

Quarks and Leptons as Nambu-Goldstone Fermions

(Based on arXiv:1004.4164 w/ M. Nojiri, M. Sudano and T. T. Yanagida)

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Fermilab Theory Seminar
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1 Introduction

- Motivations for Supersymmetry
- Coset Spaces
- An Incomplete Toy Model

2 Phenomenology of Nambu-Goldstone Fermion Scenario

- Low-energy Spectrum
- LHC Physics

3 Looking Ahead to Realistic GUT Models

- E_7/H
- Outlook

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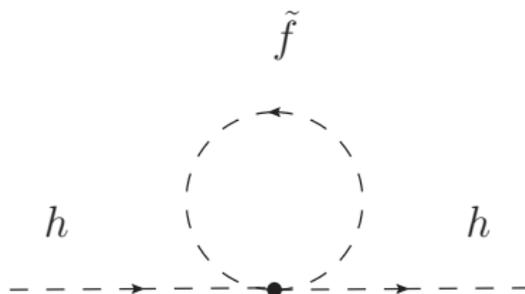
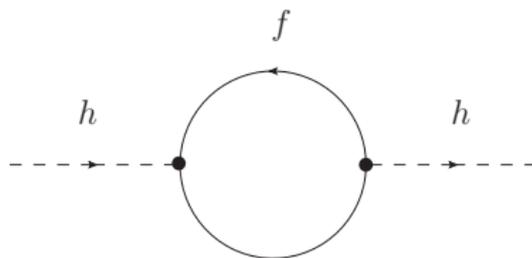
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Controlling the Higgs



Enhanced gauge unification

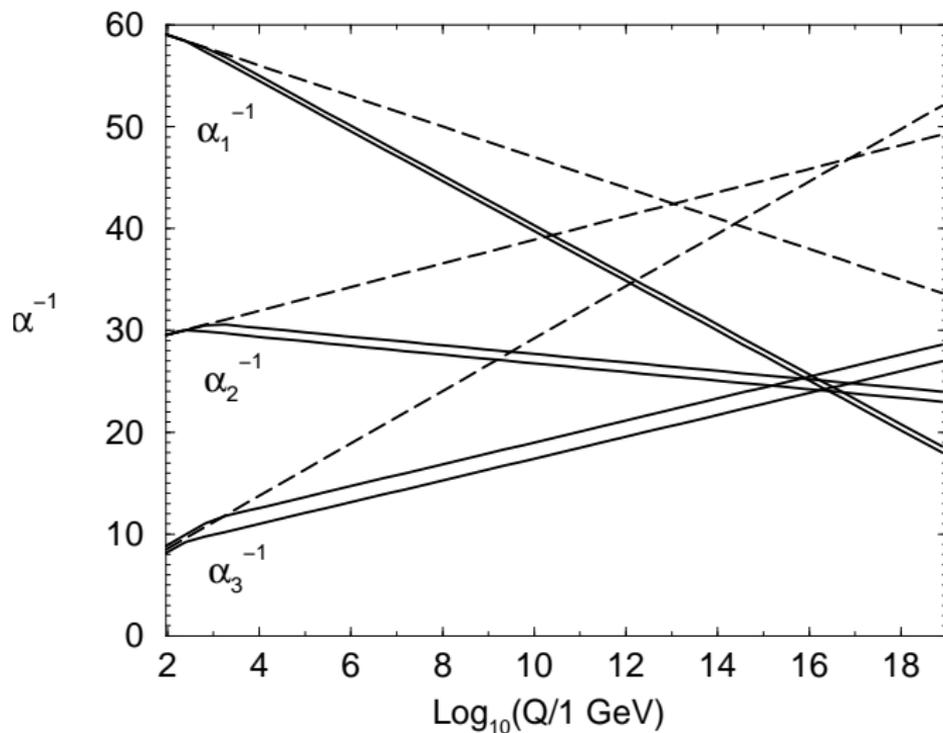
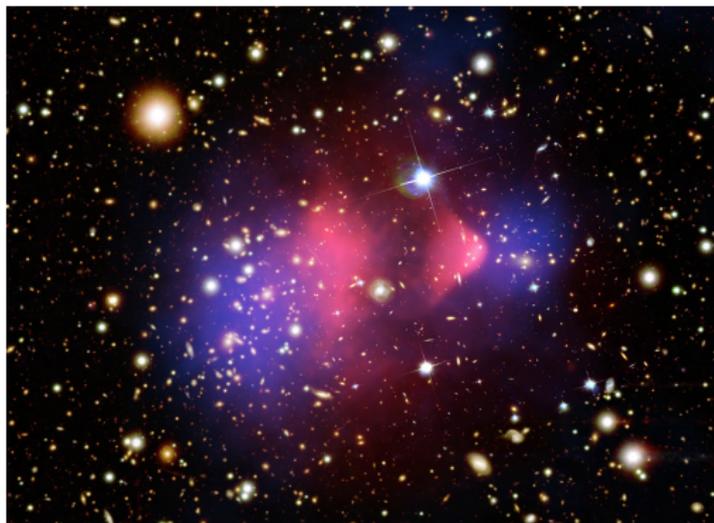
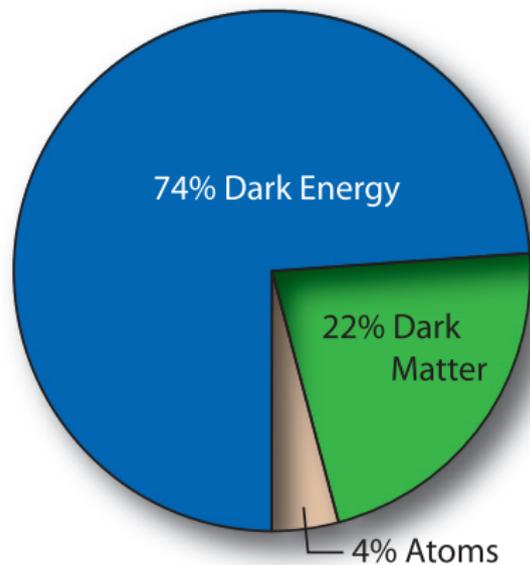
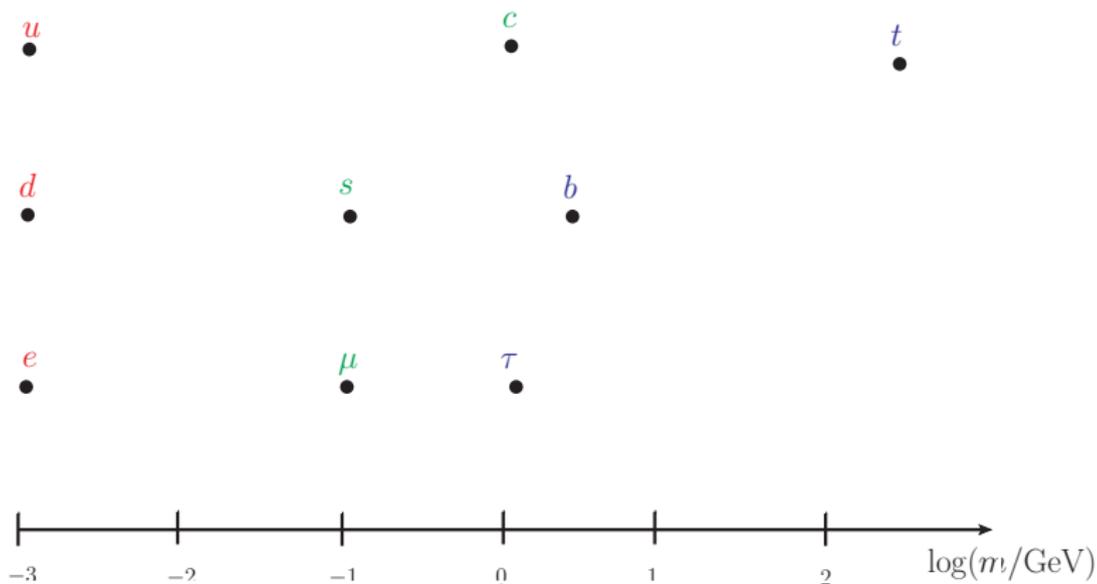


Figure: From S. P. Martin, arXiv:9709356

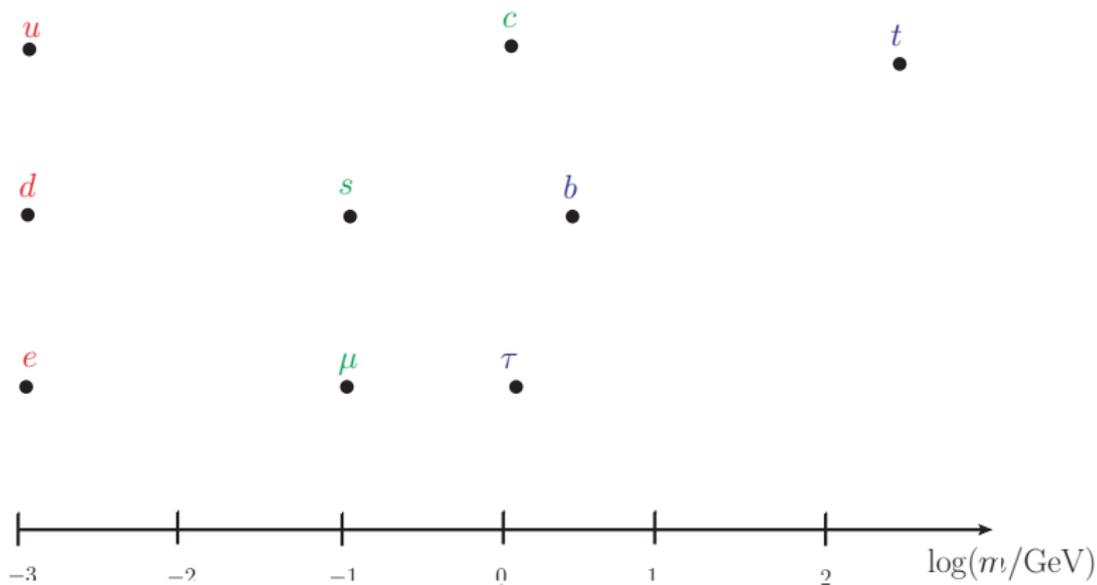
Neutral LSP as dark matter



Hierarchy of Yukawa couplings?



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Ad-hoc \Rightarrow dynamical origin of mass?

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Nambu-Goldstone fermions

- 1st and 2nd generation Standard Model fermions = SUSY partners of Nambu-Goldstone (NG) bosons
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But is it a viable strategy?

Formulation of SUSY nonlinear σ model

Under global symmetry breaking $G \rightarrow H$,

$$\mathcal{L}_{NGB}^{NL} = -(\partial^\mu \pi_i) g^{ij} (\pi/f_\pi) (\partial_\mu \pi_j)$$

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“Quasi”-NGBs n_{QNGB} minimal if G/H is Kähler!

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Then for scalars:

$$\mathcal{L}_{SUSY}^{NL} = -\partial^\mu \phi^{*i} \left[\frac{\partial^2 K(\phi^*, \phi)}{\partial \phi^{*i} \partial \phi^j} \right] \partial_\mu \phi^j$$

such that

$$\frac{\partial g_{ij}}{\partial \phi^{*k}} = \frac{\partial g_{kj}}{\partial \phi^{*i}}, \quad \frac{\partial g_{ij}}{\partial \phi^k} = \frac{\partial g_{ik}}{\partial \phi^j}$$

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Compact v. non-compact

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- \Rightarrow 1st and 2nd generation sleptons/squarks too heavy
- Bagger and Witten, Phys. Lett. B **118**, 103 (1982)

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An example manifold

- SUSY $U(6)/[U(4) \times SU(2)]$ nonlinear sigma model
- $(4 \times 2 + 1)$ NG chiral multiplets, ϕ_i^a and φ , where $a = 1, \dots, 4$ and $i = 1, 2$

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- φ is the novino.
- All d.o.f. in ϕ_i^a and one real boson in φ are NG bosons; the remaining is the QNGB.

An example manifold (cont'd)

- Arrange fields into matrix

$$\Psi = \begin{pmatrix} e^{i\kappa\varphi/v} \mathbf{1}_2 \\ \phi_i^a/v \end{pmatrix},$$

which has 12 components Ψ_i^α , $\alpha = 1, \dots, 6$.

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- v is scale of $U(6)$ breaking, $F(x)$ freedom from QNGB.
- $U(6)$ **nonlinearly realized** by ϕ_i^a, φ

- Couple to supergravity:

$$\mathcal{L} = 3 \int d^2\theta d^2\bar{\theta} \mathcal{E} \exp\left(\frac{1}{3} K(\phi_i^a, \varphi, \phi_a^{\dagger i}, \varphi^\dagger)\right)$$

Supergravity and SUSY breaking

- Couple to supergravity:

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- Introduce hidden SUSY breaking sector:

$$K = K(\phi_i^a, \varphi, \phi_a^{\dagger i}, \varphi^\dagger) + Z^\dagger Z + \dots$$

- NG bosons remain massless, but QNGB in φ gets mass $\mathcal{O}(m_{3/2})$.

Right-handed leptons and 2nd generation

- Include right-handed fermions by

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- Include 2nd generation with $(U(10)/[U(8) \times SU(2)])^2$ containing multiplets

$$(\phi_i^a)_L = \begin{pmatrix} u_L^\xi & \nu_{eL} & c_L^\xi & \nu_{\mu L} \\ d_L^\xi & e_L^- & s_L^\xi & \mu_L^- \end{pmatrix} \sim (\mathbf{8}, \mathbf{2})$$
$$(\phi_i^a)_R = \begin{pmatrix} u_R^\xi & \nu_{eR} & c_R^\xi & \nu_{\mu R} \\ d_R^\xi & e_R^- & s_R^\xi & \mu_R^- \end{pmatrix} \sim (\mathbf{8}, \mathbf{2}) .$$

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- Similar problem for novino?

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LHC phenomenology does not depend on details of model!

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Parameter scan with DarkSUSY

- Scan mSUGRA models over $M_{H_u} \sim M_{H_d} \sim \mathcal{O}(m_{3/2})$ in the subspace

$$m_{1/2} = 300 \text{ GeV}, \quad \tan \beta = 10, \quad \mu > 0, \quad A_0 = 0$$

- And $m_0 = 0$ for 1st and 2nd generation scalars, and $m_0 = 1 \text{ TeV}$ for 3rd generation scalars

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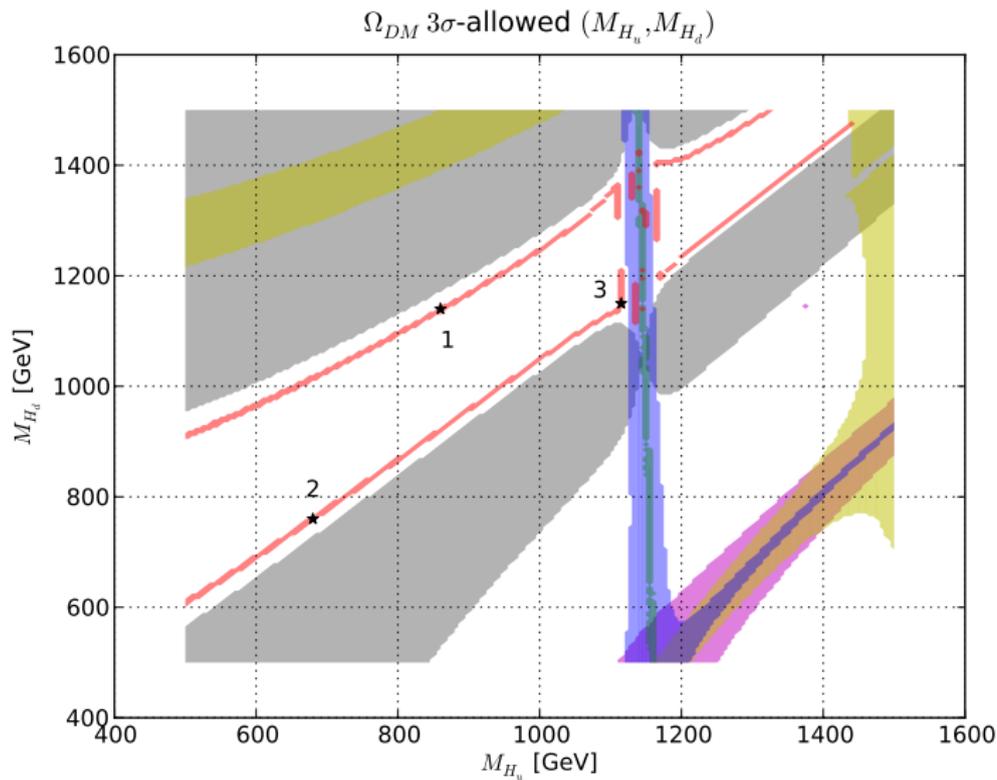
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- At small m_0 , $m_{1/2} \simeq 300 \text{ GeV}$ favored by muon $g - 2$
- $\tilde{\tau}$ no longer favored co-annihilation partner or LSP
- Choose conventional mSUGRA point (“CP”) for comparison:

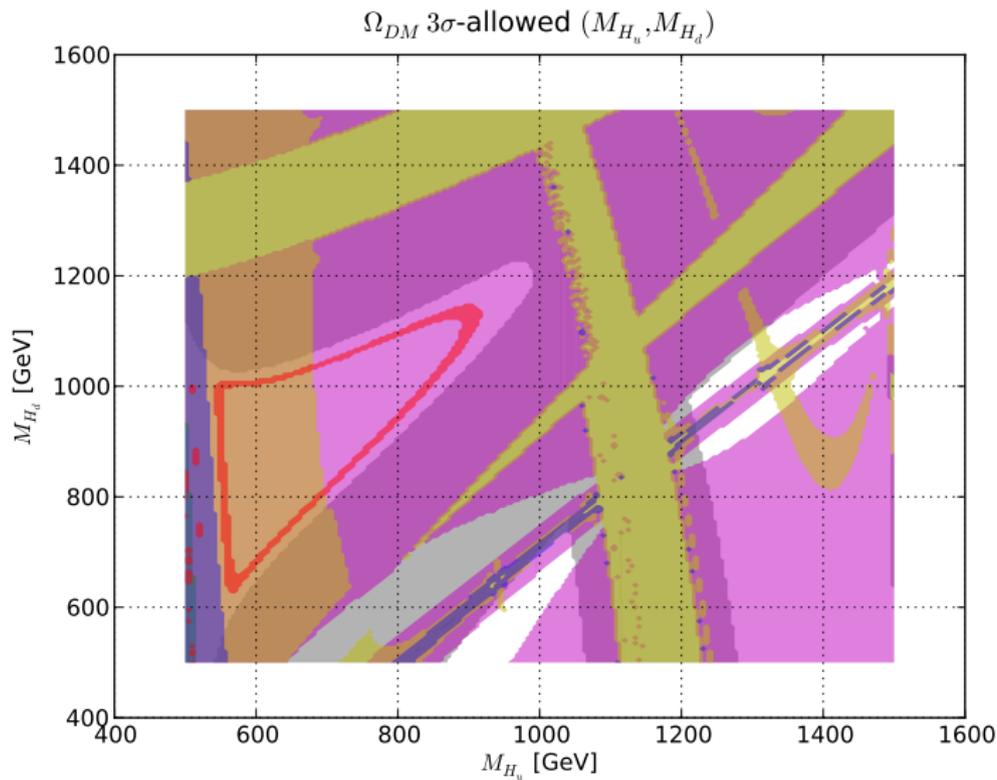
$$m_0 = 75 \text{ GeV}, \quad m_{1/2} = 300 \text{ GeV}$$

$$\tan \beta = 10, \quad \mu > 0, \quad A_0 = -200 \text{ GeV}$$

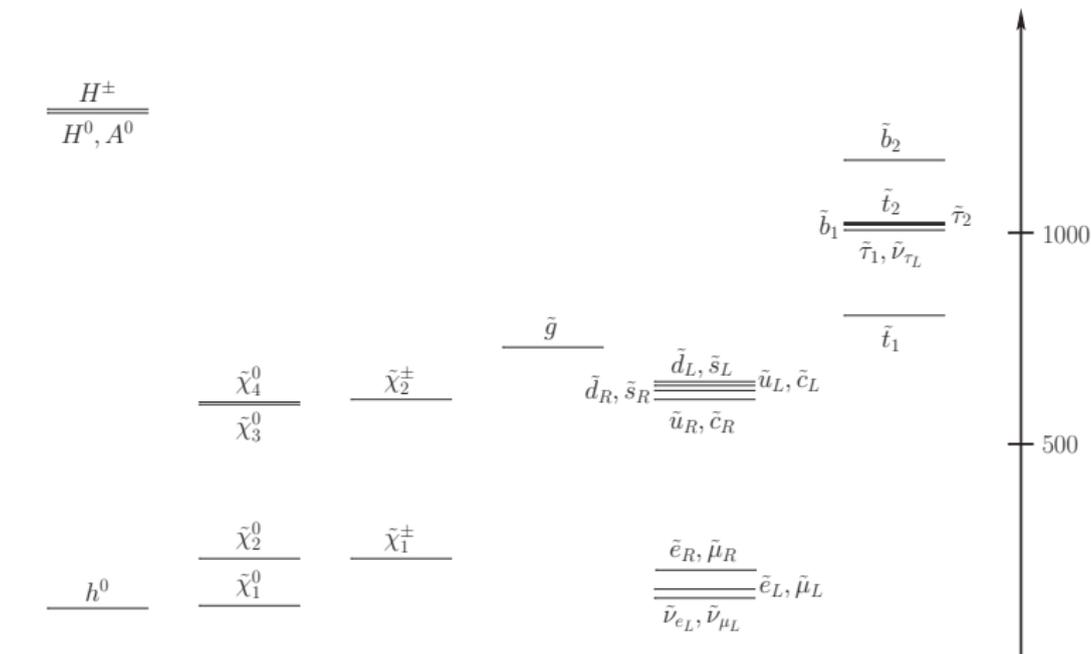
Scan results with benchmark points



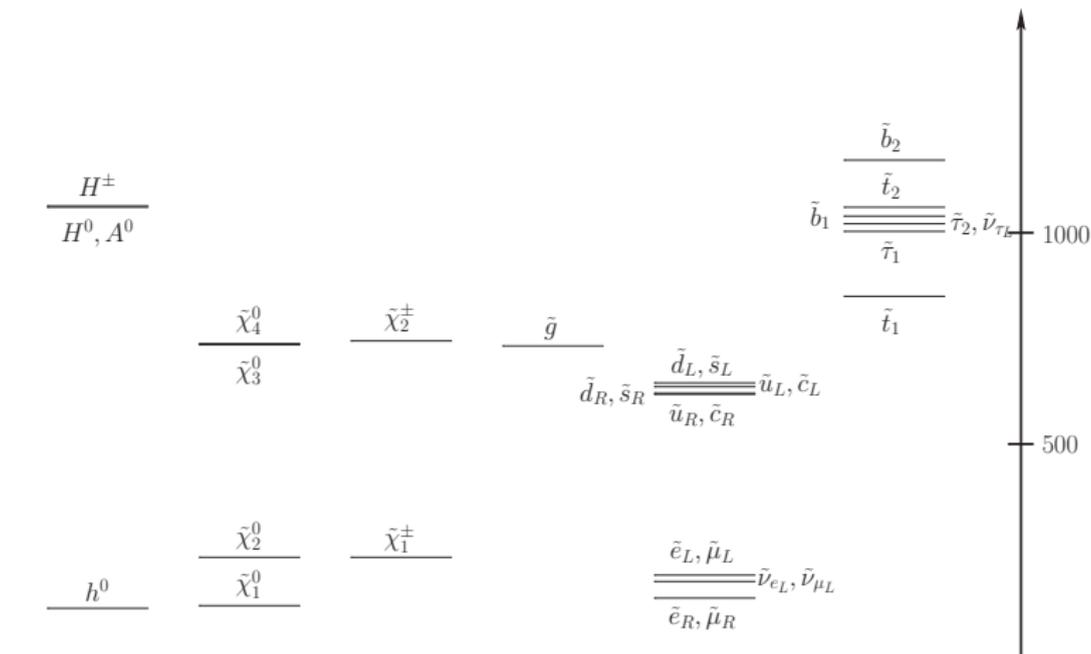
Scan results with $m_0 = 0$ for 3rd generation



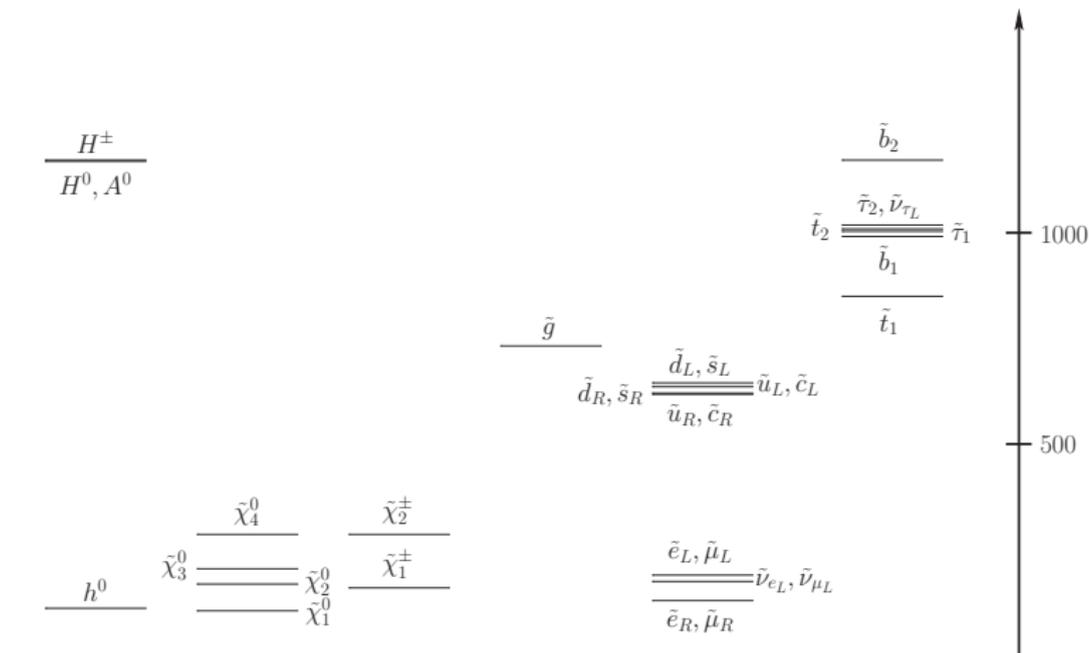
Benchmark Point 1



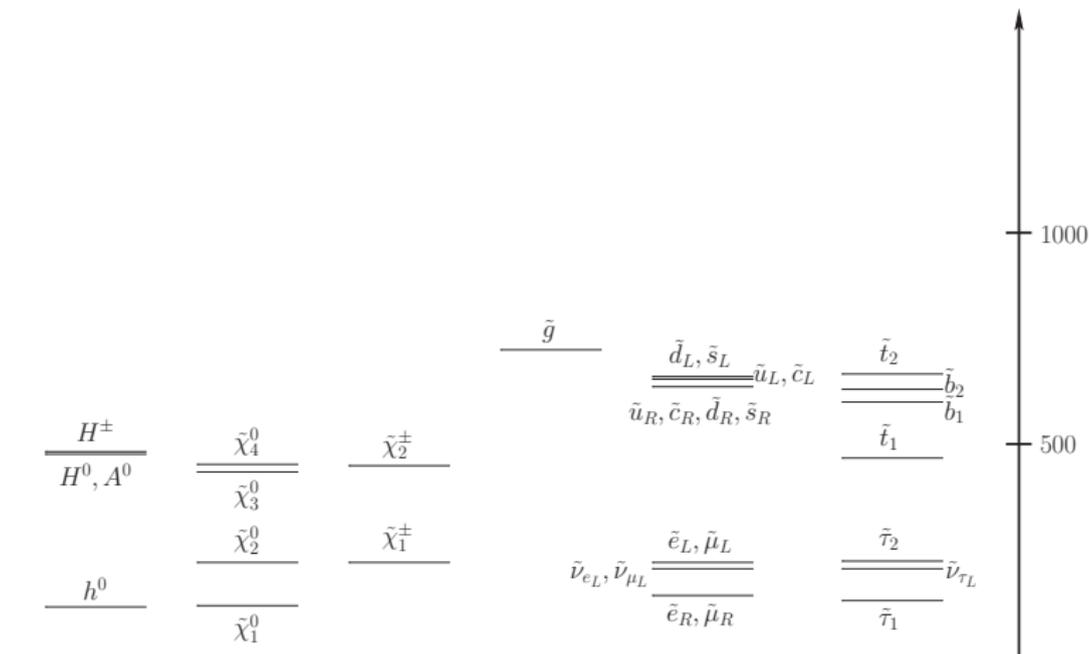
Benchmark Point 2



Benchmark Point 3



Conventional Point



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Parameters

- 10^5 signal events at 14 TeV for inclusive squark production
- Production cross section is $\gtrsim 15 \text{ pb} \Rightarrow 7 \text{ fb}^{-1}$
- Standard SFOS subtraction of chargino events from DFOS
- τ - and b -jet tagging efficiency at 80%

Discriminator: multiplicities

Multiplicities:

- number of b -jets n_b with $p_T > 50$ GeV
- number of τ -jets n_τ with $p_T > 20$ GeV
- number of leptons n_l with $p_T > 15$ GeV and $\eta < 2$.

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Model point	% $n_b \geq 1$	% $n_\tau \geq 1$	% $n_l \geq 2$
BP 1	2.29	0.04	15.80
BP 2	2.22	0.02	15.84
BP 3	3.17	2.284	28.97
CP	31.70	16.94	4.10

Discriminators: mass differences and charge asymmetry

- Mass determination and charge asymmetry from endpoint analysis of

$$(\tilde{g} \rightarrow) \tilde{q}j \rightarrow \tilde{\chi}_2^0 jj \rightarrow \tilde{l}^\pm jjl^\mp \rightarrow jjl^\pm l^\mp + \cancel{E}_T$$

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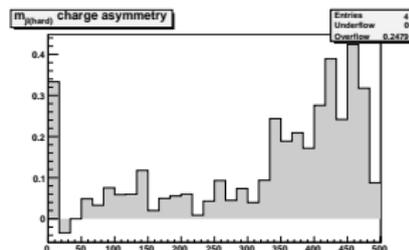
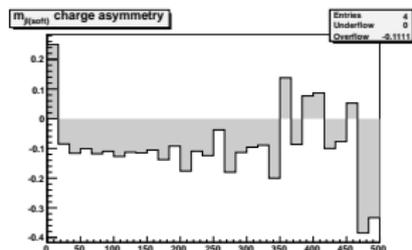
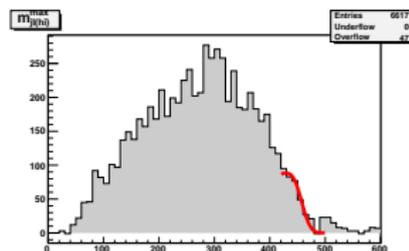
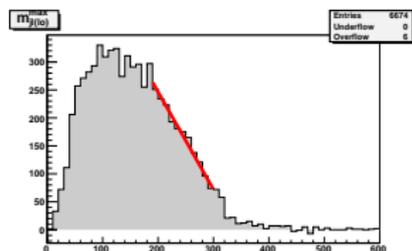
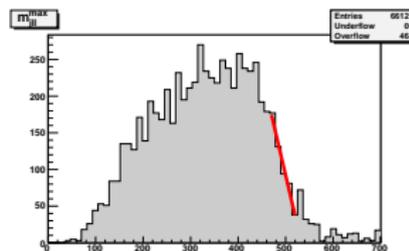
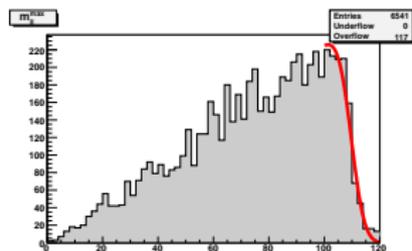
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Benchmark points can be distinguished from normal mSUGRA points!

Sample endpoint fitting (BP 1)



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GUT representations

- $SU(5) \supset (5 + 5^*)_H \oplus 10 \oplus 5^*$
- $SO(10) \supset 10_H \oplus 16 \rightarrow (5 + 5^*)_H \oplus 10 \oplus 5^*$

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- E_7 gives right flavor cosets:
 - $E_7/SU(5) \rightarrow (10 \oplus 5^*) \times 3 + 5_H$
 - $E_7/[SO(10) \times U(1)^2] \rightarrow (10 \oplus 5^*) \times 2 + (5 + 5^*)_H$

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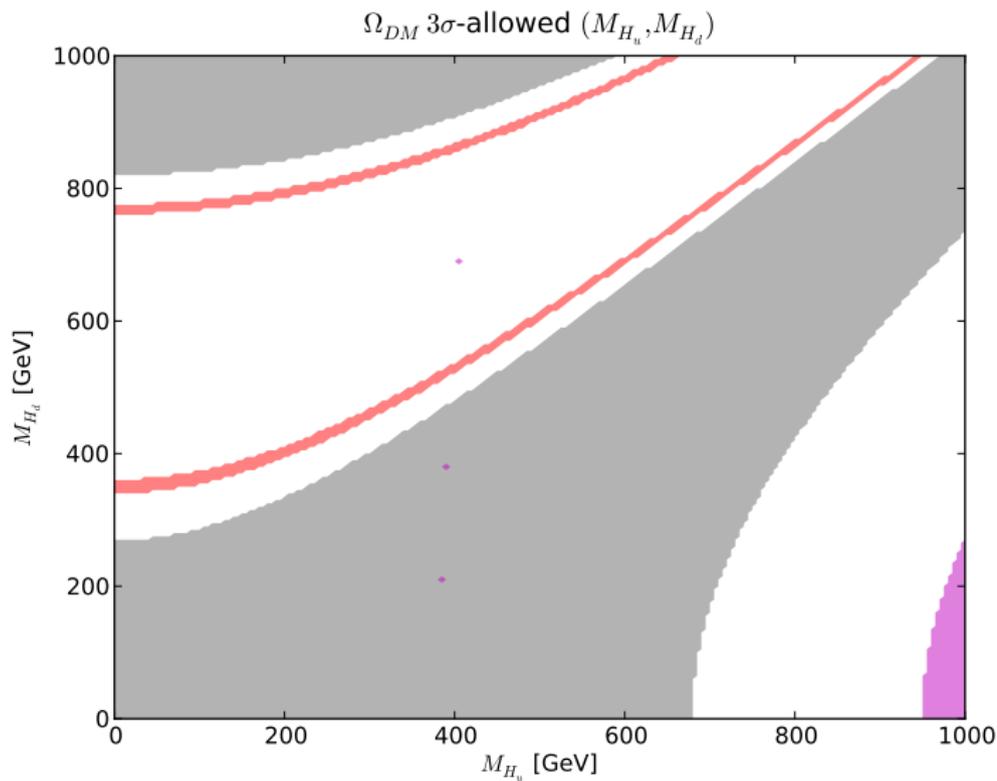
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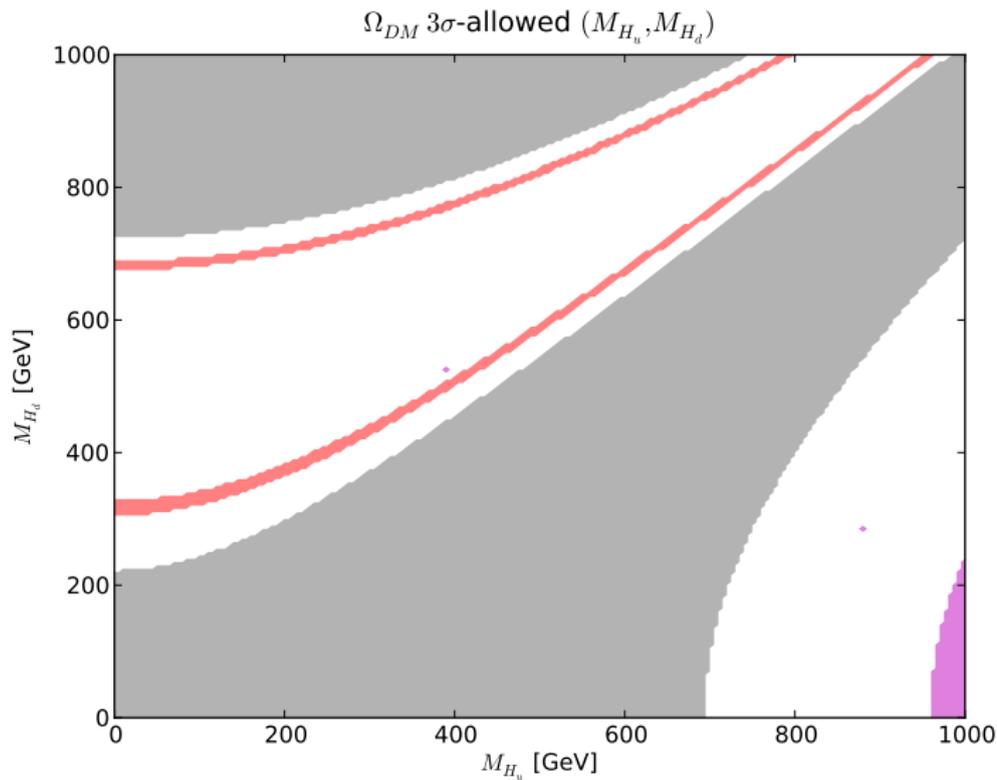
GUT representations

- $SU(5) \supset (5 + 5^*)_H \oplus 10 \oplus 5^*$
- $SO(10) \supset 10_H \oplus 16 \rightarrow (5 + 5^*)_H \oplus 10 \oplus 5^*$
- E_7 gives right flavor cosets:
 - $E_7/SU(5) \rightarrow (10 \oplus 5^*) \times 3 + 5_H$
 - $E_7/[SO(10) \times U(1)^2] \rightarrow (10 \oplus 5^*) \times 2 + (5 + 5^*)_H$
- E_6 too small, E_8 gives real representation

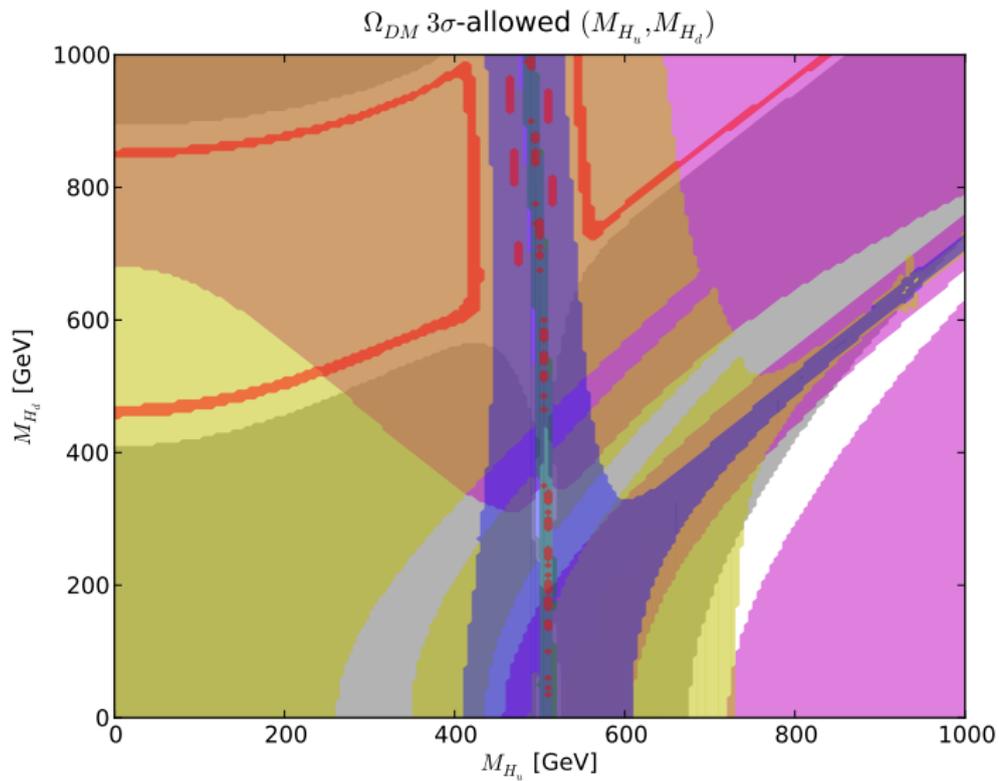
Heavy 5^* , Heavy 10

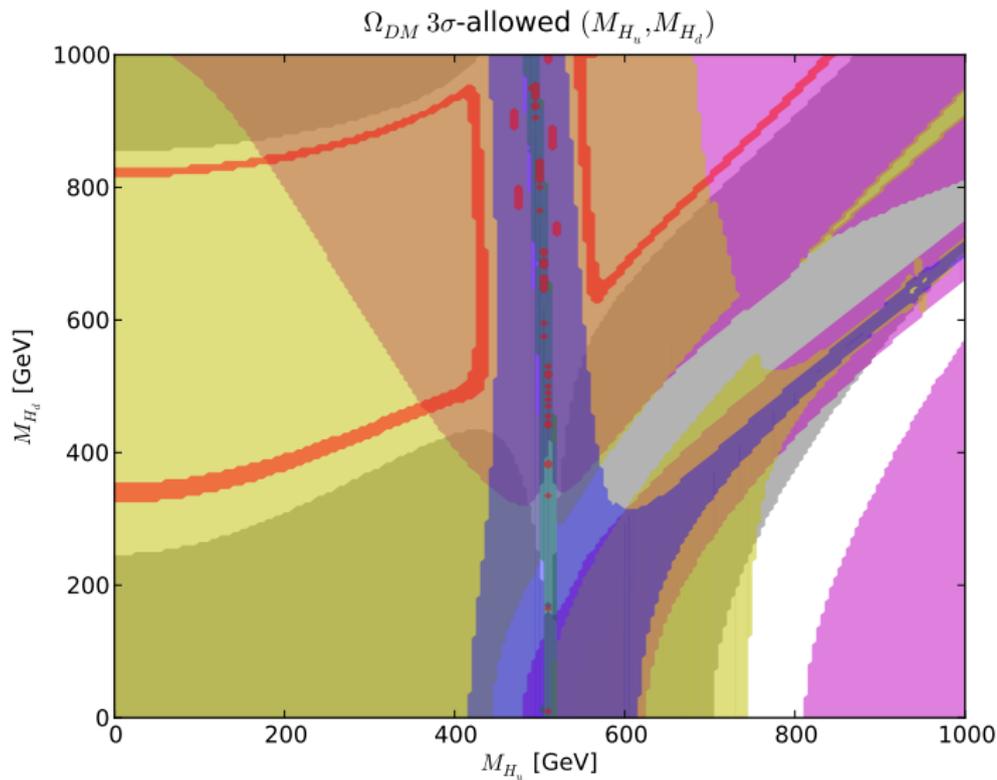


Light 5^* , Heavy 10



Heavy 5^* , Light 10





1 Introduction

- Motivations for Supersymmetry
- Coset Spaces
- An Incomplete Toy Model

2 Phenomenology of Nambu-Goldstone Fermion Scenario

- Low-energy Spectrum
- LHC Physics

3 Looking Ahead to Realistic GUT Models

- E_7/H
- Outlook

Dark matter

- BP 1 and BP 2 annihilations helicity-suppressed
- Mostly bino — suppressed gauge final states and direct detection cross-section
- Total cross-section $\mathcal{O}(10^{-30}) \text{ cm}^3 \text{ s}^{-1}$

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FCNCs

- First “transition parameter” δ_{12} suppressed by λ^5 — near upper bound
- $s \rightarrow b$ suppressed only by λ_d^2 — contributes to $B_s - \bar{B}_s$ mixing?
- See Gabrielli, Masiero, Silvestrini, Phys. Lett. B **374**, 80 (1996)

Positive aspects

- Quarks and leptons as NG fermions a viable explanation of Yukawa hierarchy
- Scenario easily distinguished at LHC
- Good dark matter candidate

Conclusions

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- Gravitino and gravitino astrophysics
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Looks interesting!