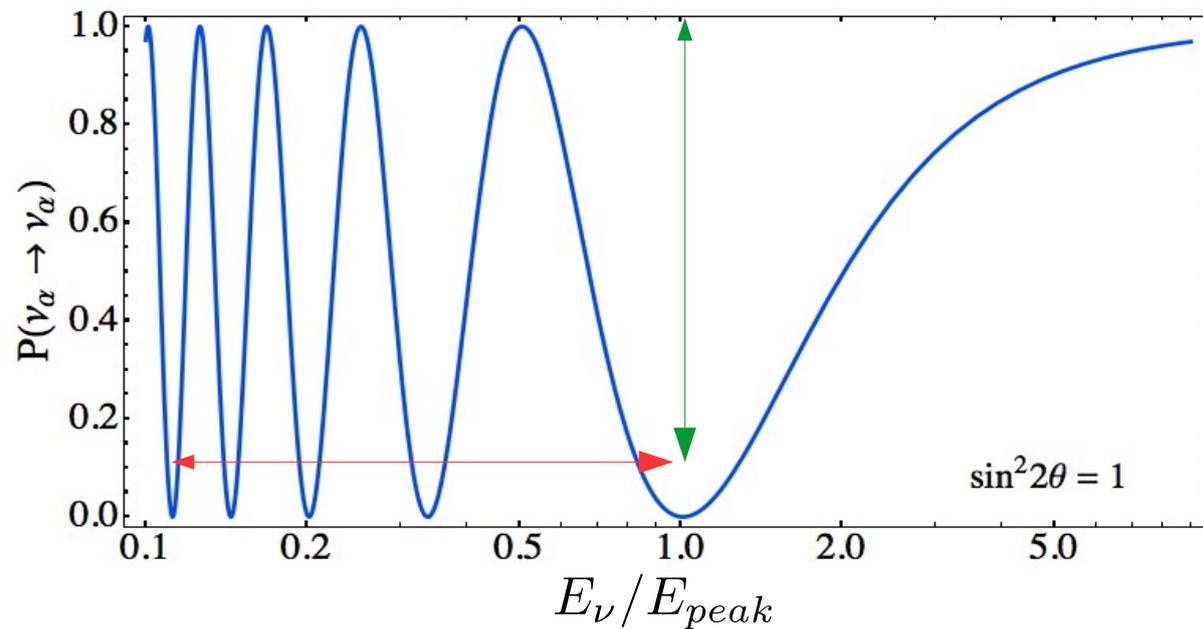
$$K^- \rightarrow e^- \bar{\nu}_e$$

**NOTE: None of these fluxes can be computed analytically!**

# The very basics

$$P_{\alpha\alpha} = 1 - \sin^2(2\theta_{\alpha\alpha}) \sin^2\left(\frac{\Delta m_{\alpha\alpha}^2 L}{4E}\right)$$

Tuned to be maximum



# CP violation searches

Three-family  $\nu_e$  appearance oscillation probability:

$$P_{\mu e} = (s_{23} \sin 2\theta_{13})^2 A_{atm}^2 \\ + \epsilon \sin 2\theta_{23} \sin 2\theta_{13} c_{13} A_{atm} A_{sol} \cos(\pm\delta + \Delta_{31}) \\ + O(\epsilon^2)$$

Nu/ Nubar



$$\Delta_{31} \equiv \frac{\Delta m_{31}^2 L}{4E}$$

Cervera et al, hep-ph/0002108  
(see also Asano and Minakata, 1103.4387)

# 1<sup>st</sup> vs 2<sup>nd</sup> oscillation maxima

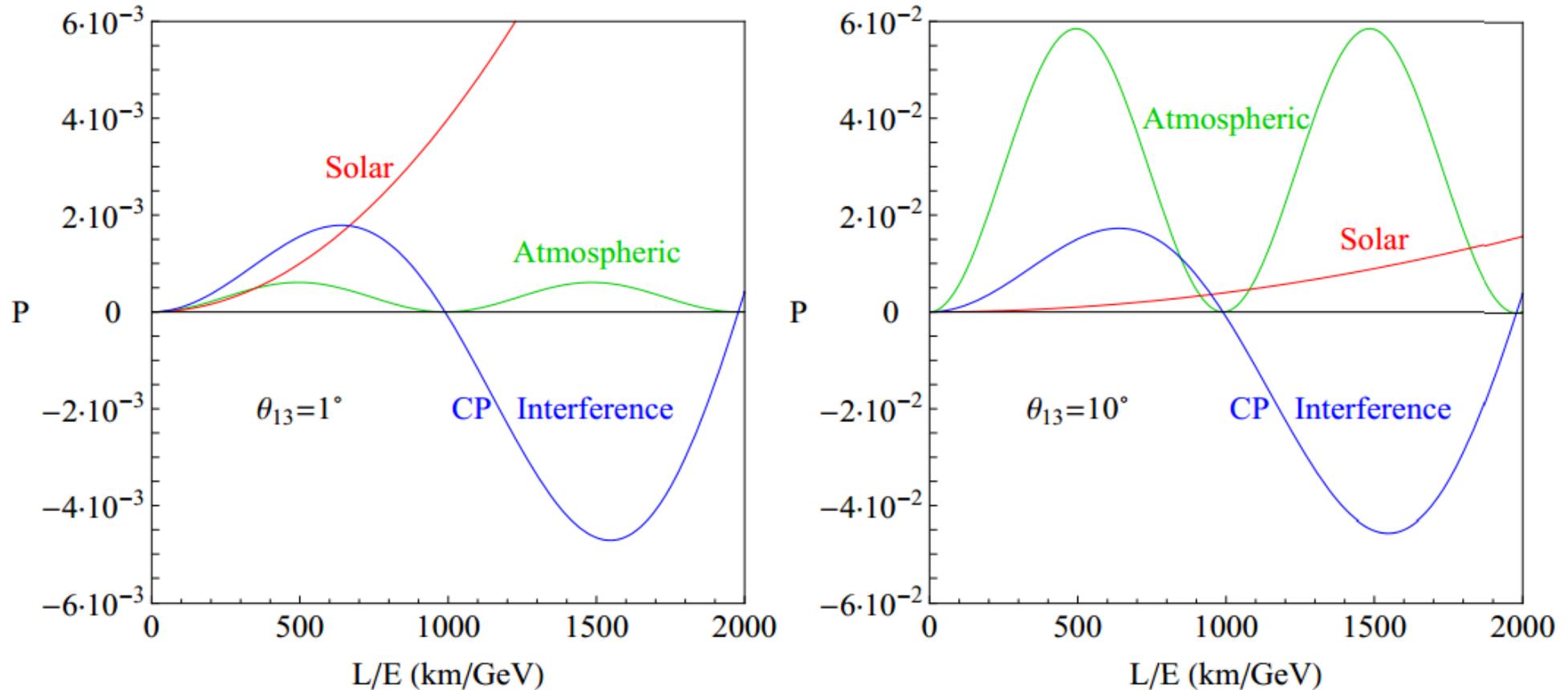
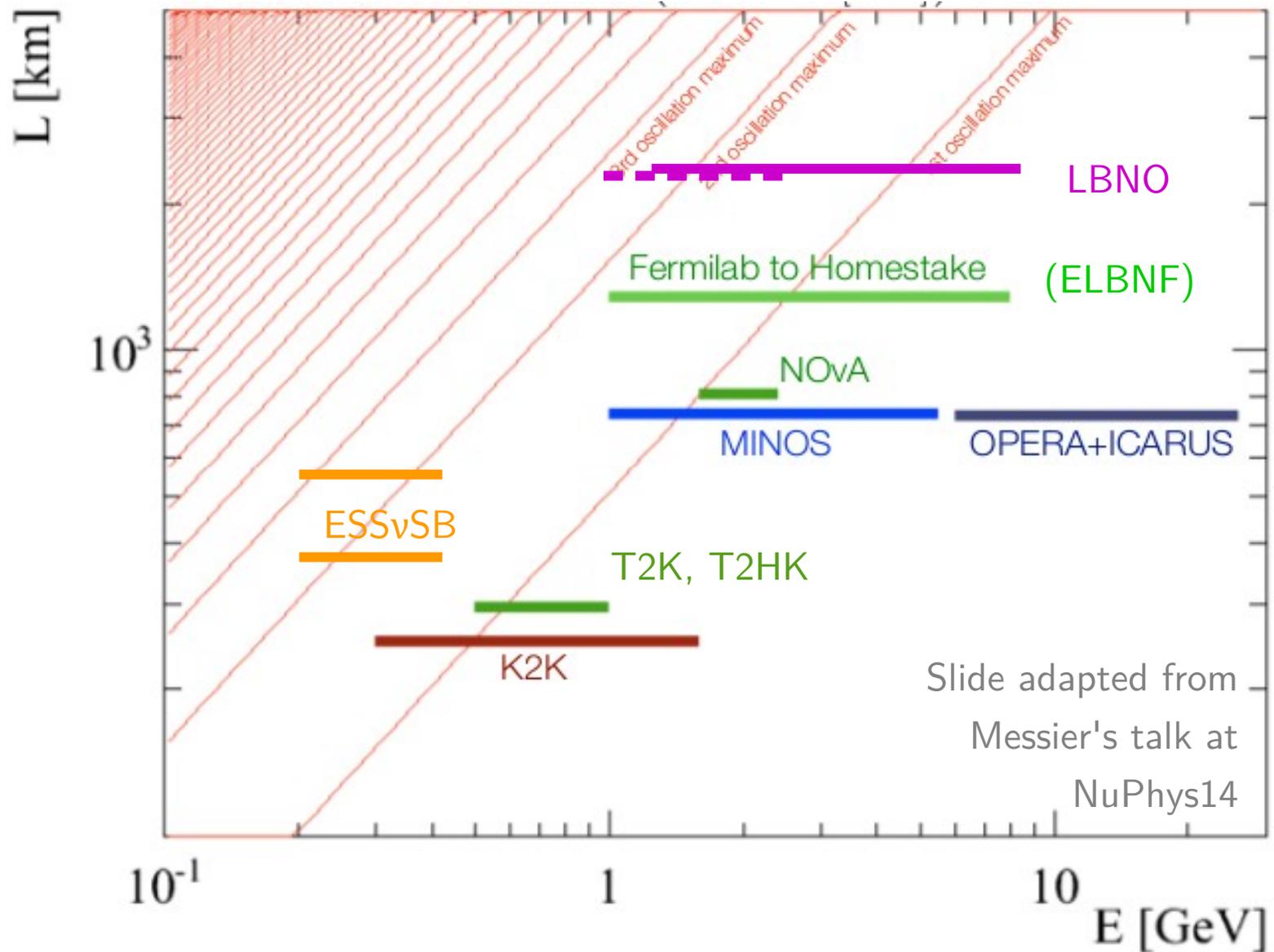


Figure from Coloma and Fernandez-Martinez, 1110.4583 [hep-ph].

See also: Marciano, hep-ph/0108181, Ishitsuka et al, hep-ph/0504026, Mereaglia and Rubbia, 0801.4035

# Long-baseline experiments in the market



# Possible ways to search for CP violation

- **Rate comparison**

Typically off-axis

Tests differences between  $\nu$  and anti- $\nu$

Dependent on systematics

Prone to degeneracies

- **Spectral info**

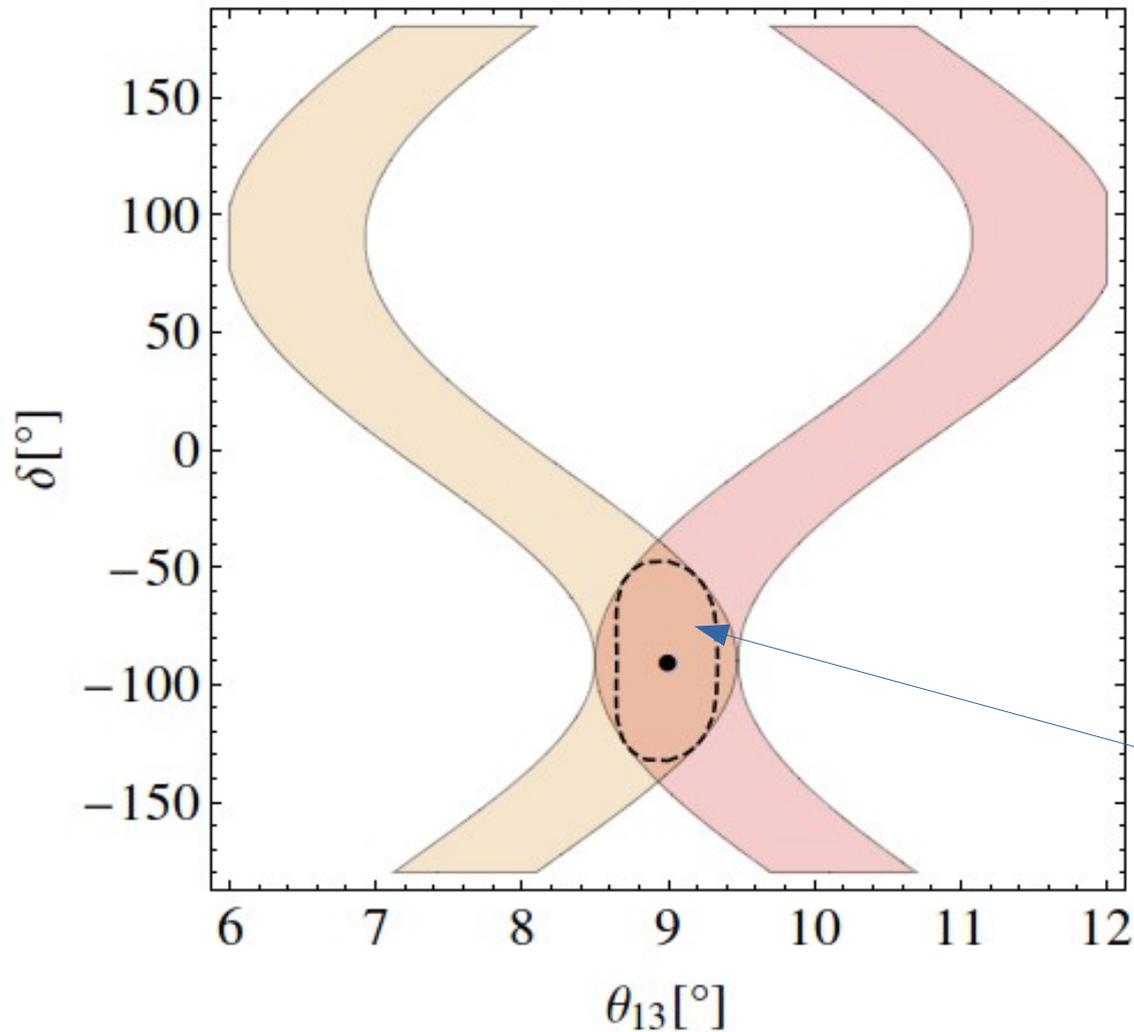
Typically wide-band beams

Tests the energy dependence of the oscillation probability

?

Degeneracies are easier to kill

# Rate info vs energy info



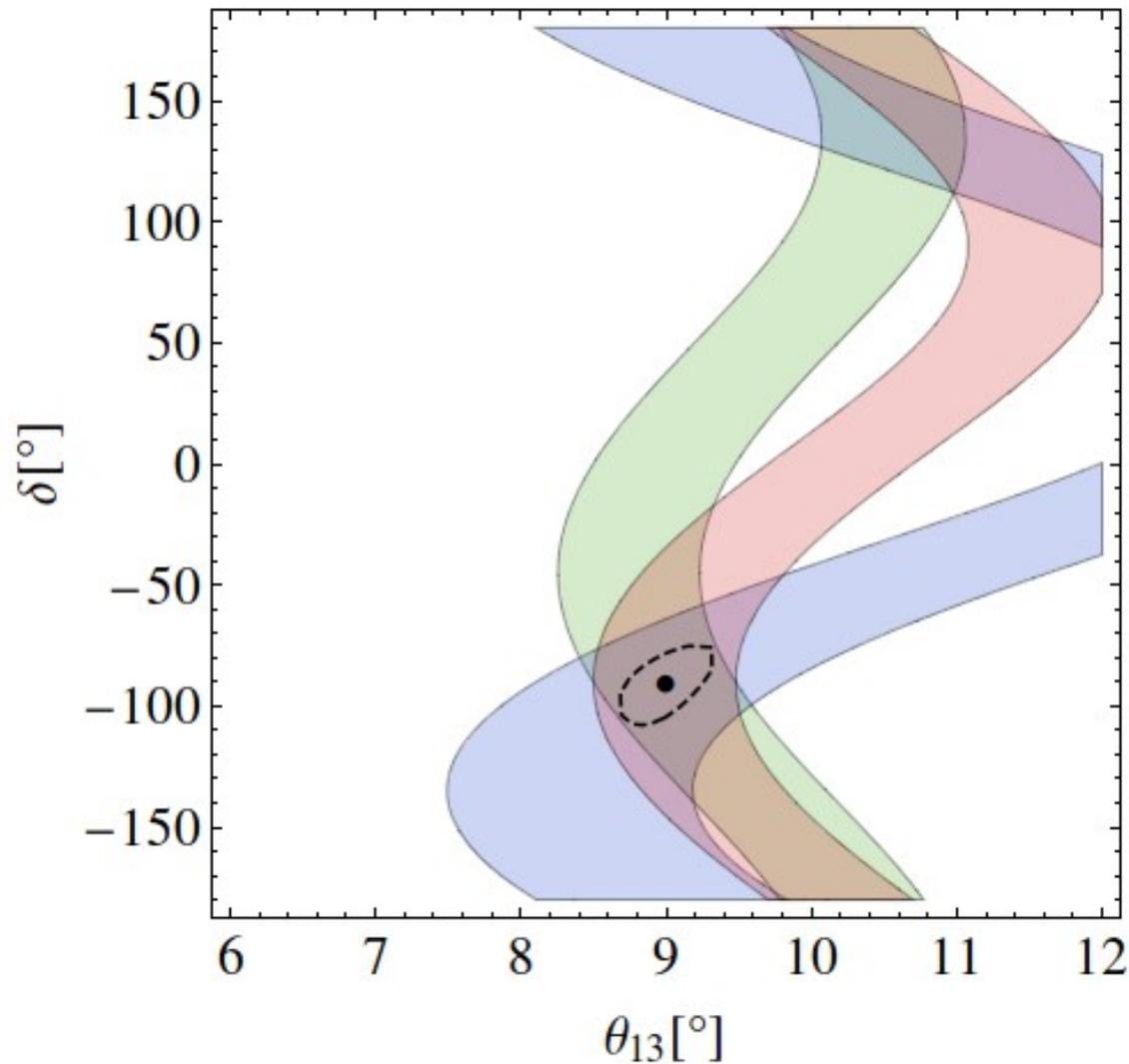
$$P_{\nu_\mu \rightarrow \nu_e}(\theta_{13}, \delta) = \overline{P}_\nu$$

$$E_\nu = E_{peak}$$

$$P_{\bar{\nu}_\mu \rightarrow \bar{\nu}_e}(\theta_{13}, \delta) = \overline{P}_{\bar{\nu}}$$

Allowed region

# Rate info vs energy info



$$P_{\nu_\mu \rightarrow \nu_e}(\theta_{13}, \delta) = \overline{P_\nu}$$

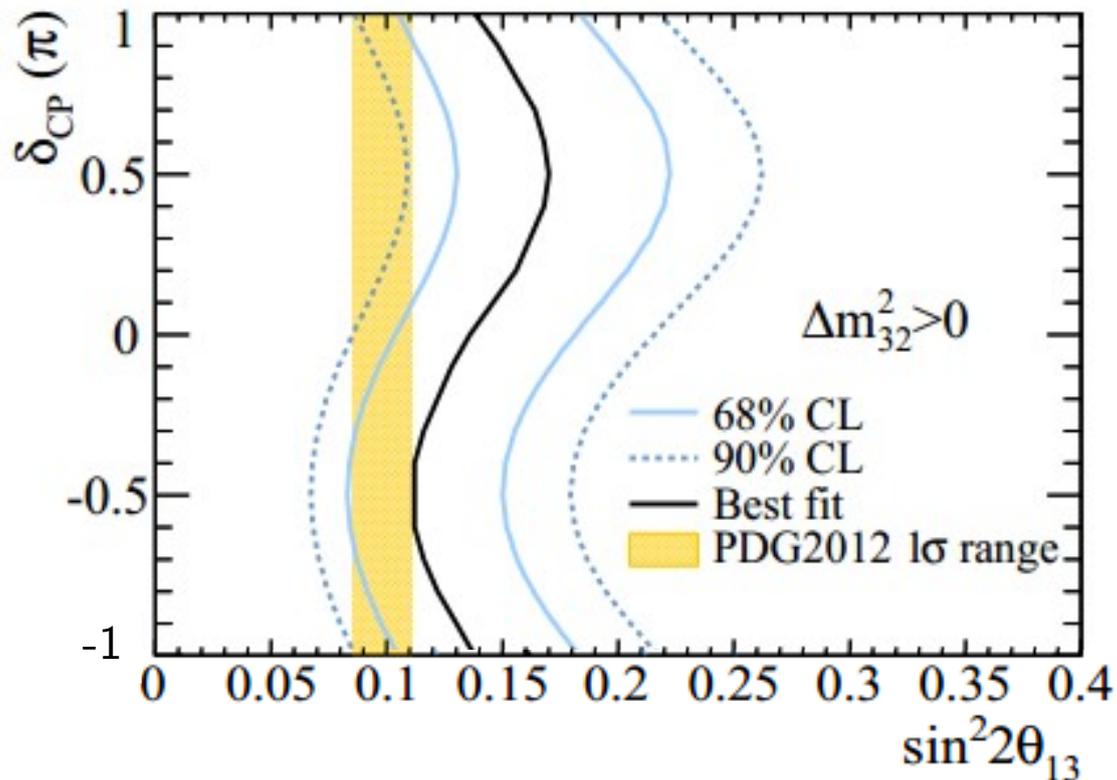
$$E_\nu = E_{peak}$$

$$E_\nu = 2E_{peak}$$

$$E_\nu = 0.6E_{peak}$$

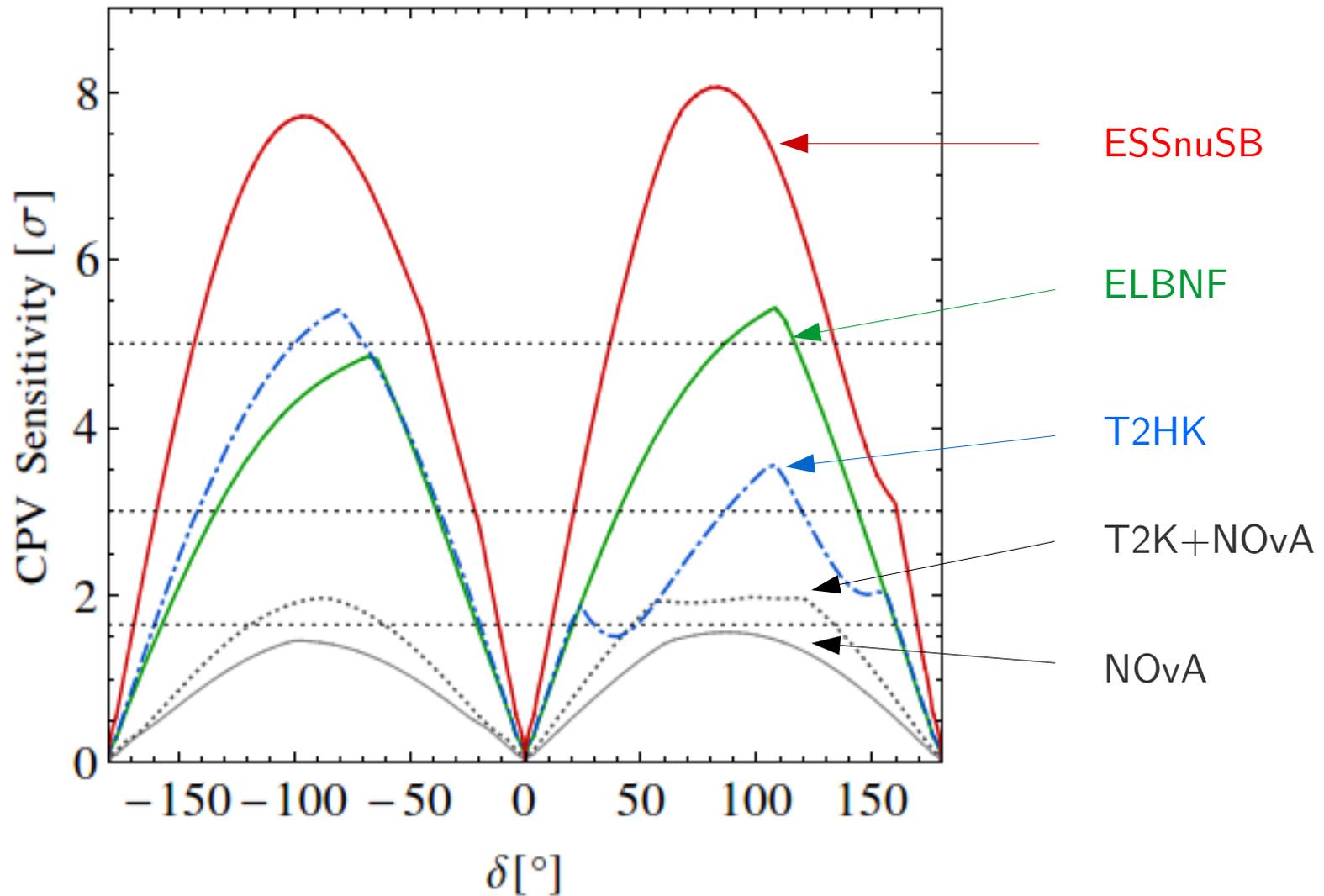
# The current hint for CP violation

The combination of current T2K and Daya Bay (mainly) seems to indicate that delta is not CP conserving:



T2K coll., 1311.4750 (see  
also 1502.01550)

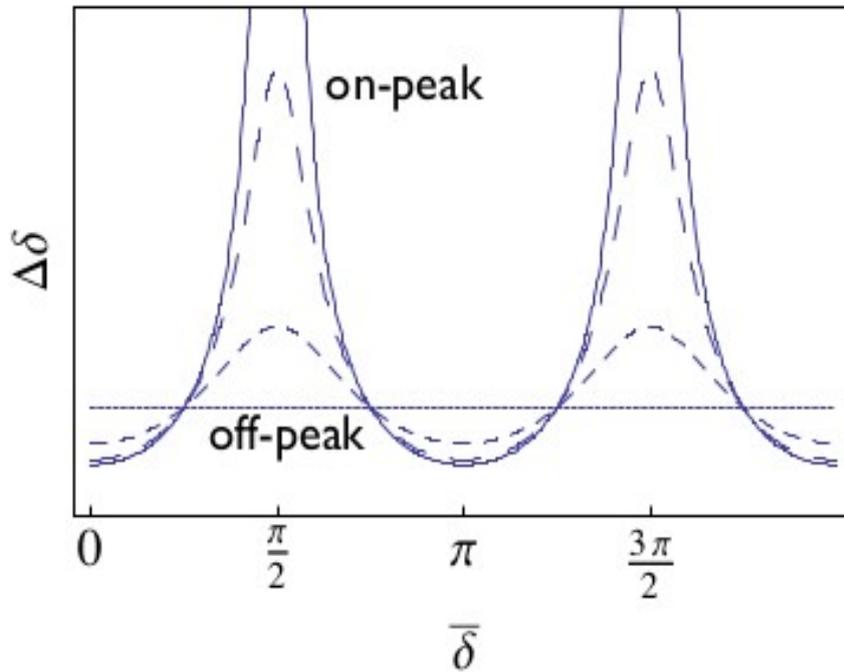
# CP violation prospects



# Precision on $\delta$

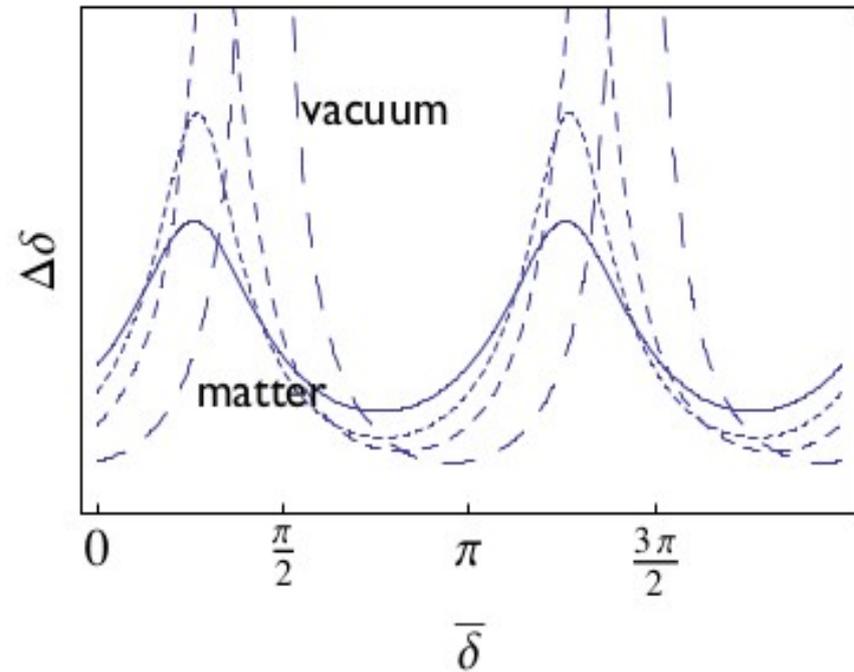
VACUUM

$$(\Delta\delta)_{\pm} \propto [\sin(\Delta \mp \delta)]^{-1}$$



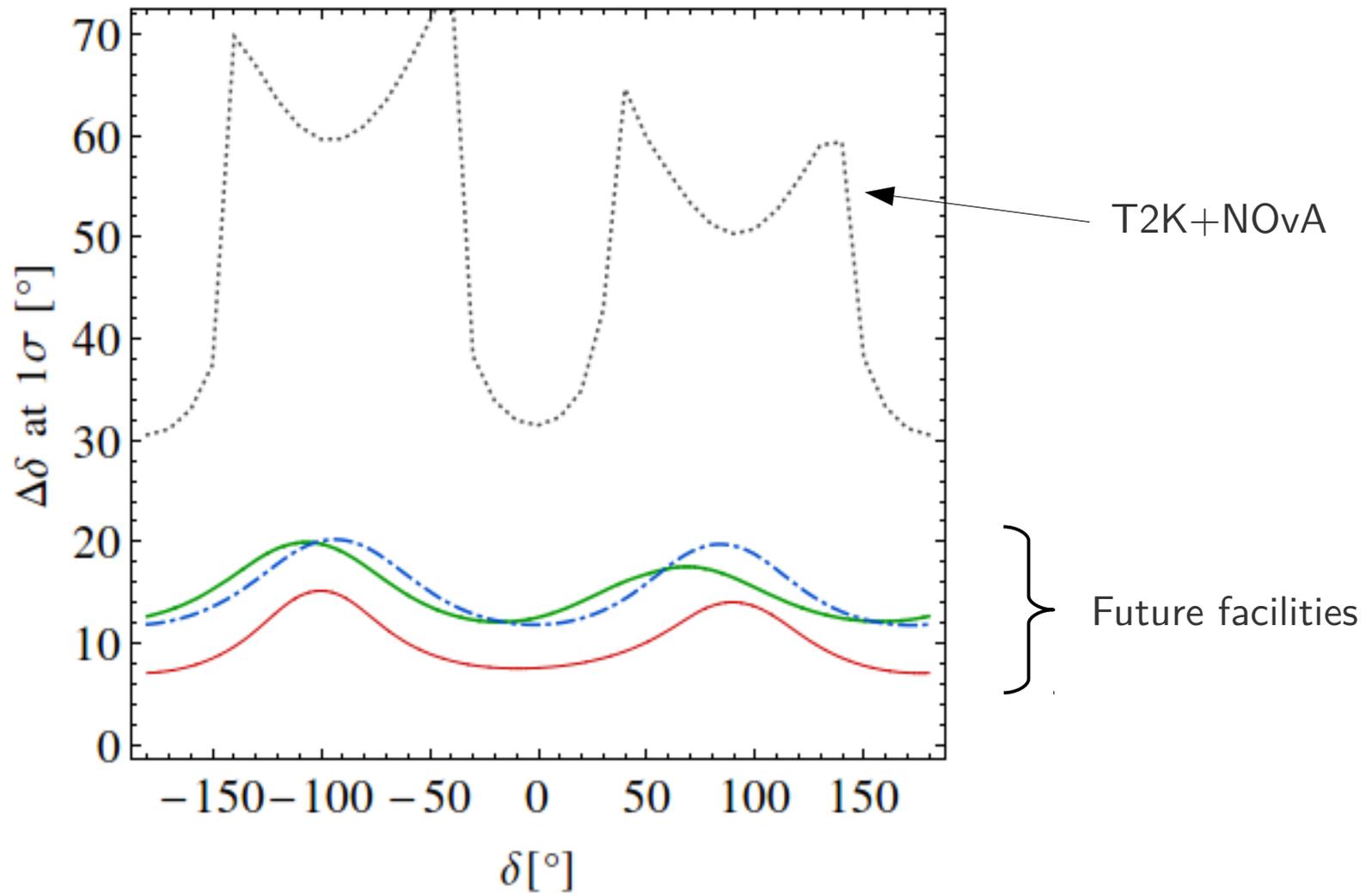
MATTER

$$(\Delta\delta)_{\pm} \propto \left[ \sin \left( \Delta \frac{\hat{A}}{1 \mp \hat{A}} \mp \delta \right) \right]^{-1}$$



Coloma, Donini, Fernandez-Martinez, Hernandez, 1203.5651 [hep-ph]

# Precision on $\delta$



theta23

Recent literature:

Agarwalla, Prakash, Sankar, 1304.3251 and 1301.2574

Ghosh, Ghoshal, Goswami, Raut, 1306.2500 and 1308.5979

Machado, Minakata, Nunokawa, Zukanovich Funchal, 1307.3248

Barger, Bhattacharya, Chatterjee, Gandhi, Marfatia, Masud, 1405.1054, 1307.2519

Barger et al, 1203.6012

P. Coloma -  $\nu$  oscillations

# Precision on $\theta_{23}$

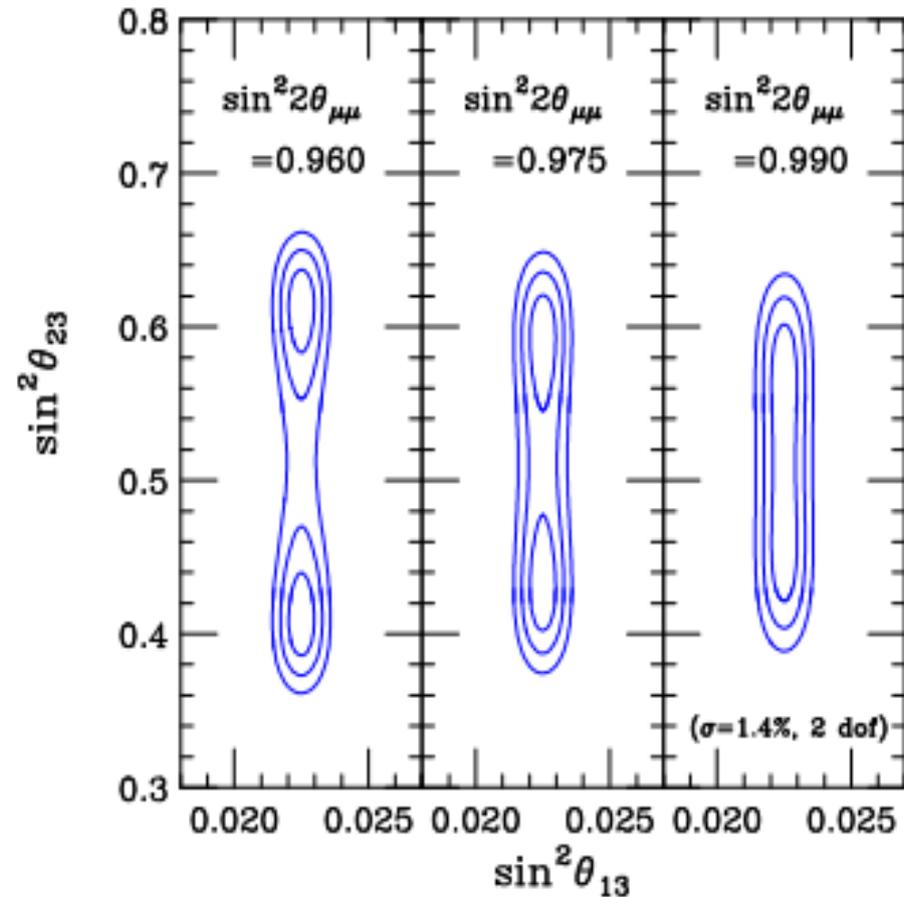
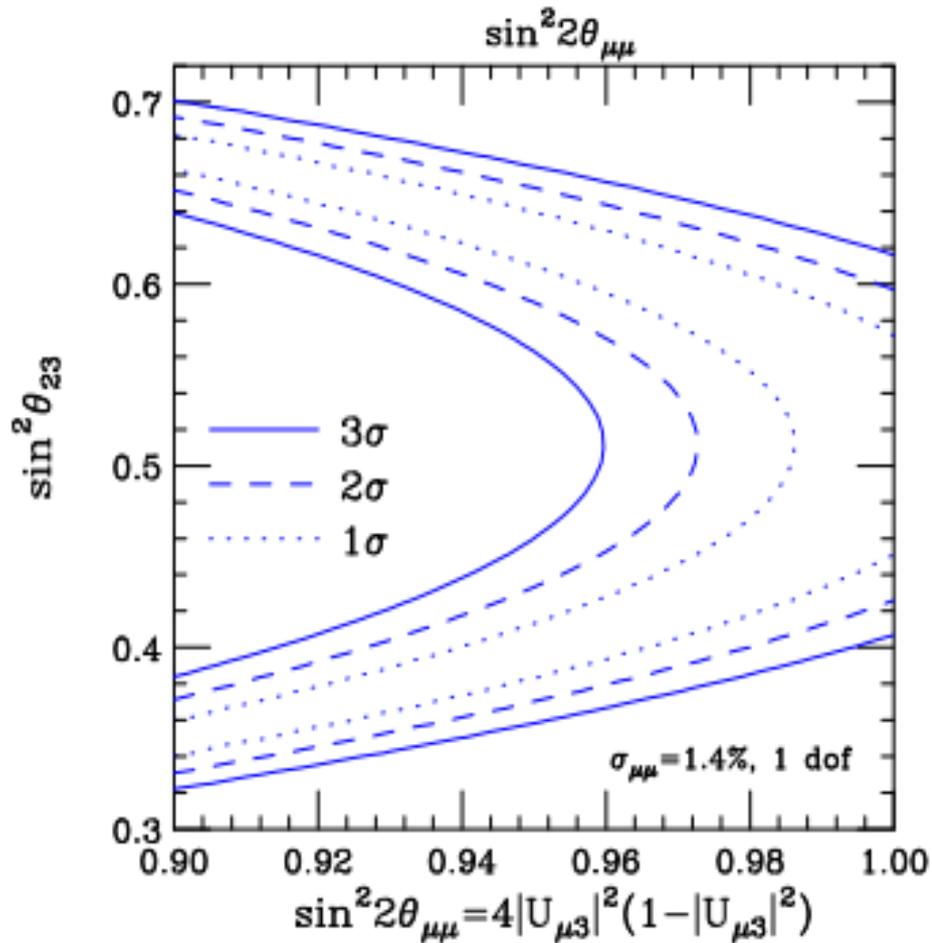
In disappearance:

$$\begin{aligned} P_{\mu\mu}^{vac} &\simeq 1 - \sin^2 2\theta_{23} \sin^2 \Delta_{31} \\ &+ 4\sin^2 \theta_{13} \sin^2 \theta_{23} \cos 2\theta_{23} \sin^2 \Delta_{31} \\ &+ \mathcal{O}(s_{13}\epsilon) + \mathcal{O}(\epsilon^2) \end{aligned}$$

$$P_{\mu\mu} = 1 - \sin^2 2\theta_{\mu\mu} \sin^2 \Delta_{\mu\mu}$$

$$\Delta_{31} \equiv \frac{\Delta m_{31}^2 L}{4E} \quad \epsilon \equiv \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \quad c_{ij} \equiv \cos \theta_{ij} \\ s_{ij} \equiv \sin \theta_{ij}$$

# Precision on $\theta_{23}$



S. Raut, 1209.5658 [hep-ph]

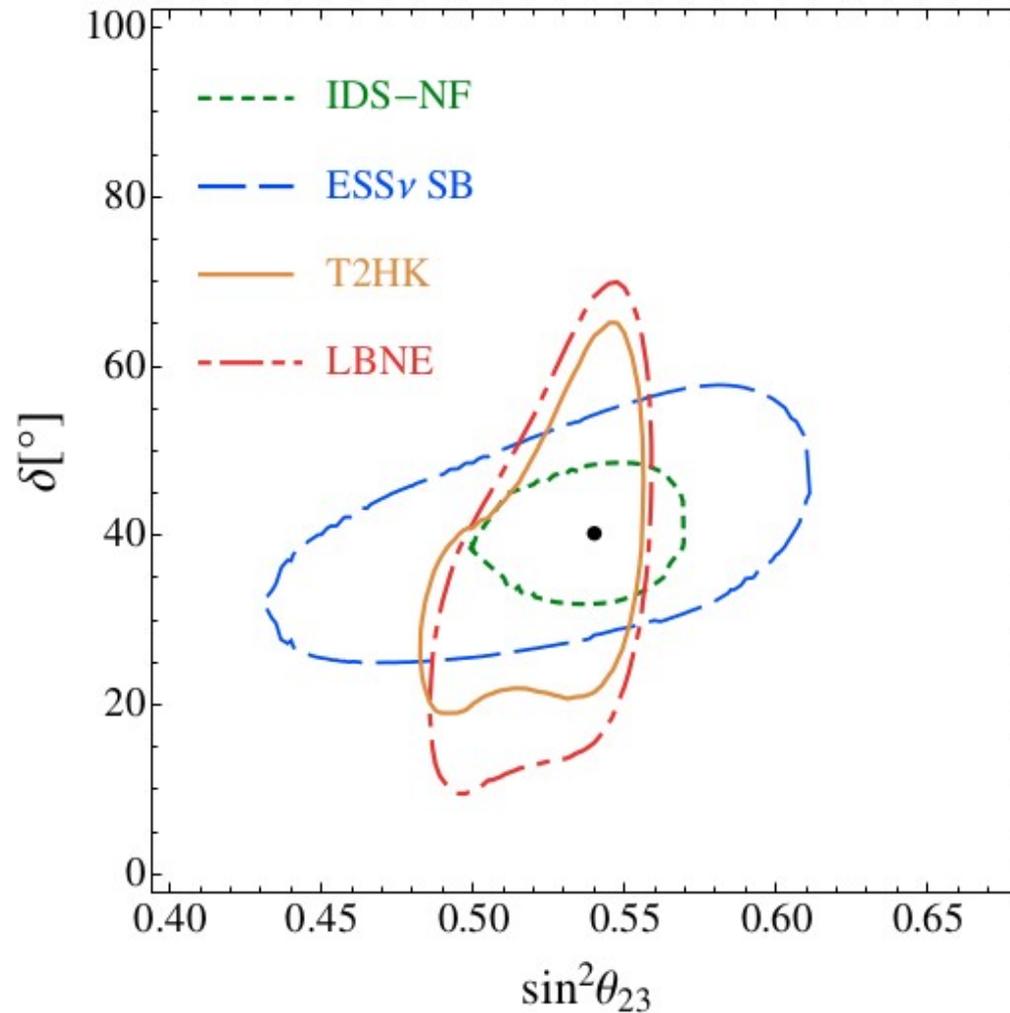
Coloma, Minakata, Parke, 1406.2551 [hep-ph]

# Precision on $\theta_{23}$

In appearance:

$$P_{\mu e} = (s_{23} \sin 2\theta_{13})^2 A_{atm}^2$$
$$+ \epsilon \sin 2\theta_{23} \sin 2\theta_{13} c_{13} A_{atm} A_{sol} \cos(\delta + \Delta_{31})$$
$$+ O(\epsilon^2)$$

# Precision on $\theta_{23}$



Coloma, Minakata, Parke, 1406.2551 [hep-ph]

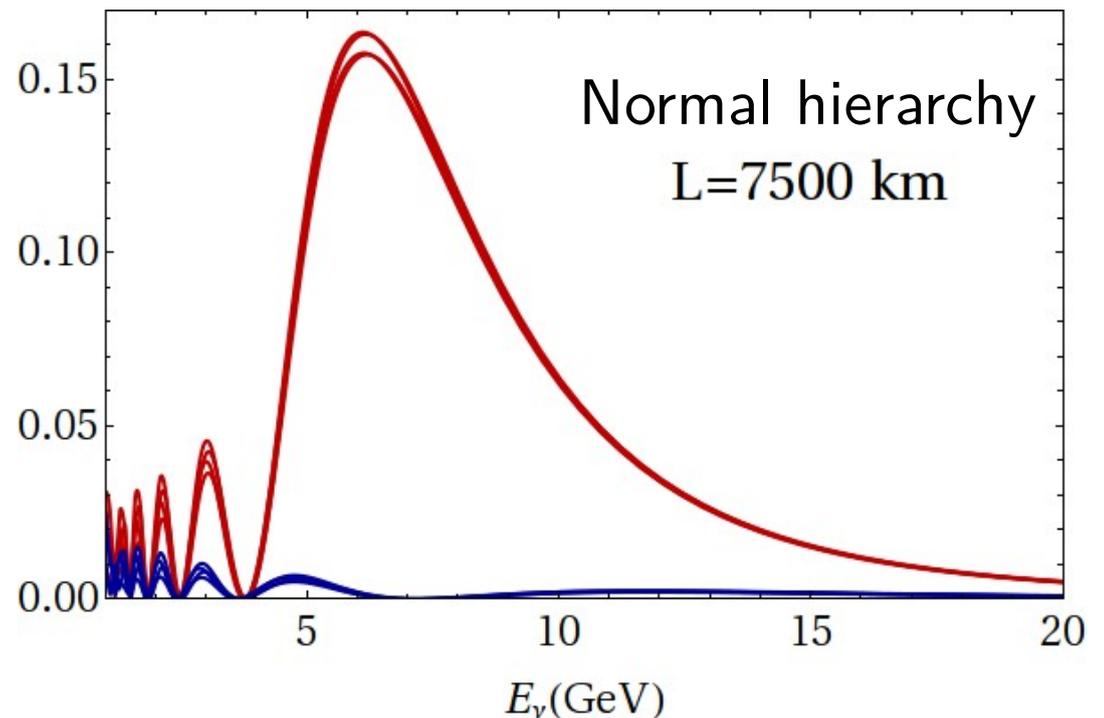
Ordering of neutrino masses

# Matter effects in appearance (beams)

In two-families:

$$P = \sin^2 2\theta_M \sin^2 \left( \frac{\Delta m_M^2 L}{4E} \right)$$

$$\sin^2 2\theta_M = \frac{\sin^2 2\theta}{\sin^2 2\theta + (\cos \theta - A)^2}; \quad A = \frac{2EV}{\Delta m^2}$$



Wolfenstein ('78), Barger et al ('80),  
Mikheev and Smirnov ('85)

# Other ways to measure the MO

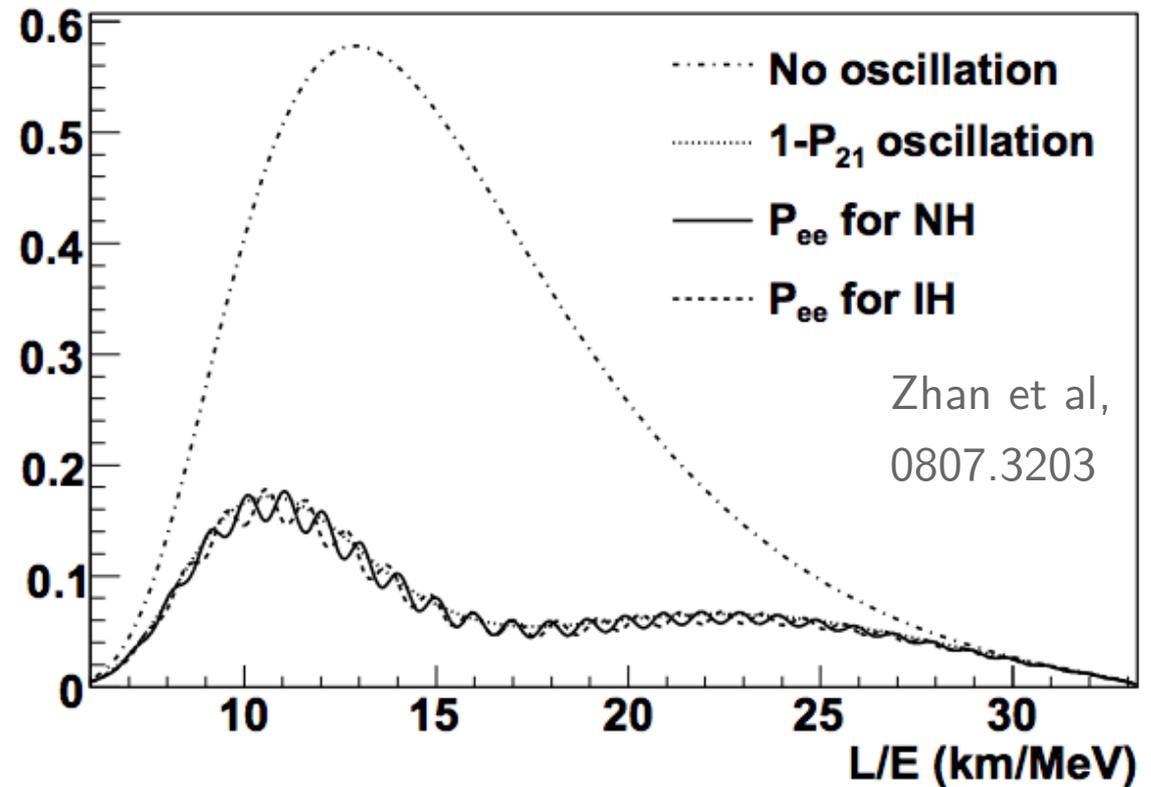
- 1) Reactor experiments at medium baselines (JUNO, RENO50)
- 2) Matter effects in atmospheric neutrino experiments (PINGU, ORCA, INO, HK)
- 3) Precise determination of mass splittings

# Reactor experiments at medium baselines

Petcov, Piai, hep-ph/01102074

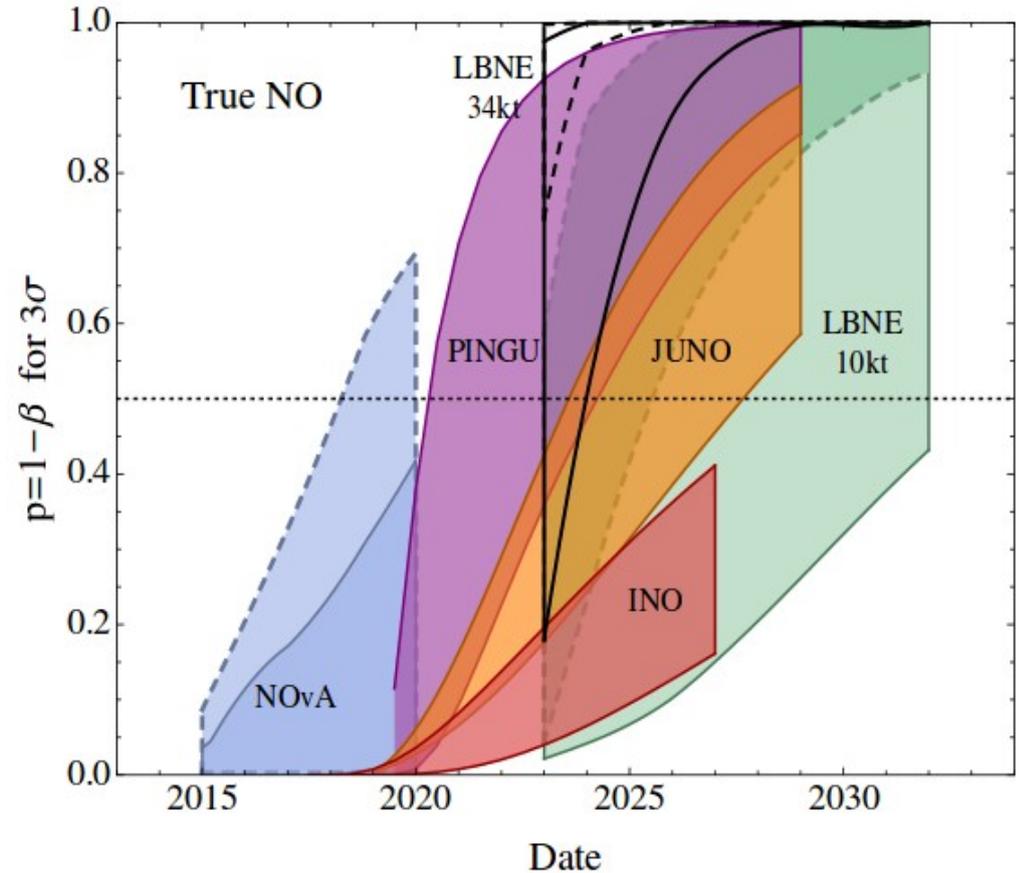
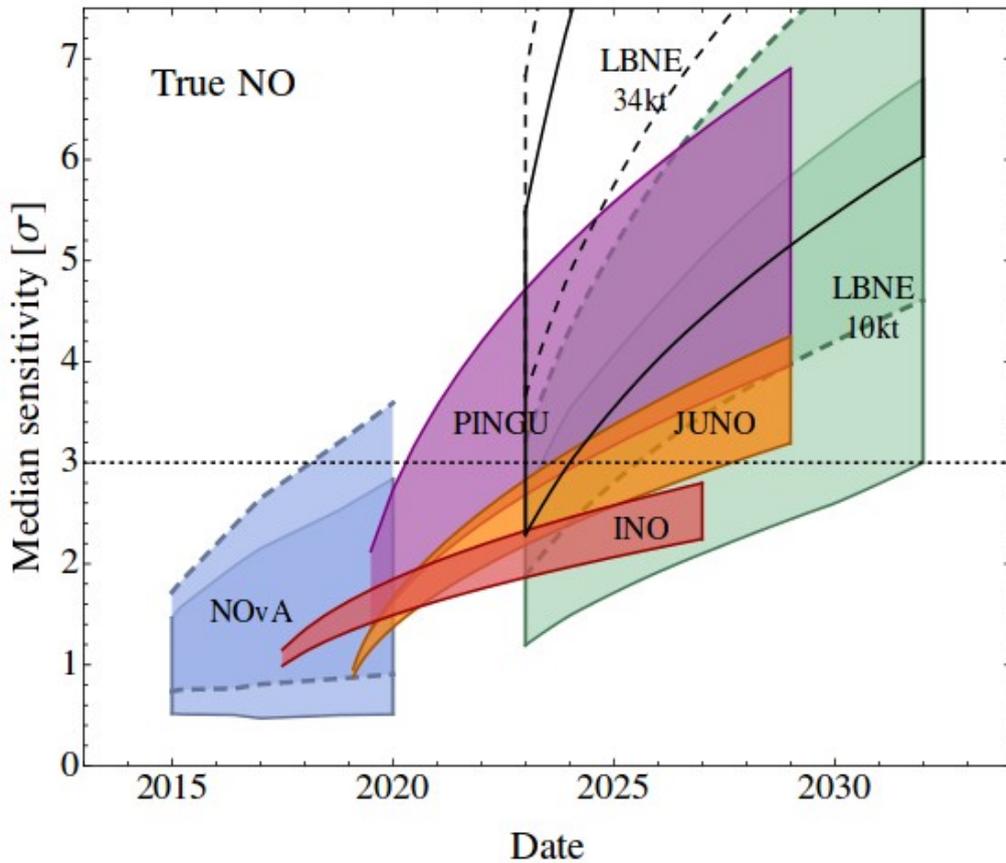
Choubey, Petcov, Piai,

hep-ph/0306017



$$\begin{aligned}
 P_{ee} &= 1 - c_{13}^4 \sin^2 2\theta_{12} \sin^2 \left( \frac{\Delta m_{21}^2 L}{4E} \right) \\
 &- \sin^2 2\theta_{13} \left[ c_{12}^2 \sin^2 \left( \frac{\Delta m_{31}^2 L}{4E} \right) + s_{12}^2 \sin^2 \left( \frac{\Delta m_{32}^2 L}{4E} \right) \right]
 \end{aligned}$$

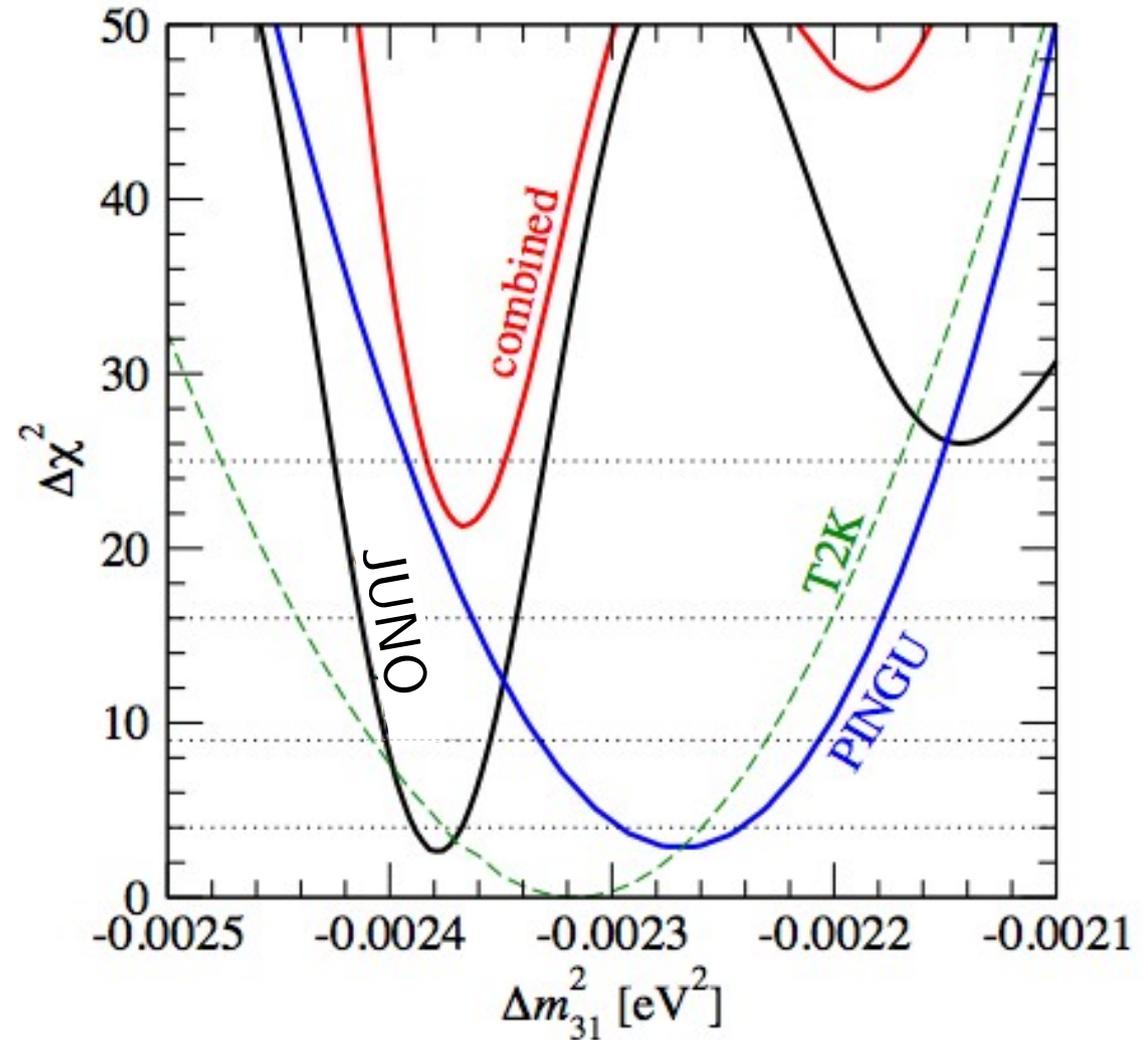
# Prospects for mass ordering



Blennow, Coloma, Huber and Schwetz, 1311.1822 [hep-ph]

# Precise measurement of mass splittings

The ordering of neutrino masses may as well come from a global fit to different data



Blennow, Schwetz, 1306.3988 [hep-ph]

(see also Li *et al*, 1303.6733 [hep-ph], for instance)

# Systematics and nuclear effects

# Near detectors and systematics

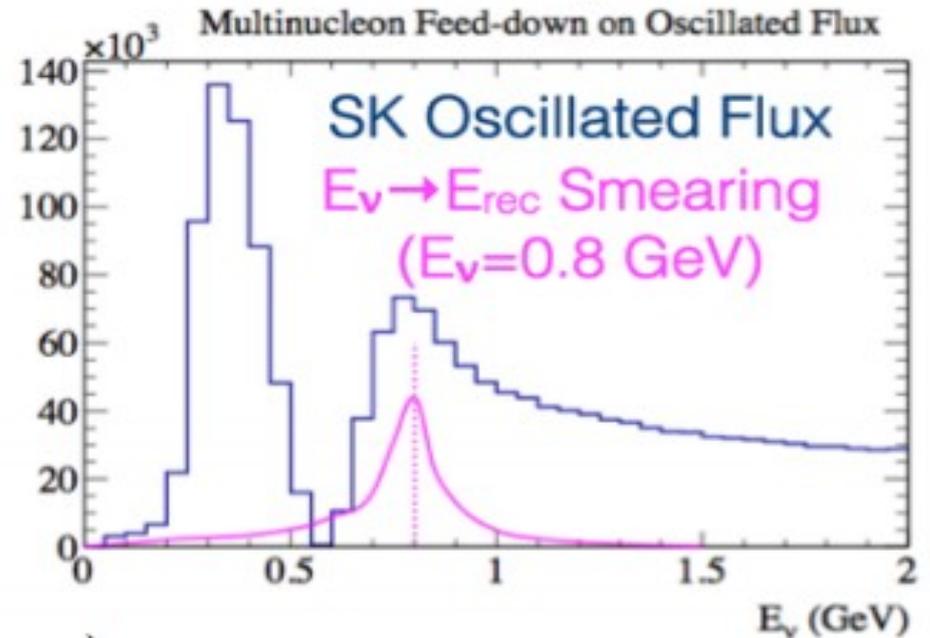
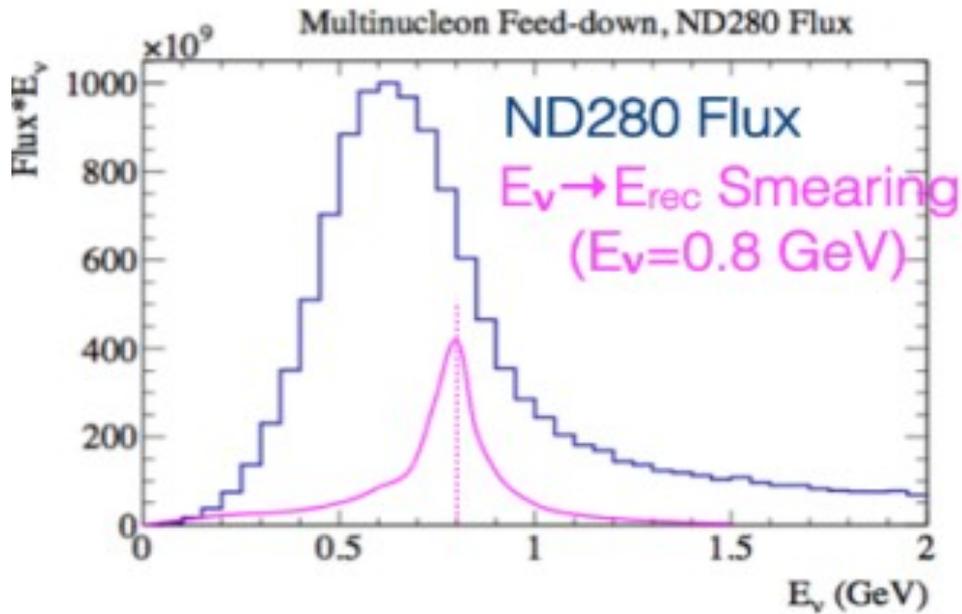
$$n_{\alpha \rightarrow \beta}(L, E) \sim \frac{1}{L^2} \epsilon_{\beta}(E) \times \sigma_{\beta}(E) \times \phi_{\alpha}(E) \times P_{\alpha\beta}(L, E)$$

At reactor experiments, the cancellation of systematics between near/far detectors is very effective:

$$\frac{n_{ee}^{FD}}{n_{ee}^{ND}} \sim \frac{L_{ND}^2}{L_{FD}^2} \frac{\cancel{\epsilon_e \sigma_e \phi_e}}{\cancel{\epsilon_e \sigma_e \phi_e}} P_{ee}$$

# Nuclear effects

The **big** problem with nuclear effects in neutrino oscillation experiments is the determination of the neutrino energy



(Figures by K. Mahn, nuSTEC school 2014)

# Conclusions

- The neutrino picture is still far from being complete
- Next milestone seems to be the ordering of neutrino masses
- Current generation of experiments is already producing exciting new results
- A next generation of long-baseline experiments is well-motivated:
  - Provide a clear signal for CP violation
  - Provide a clear determination of the mass ordering
  - Enter the era of precision in neutrino oscillations  
(searches for New Physics, model discrimination, etc)

Thank you!