

# Test for Lorentz and CPT violation with MiniBooNE excesses

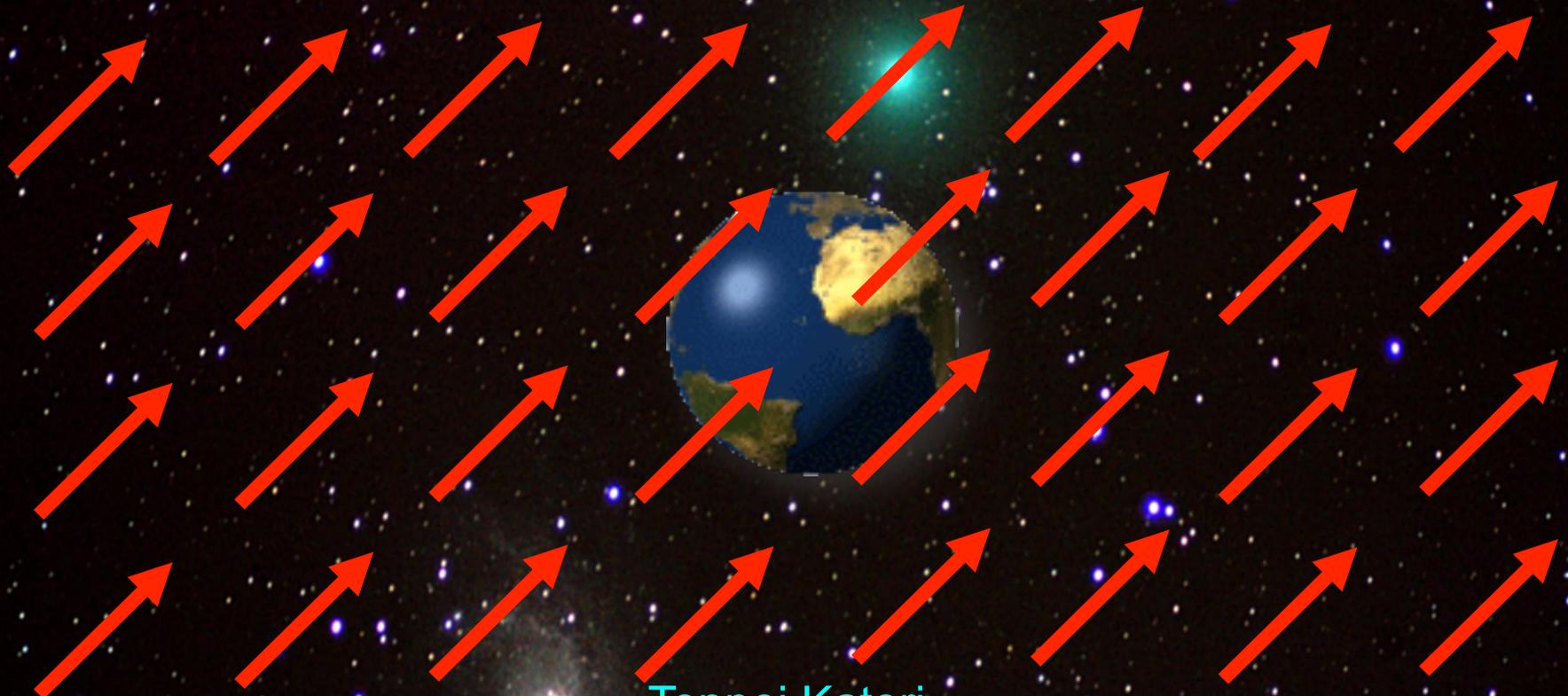
ArXiv:1109.3480



Teppei Katori  
Massachusetts Institute of Technology  
Wine and Cheese seminar, Fermilab, Batavia, Nov. 11, 2011

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## outline

1. Spontaneous Lorentz symmetry breaking
2. What is Lorentz and CPT violation?
3. Modern test of Lorentz and CPT violation
4. Lorentz violation with neutrino oscillation
5. MiniBooNE experiment
6. Lorentz violation with MiniBooNE neutrino data
7. Lorentz violation with MiniBooNE anti-neutrino data
8. Conclusion

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- 1. Spontaneous Lorentz symmetry breaking**
2. What is Lorentz and CPT violation?
3. Modern tests of Lorentz and CPT violation
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# 1. Spontaneous Lorentz symmetry breaking

Every fundamental symmetry needs to be tested, including Lorentz symmetry.

After the discovery of theoretical processes that create Lorentz violation, testing Lorentz invariance becomes very exciting

Lorentz and CPT violation has been shown to occur in Planck scale physics, including:

- string theory
- noncommutative field theory
- quantum loop gravity
- extra dimensions
- etc

However, it is very difficult to build a self-consistent theory with Lorentz violation...

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However, it is very difficult to build a self-consistent theory with Lorentz violation...

Spontaneous  
Symmetry Breaking  
(SSB)!



Y. Nambu  
(Nobel prize winner 2008),  
picture taken from CPT04 at  
Bloomington, IN

# 1. Spontaneous Lorentz symmetry breaking

e.g.) SSB of scalar field

$$L = \frac{1}{2} (\partial_\mu \varphi)^2 - V(\varphi)$$

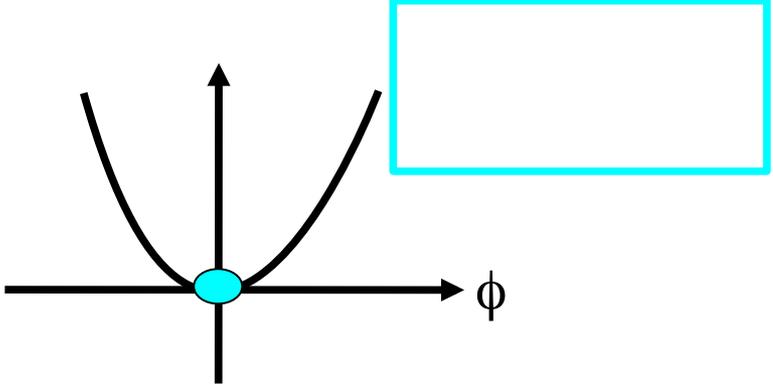
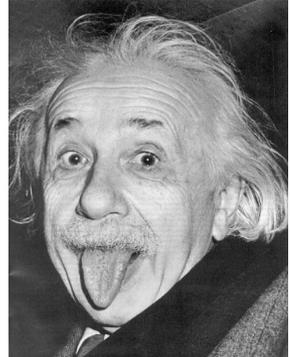
$$V(\varphi) = \frac{1}{2} \mu^2 (\varphi^* \varphi) + \frac{1}{4} \lambda (\varphi^* \varphi)^2$$

If fields have negative mass term

$$M^2(\varphi) = \mu^2 < 0$$

e.g.) vacuum Lagrangian for fermions

$$L = i\bar{\Psi}\gamma_\mu \partial^\mu \Psi$$



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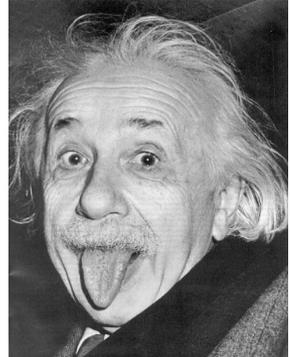
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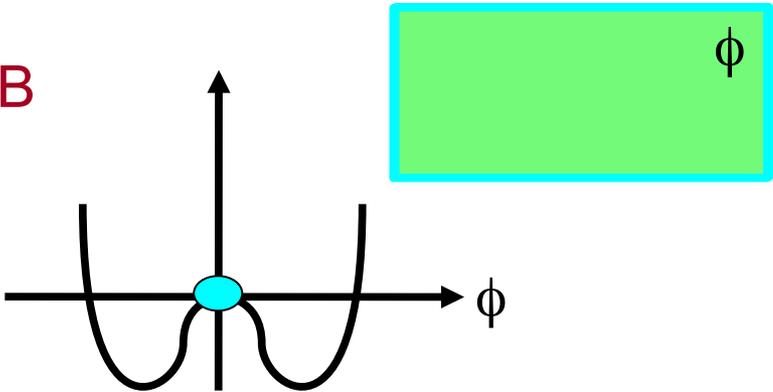
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$$L = i\bar{\Psi}\gamma_\mu \partial^\mu \Psi - m\bar{\Psi}\Psi$$



Particle acquires mass term!

SSB



# 1. Spontaneous Lorentz symmetry breaking

ex) Spontaneous Lorentz symmetry breaking in string field theory

there is a possibility that Lorentz vector field makes non zero vacuum expectation values,

ex) scalar-vector-vector coupling

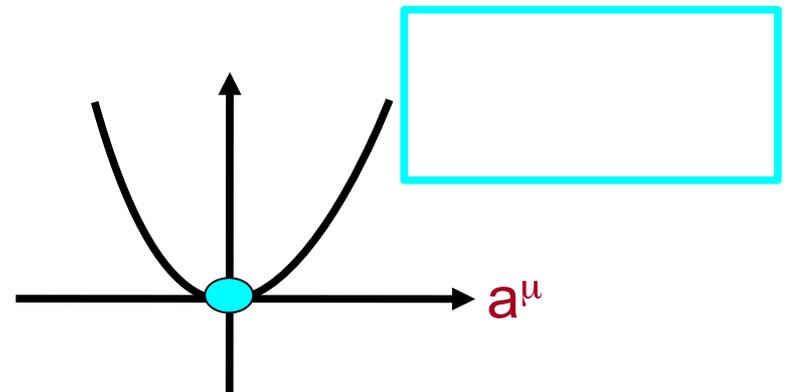
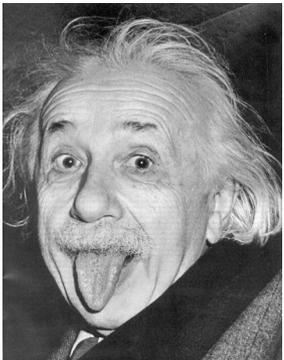
$$\phi a^\mu a_\mu \rightarrow \langle \phi \rangle a^\mu a_\mu$$

If the scalar field creates negative v.e.v, then the vector field has negative square mass term

$$\langle \phi \rangle = M^2 (a^\mu) = \mu^2 < 0$$

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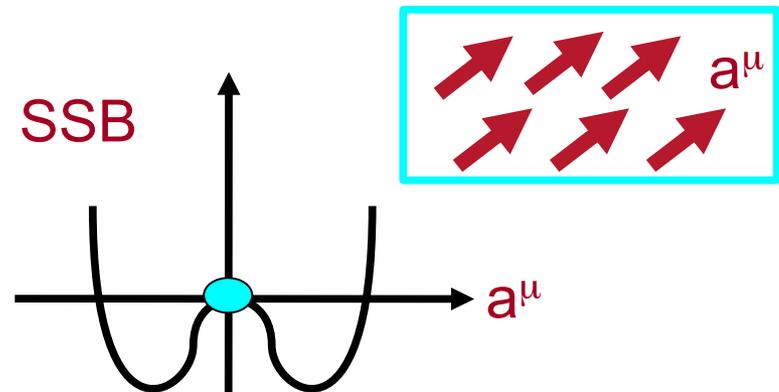
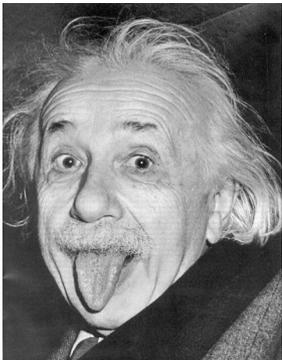
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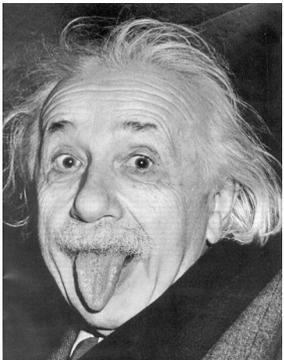
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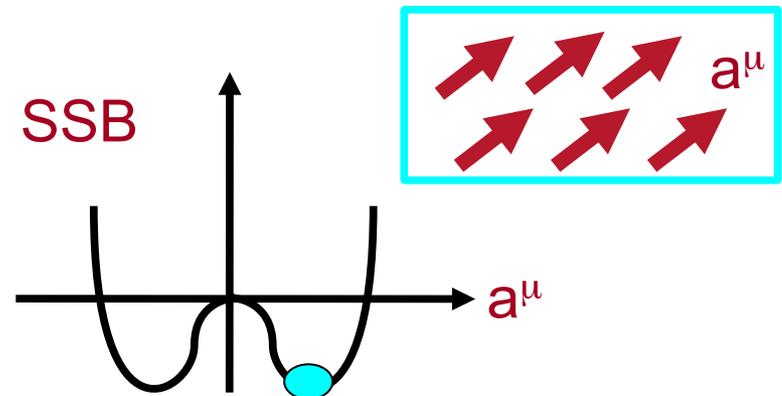
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Lorentz symmetry  
is spontaneously  
broken!



# 1. Spontaneous Lorentz symmetry breaking

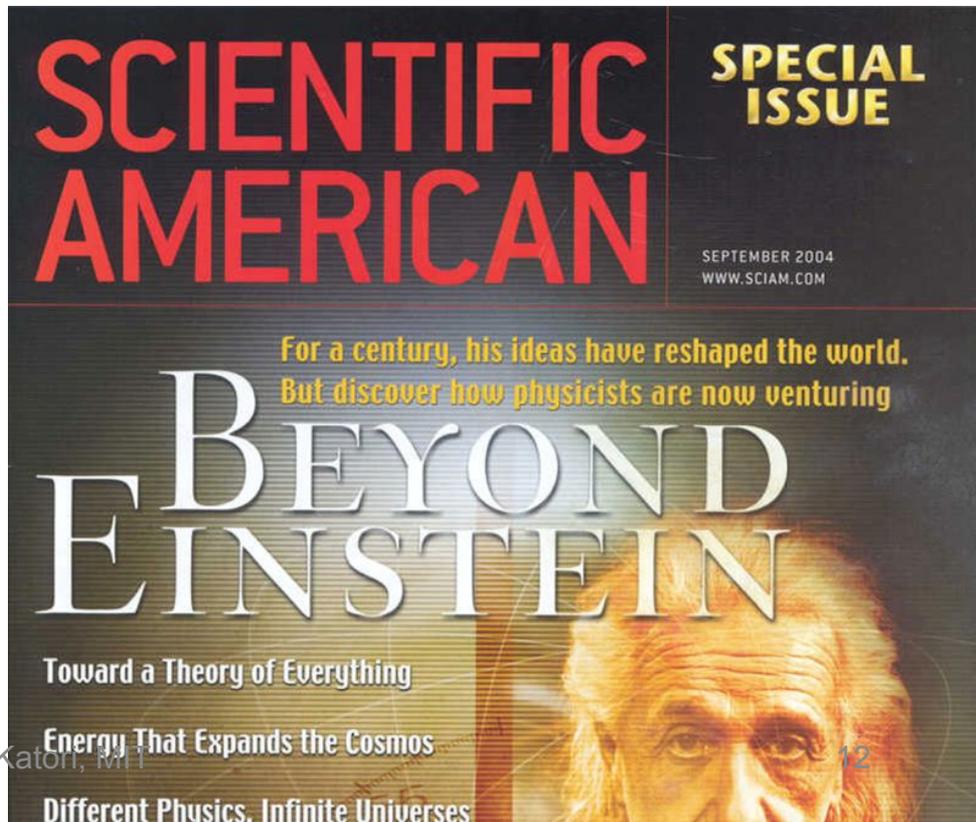
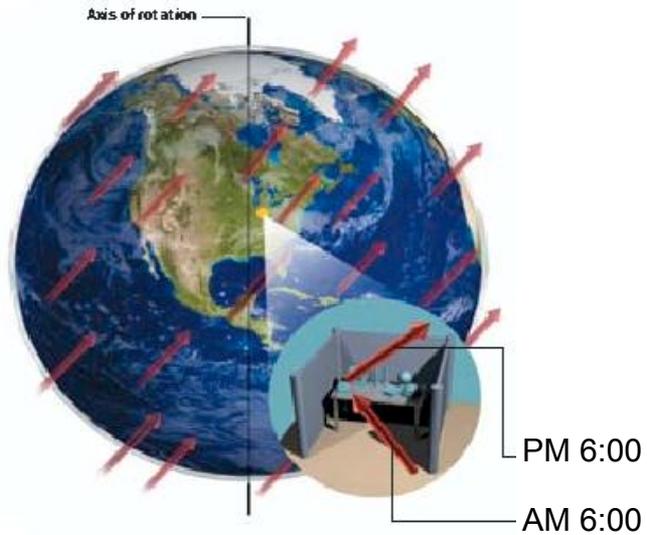
Test of Lorentz violation is to find the coupling of these background fields and ordinary fields (electrons, muons, neutrinos etc), then physical quantities may depend on the rotation of the earth.

vacuum Lagrangian for fermion

$$L = i\bar{\Psi}\gamma_{\mu}\partial^{\mu}\Psi - m\bar{\Psi}\Psi + \bar{\Psi}\gamma_{\mu}a^{\mu}\Psi + \bar{\Psi}\gamma_{\mu}c^{\mu\nu}\partial_{\nu}\Psi \dots$$

background field of the universe

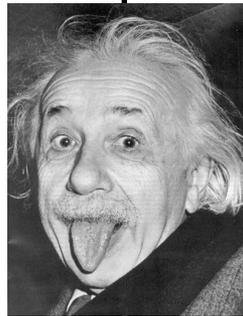
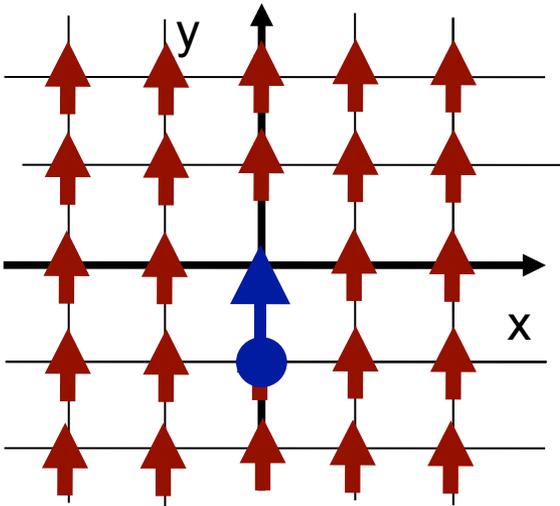
Scientific American (Sept. 2004)



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## 2. What is Lorentz violation?

$$\bar{\Psi}(x)\gamma_{\mu}a^{\mu}\Psi(x)$$

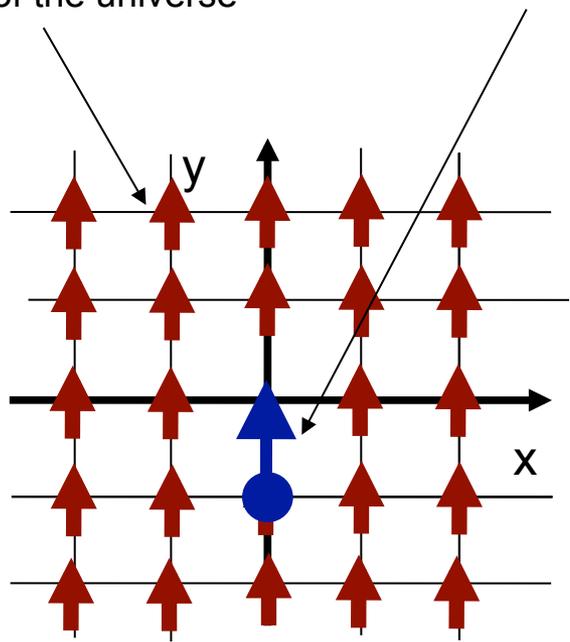


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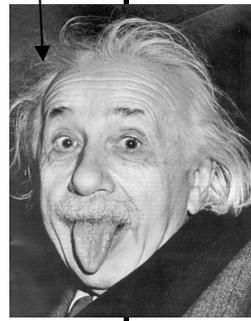
$$\bar{\Psi}(x)\gamma_{\mu}a^{\mu}\Psi(x)$$

background vector field of the universe

ex) moving particle



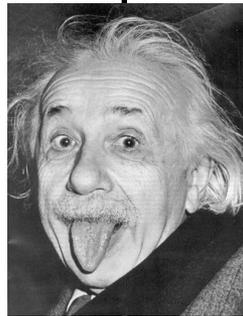
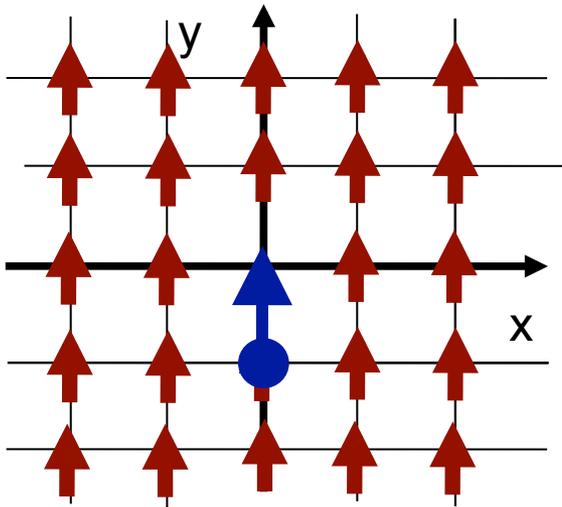
Einstein (observer)



## 2. What is Lorentz violation?

Under the **particle** Lorentz Transformation;

$$U \bar{\Psi}(x) \gamma_{\mu} a^{\mu} \Psi(x) U^{-1}$$

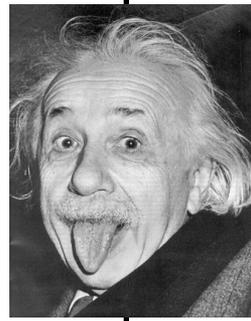
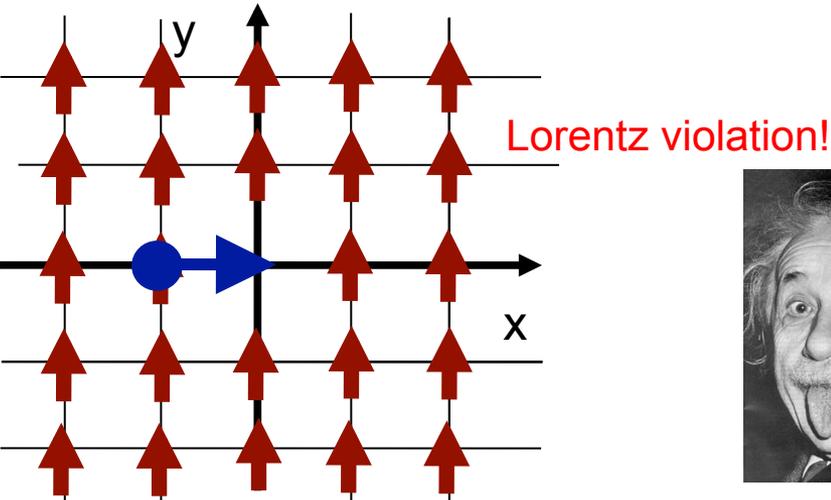


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Under the **particle** Lorentz Transformation;

$$\bar{\Psi}(x)\gamma_{\mu}a^{\mu}\Psi(x) \rightarrow U[\bar{\Psi}(x)\gamma_{\mu}a^{\mu}\Psi(x)]U^{-1}$$
$$\neq \bar{\Psi}(\Lambda x)\gamma_{\mu}a^{\mu}\Psi(\Lambda x)$$

Lorentz violation is observable when particle is moving in the fixed coordinate space



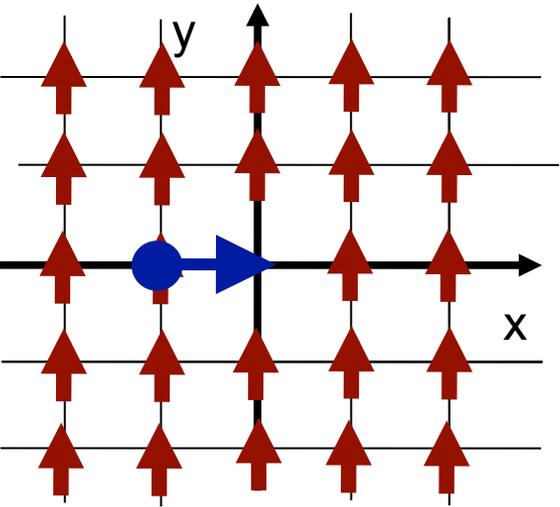
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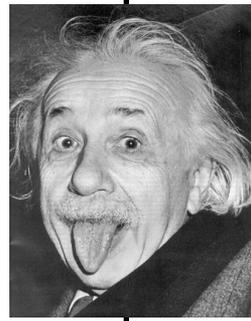
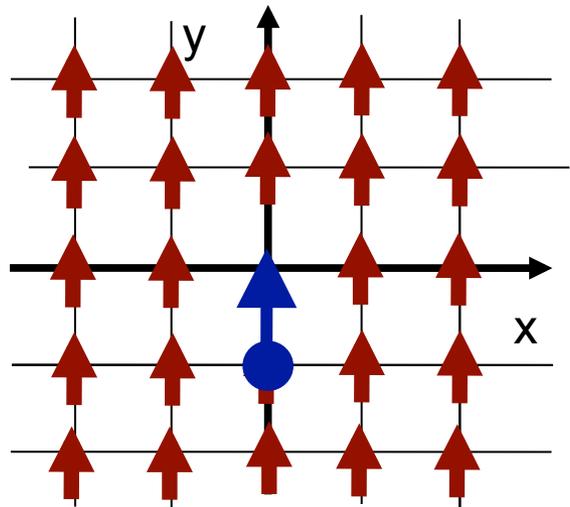
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Under the **observer** Lorentz Transformation;

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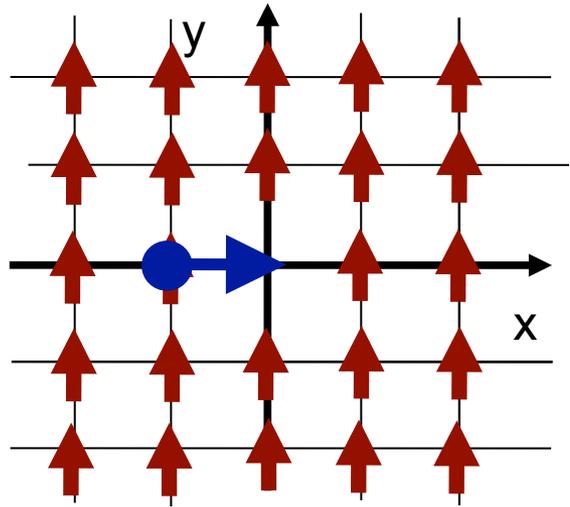
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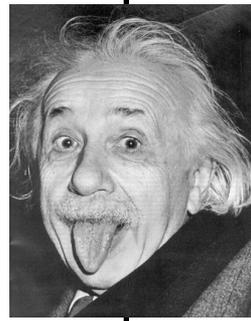
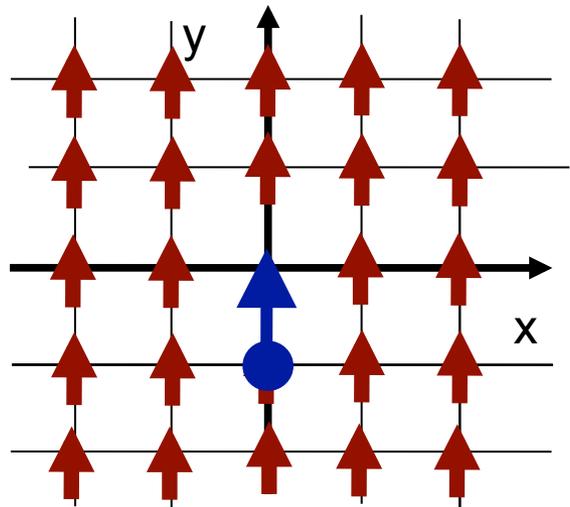
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Under the **observer** Lorentz Transformation;

$$\bar{\Psi}(x)\gamma_{\mu}a^{\mu}\Psi(x)$$

$$x \rightarrow \Lambda^{-1}x$$



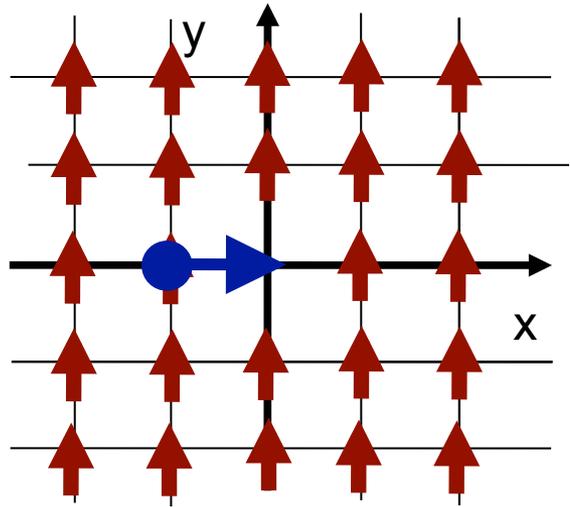
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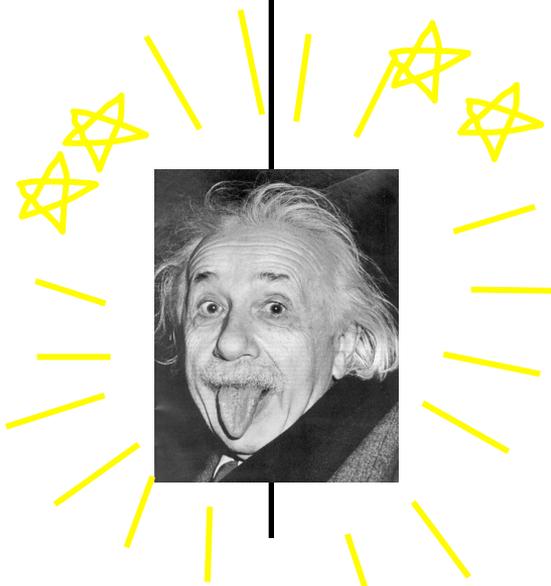
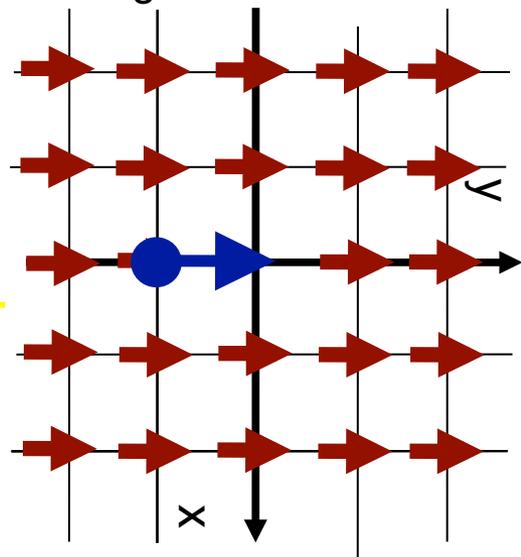


Under the **observer** Lorentz Transformation;

$$\bar{\Psi}(x)\gamma_{\mu}a^{\mu}\Psi(x) \xrightarrow{\Lambda^{-1}} \bar{\Psi}(\Lambda^{-1}x)\gamma_{\mu}a^{\mu}\Psi(\Lambda^{-1}x)$$

Lorentz violation cannot be seen by observers motion (coordinate transformation is unbroken)

any observers agree for all observations



## 2. What is CPT violation?

### Parity violation for weak current

$$J \sim \bar{\Psi}(\gamma_{\mu} - \gamma_{\mu}\gamma_5)\Psi \dots$$

under the parity transformation

$$\gamma_{\mu} \xrightarrow{P} P\gamma_{\mu}P^{-1} = -\gamma_{\mu} \quad \text{parity odd} \qquad \gamma_{\mu}\gamma_5 \xrightarrow{P} P\gamma_{\mu}\gamma_5P^{-1} = \gamma_{\mu}\gamma_5 \quad \text{parity even}$$

therefore, the current is not invariant under the parity transformation

$$J \xrightarrow{P} J \sim \bar{\Psi}(\gamma_{\mu} + \gamma_{\mu}\gamma_5)\Psi \dots$$

The combination cannot be invariant under the parity transformation, because each term change its sign differently.

In the case of CPT violation, the combination of CPT even and CPT odd term violate CPT symmetry, then **particle mass and anti-particle mass need not to be different for CPT violation.**

# 2. What is CPT violation?

What is the analogy of Parity violation?

QED Lagrangian

$$L = i\bar{\psi}\gamma_{\mu}\partial^{\mu}\psi - m\bar{\psi}\psi + ie\bar{\psi}\gamma_{\mu}A^{\mu}\psi\dots$$

$$L \xrightarrow{\text{CPT}} L' = \Theta[i\bar{\psi}\gamma_{\mu}\partial^{\mu}\psi]\Theta^{-1} - \Theta[m\bar{\psi}\psi]\Theta^{-1} + \Theta[ie\bar{\psi}\gamma_{\mu}A^{\mu}\psi]\Theta^{-1} \dots = L$$

CPT even
CPT even
CPT even...

CPT theorem guarantees all Lorentz invariant terms gives phase +1 (CPT-even), because there are always even number of Lorentz indices.

$$(-1)^{2n} = +1 \quad \Rightarrow \quad L \xrightarrow{\text{CPT}} L' = L$$

# 2. What is CPT violation?

Lorentz violation makes CPT-odd term in Lagrangian.

## QED Lagrangian with Lorentz violating terms

$$L = i\bar{\psi}\gamma_{\mu}\partial^{\mu}\psi - m\bar{\psi}\psi + ie\bar{\psi}\gamma_{\mu}A^{\mu}\psi + \boxed{\bar{\psi}\gamma_{\mu}a^{\mu}\psi} + \boxed{\bar{\psi}\gamma_{\mu}c^{\mu\nu}\partial_{\nu}\psi} \dots$$

$$L \xrightarrow{\text{CPT}} L' = \Theta[i\bar{\psi}\gamma_{\mu}\partial^{\mu}\psi]\Theta^{-1} - \Theta[m\bar{\psi}\psi]\Theta^{-1} + \Theta[ie\bar{\psi}\gamma_{\mu}A^{\mu}\psi]\Theta^{-1} \dots \neq L$$

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when you have odd number of particle Lorentz violating indices, CPT violation happens

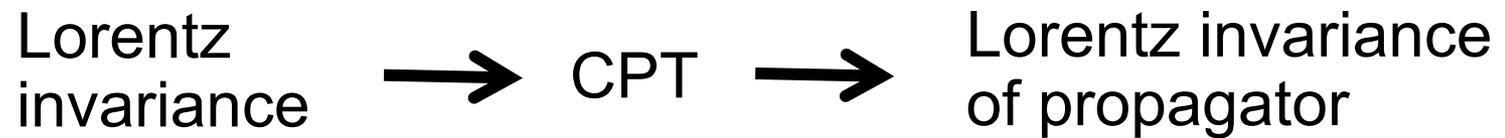
$$(-1)^{2n+1} = -1 \quad \Rightarrow \quad L \xrightarrow{\text{CPT}} L' \neq L$$

There are 2 types of Lorentz violation,

CPT-odd Lorentz violating coefficients (odd number Lorentz indices, ex.,  $a^{\mu}$ ,  $g^{\lambda\mu\nu}$ )

CPT-even Lorentz violating coefficients (even number Lorentz indices, ex.,  $c^{\mu\nu}$ ,  $\kappa^{\alpha\beta\mu\nu}$ )

## 2. CPT violation implies Lorentz violation



CPT violation implies Lorentz violation in interactive quantum field theory.

1. Spontaneous Lorentz symmetry breaking
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# 3. Standard Model Extension (SME)

## How to detect Lorentz violation?

Lorentz violation is realized as a coupling of particle fields and the background fields, so the basic strategy is to find the Lorentz violation is;

- (1) choose the coordinate system to compare the experimental result
- (2) write down Lagrangian including Lorentz violating terms under the formalism
- (3) write down the observables using this Lagrangian

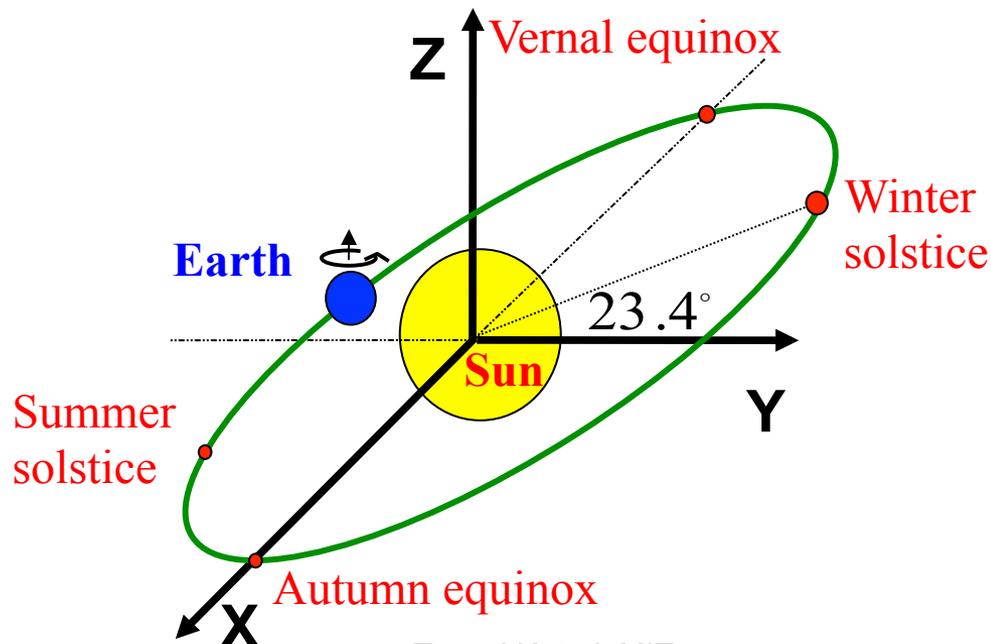
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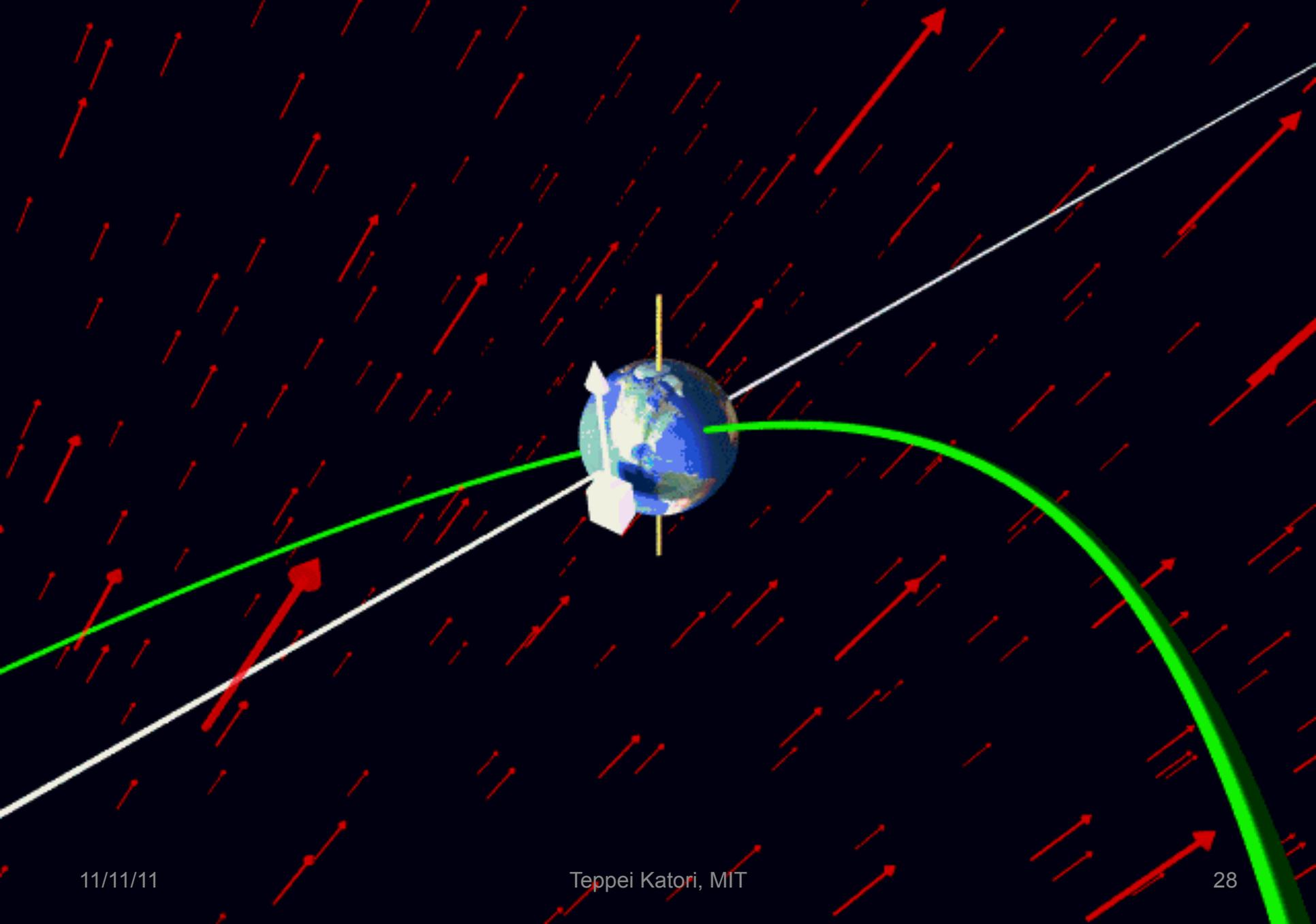
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The standard choice of the coordinate is Sun-centred celestial equatorial coordinates

As a standard formalism for the general search of Lorentz violation, **Standard Model Extension (SME)** is widely used in the community. SME is self-consistent low-energy effective theory with Lorentz and CPT violation within conventional QM (minimum extension of QFT with Particle Lorentz violation)

$$L_{\text{SME}} = L_{\text{SM}} + \delta L$$

$$\delta L = \bar{\Psi} \gamma_{\mu} a^{\mu} \Psi + \bar{\Psi} \gamma_{\mu} c^{\mu\nu} \partial_{\nu} \Psi \dots$$

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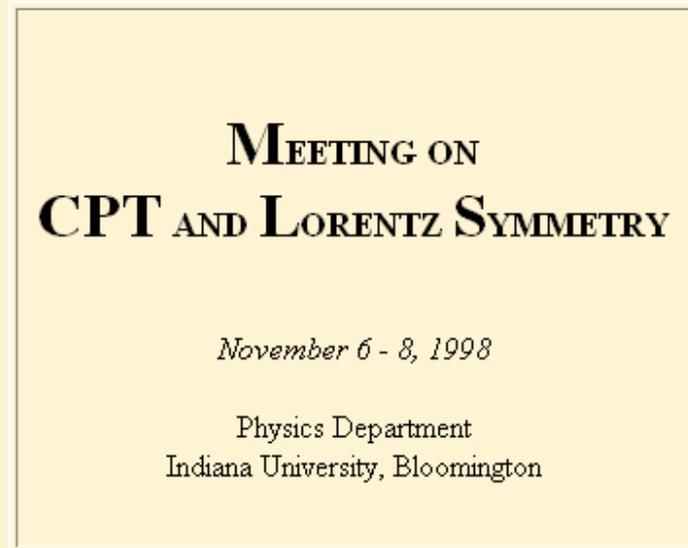
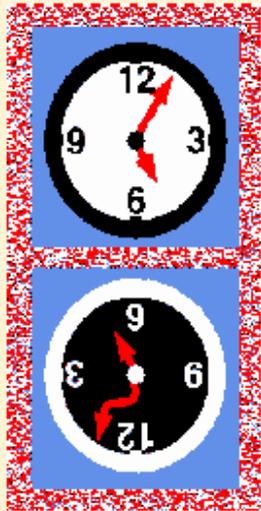
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The observables can be, energy spectrum, frequency of atomic transition, neutrino oscillation probability, etc. Among the non standard phenomena predicted by Lorentz violation, the smoking gun is the **sidereal time dependence** of the observables.

Dedicated group of people formed a meeting since 1998.

### 3. Modern tests of Lorentz violation

<http://www.physics.indiana.edu/~kostelec/faq.html>



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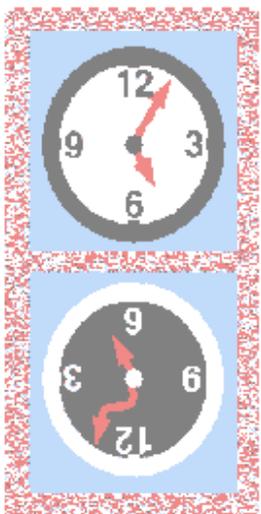
A meeting on CPT and Lorentz symmetry will be held in the [Physics Department, Indiana University](#) in [Bloomington](#), Indiana, U.S.A. on November 6 - 8, 1998. The meeting will focus on recent developments involving tests of these fundamental symmetries, including both experimental and theoretical aspects.

Topics to be covered include:

- experimental bounds on CPT and Lorentz symmetry from
  - ◊ measurements on K, B, and D mesons
  - ◊ precision comparisons of particle and antiparticle properties (anomalous moments, charge-to-mass ratios, lifetimes, etc.)
  - ◊ spectroscopy of hydrogen and antihydrogen
  - ◊ clock-comparison tests
  - ◊ properties of light
  - ◊ other tests
- theoretical descriptions of and constraints on possible violations

# 3. Modern tests of Lorentz violation

<http://www.physics.indiana.edu/~kostelec/faq.html>



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**MEETING ON  
CPT AND LORENTZ SYMMETRY**

Topics:

- \* experimental bounds on CPT and Lorentz symmetry from measurements on K, B, and D mesons
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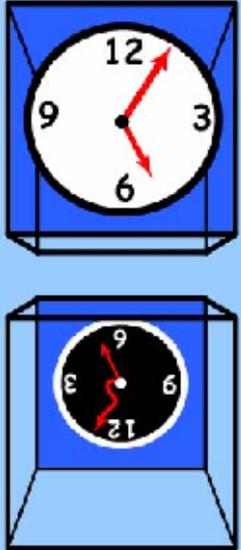
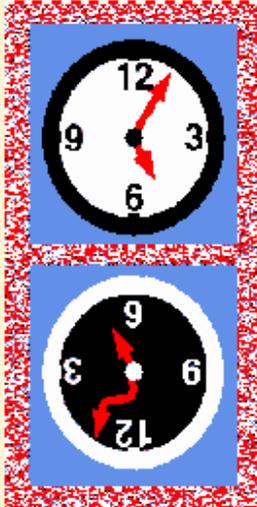
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# 3. Modern tests of Lorentz violation

The second meeting was in 2001.

<http://www.physics.indiana.edu/~kostelec/faq.html>



*Second Meeting on  
CPT and Lorentz Symmetry*

*August 15-18, 2001*

**Indiana University, Bloomington**

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A meeting on CPT and Lorentz symmetry will be held in the [Physics Department, Indiana University](#) in [Bloomington, U.S.A.](#) on August 15-18, 2001. The meeting will focus on experimental tests of these fundamental symmetries and related issues, including scenarios for possible violations.

Subjects to be covered include:

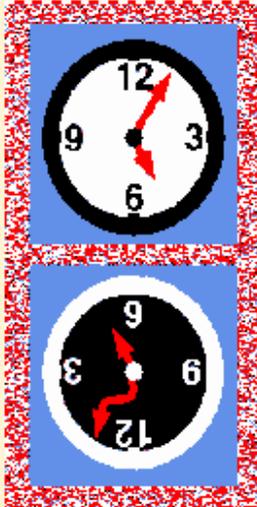
- experimental constraints on CPT and Lorentz symmetry from
  - ◊ oscillations and decays of K, B, D mesons and other particles
  - ◊ comparisons of particle and antiparticle properties
  - ◊ spectroscopy of hydrogen and antihydrogen

Teppei Katori, MIT

# 3. Modern tests of Lorentz violation

The second meeting was in 2004.

<http://www.physics.indiana.edu/~kostelec/faq.html>



[Meeting home](#)

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Tepei Katori, MIT

- experimental searches for CPT and Lorentz violations involving resonant cavity and interferometric behavior of photons

**Third Meeting on  
CPT and Lorentz Symmetry**

**August 4-7, 2004**

**Indiana University, Bloomington**

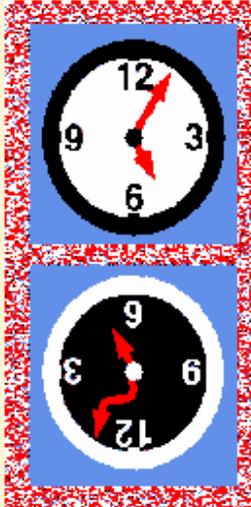
The Third Meeting on CPT and Lorentz Symmetry will be held in the [Physics Department](#) August 4-7, 2004. The meeting will focus on experimental tests of these fundamental symmetries and possible violations.

Subjects to be covered include:

# 3. Modern tests of Lorentz violation

The second meeting was in 2007.

<http://www.physics.indiana.edu/~kostelec/faq.html>



[Meeting home](#)

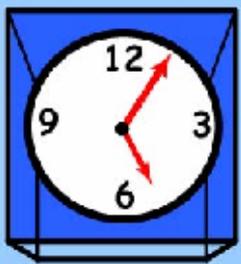
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Teppei Katori, MIT

**Fourth**  
**CPT and Lorentz**  
**August**  
**Indiana University**

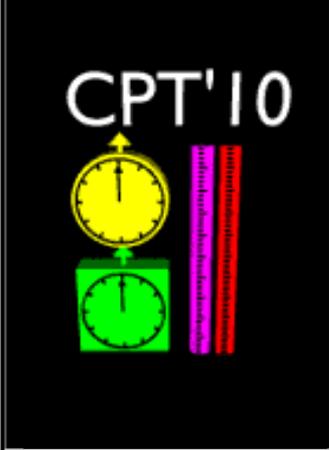
The Fourth Meeting on CPT and Lorentz Symmetry will be held in the U.S.A. on August 8-11, 2007. The meeting will focus on experimental tests of Lorentz symmetry, including scenarios for possible violations.

Subjects to be covered include:

# 3. Modern tests of Lorentz violation

The latest meeting was in summer 2010.

<http://www.physics.indiana.edu/~kostelec/faq.html>



## ***Fifth Meeting on***

# **CPT AND LORENTZ SYMMETRY**

## ***June 28-July 2, 2010***

### **Indiana University, Bloomington**

**MEETING LINKS**

[Meeting Home](#)  
[Registration](#)  
[Program](#)  
[Proceedings](#)  
[Travel](#)  
[Accommodations](#)

The *Fifth Meeting on CPT and Lorentz Symmetry* will be held in the [Physics Department, Indiana University](#) in [Bloomington](#), Indiana, U.S.A. on June 28-July 2, 2010. The meeting will focus on tests of these fundamental symmetries and on related theoretical issues, including scenarios for possible violations.

Topics include:

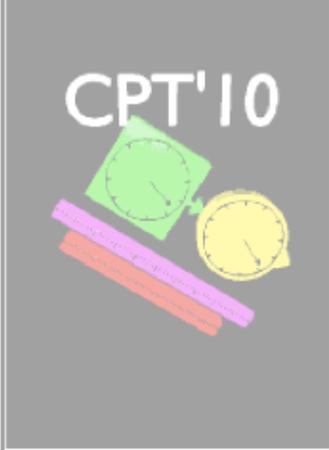
- searches for CPT and Lorentz violations involving
  - birefringence and dispersion from cosmological sources
  - clock-comparison measurements
  - CMB polarization
  - collider experiments
  - electromagnetic resonant cavities
  - equivalence principle
  - gauge and Higgs particles
  - high-energy astrophysical observations
  - laboratory and gravimetric tests of gravity

**LOCAL LINKS**

[IU Physics](#)  
[IU Astronomy](#)  
[IU Bloomington](#)  
[Bloomington area](#)

# 3. Modern tests of Lorentz violation

http://www.physics.indiana.edu/~kostelec/faq.html



**MEETING LINKS**

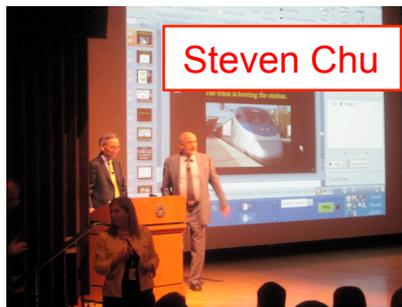
Meeting Home  
 Registration  
 Program  
 Proceedings  
 Travel  
 Accommodations

**LOCAL LINKS**

IU Physics  
 IU Astronomy  
 IU Bloomington  
 Bloomington area  
 11/11/11

- Topics:
- \* searches for CPT and Lorentz violations involving
    - birefringence and dispersion from cosmological sources
    - clock-comparison measurements
    - CMB polarization
    - collider experiments
    - electromagnetic resonant cavities
    - equivalence principle
    - gauge and Higgs particles
    - high-energy astrophysical observations
    - laboratory and gravimetric tests of gravity
    - matter interferometry
    - neutrino oscillations
    - oscillations and decays of K, B, D mesons
    - particle-antiparticle comparisons
    - post-newtonian gravity in the solar system and beyond
    - second- and third-generation particles
      - space-based missions
      - spectroscopy of hydrogen and antihydrogen
      - spin-polarized matter
  - \* theoretical studies of CPT and Lorentz violation involving
    - physical effects at the level of the Standard Model, General Relativity, and beyond
    - origins and mechanisms for violations
    - classical and quantum issues in field theory, particle physics, gravity, and strings

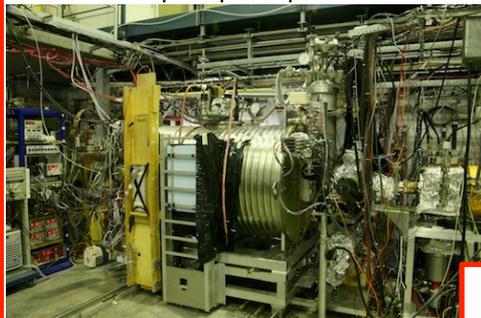
Atomic Interferometer  
(a,c)<sup>n,p,e</sup> < 10<sup>-6</sup>



Steven Chu

PRL106(2011)151102

CERN Antiproton Decelerator  
(M<sub>p</sub>-M<sub>p̄</sub>)/M<sub>p</sub> < 10<sup>-8</sup>



Nature419(2002)456

Veatron and LEP  
 $-5.8 \times 10^{-12} < \kappa_{tr} - 4/3 c_e^{00} < 1.2 \times 10^{-11}$



g-2 Δω<sub>a</sub> measurement  
b<sup>μ</sup> < 10<sup>-23</sup> GeV

GRB vacuum birefringence  
κ<sub>e+</sub>, κ<sub>e-</sub> < 10<sup>-37</sup>



PRL97(2006)140401

sources

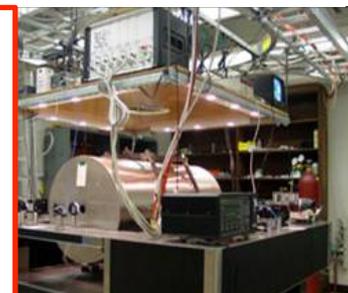
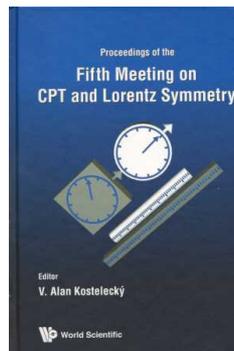
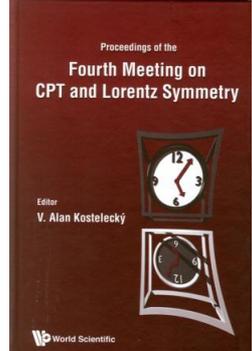
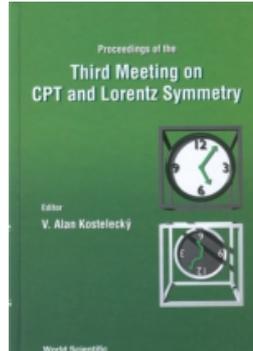
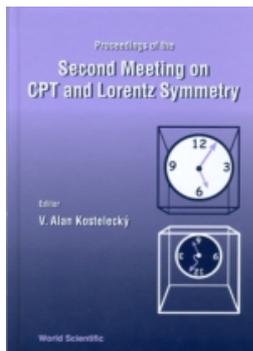
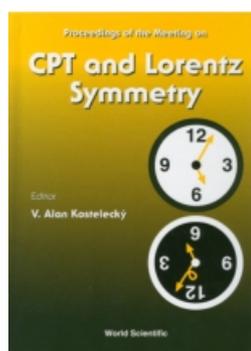
KTeV/KLOE (strange)  
Δa<sub>K</sub> < 10<sup>-22</sup> GeV

FOCUS

Δa<sub>D</sub> <  
BaBar/B  
Δm<sub>B</sub>



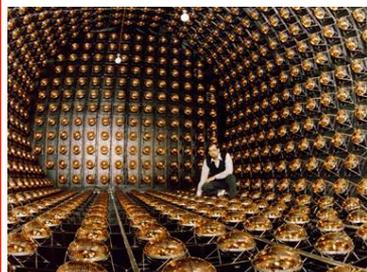
proceedings of Lorentz and CPT symmetry I, II, III, IV, V (world scientific)



mic optical resonator  
Δc/c < 10<sup>-16</sup>

second- and third-gen

LSND



PRD72(2005)076004

MINOS ND



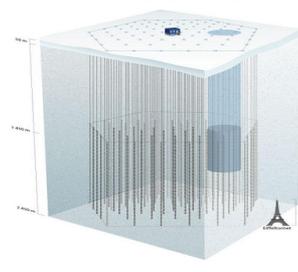
PRL101(2008)151601

MINOS FD



PRL105(2010)151601

IceCube



PRD82(2010)112003

MiniBooNE

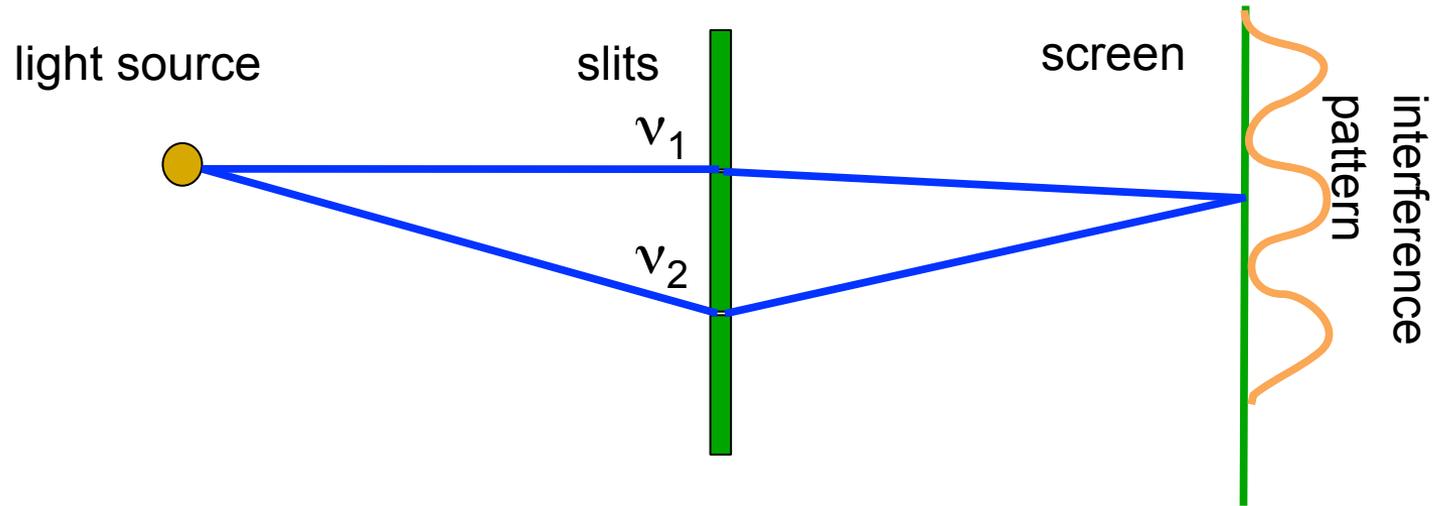


arXiv:1109.3480

1. Spontaneous Lorentz symmetry breaking
2. What is Lorentz and CPT violation?
3. Modern tests of Lorentz and CPT violation
- 4. Lorentz violation with neutrino oscillation**
5. MiniBooNE experiment
6. Lorentz violation with MiniBooNE neutrino data
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8. Conclusion

## 4. Lorentz violation with neutrino oscillation

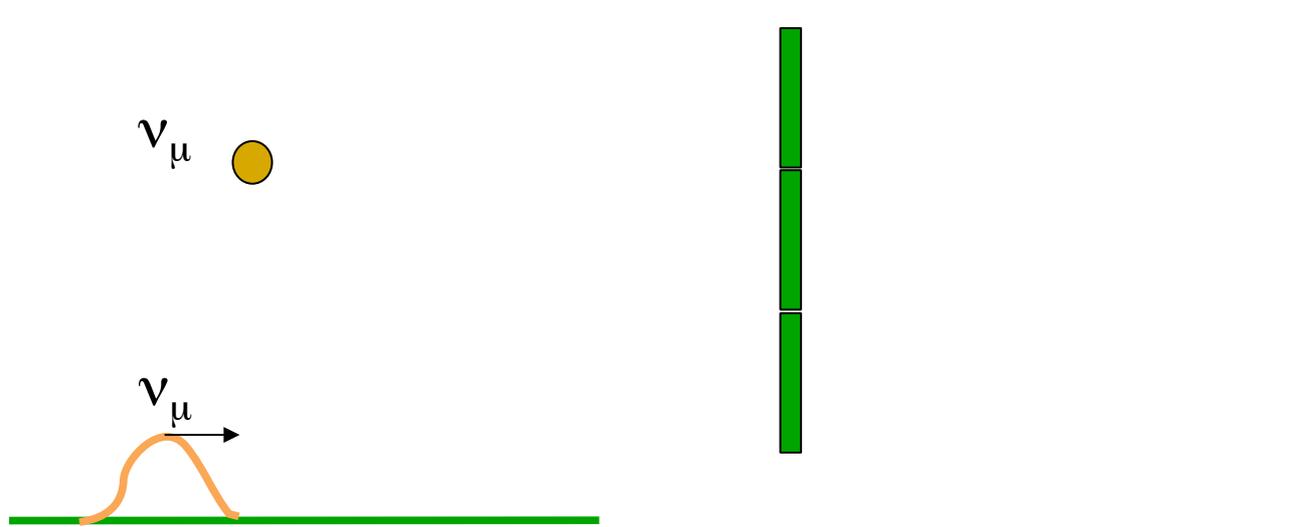
Neutrino oscillation is an interference experiment (cf. double slit experiment)



For double slit experiment, if path  $\nu_1$  and path  $\nu_2$  have different length, they have different phase rotations and it causes interference.

## 4. Lorentz violation with neutrino oscillation

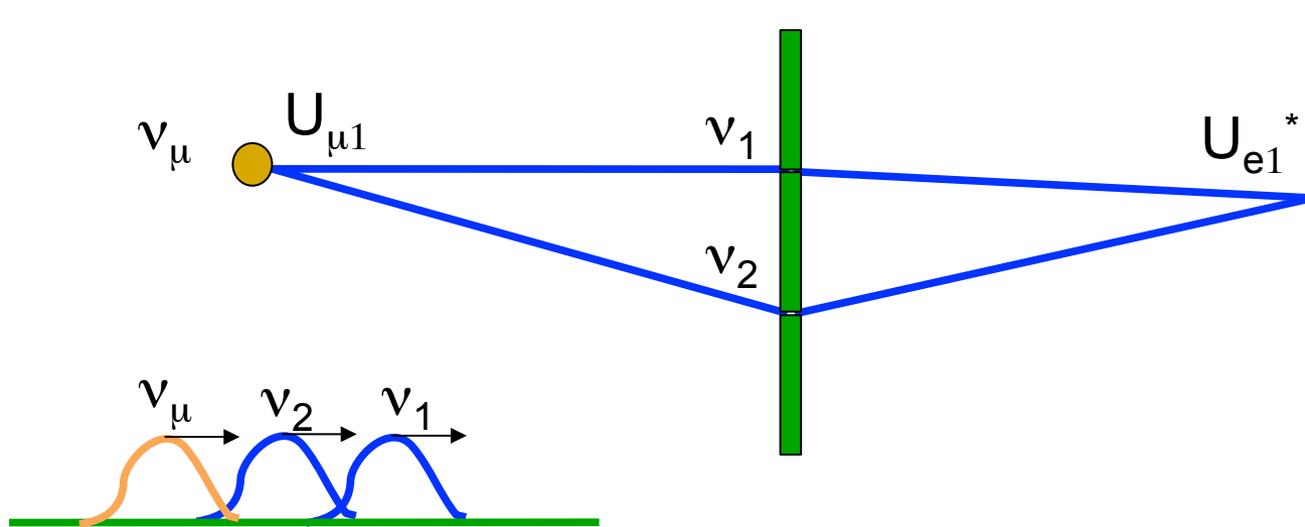
Neutrino oscillation is an interference experiment (cf. double slit experiment)



If 2 neutrino Hamiltonian eigenstates,  $\nu_1$  and  $\nu_2$ , have different phase rotation, they cause quantum interference.

## 4. Lorentz violation with neutrino oscillation

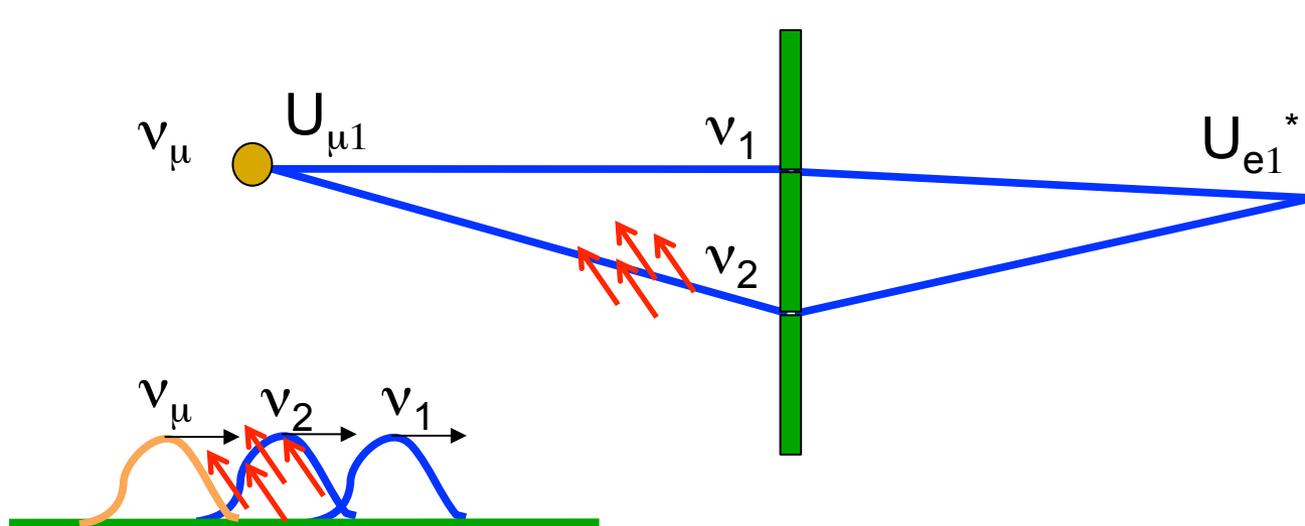
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Neutrino oscillation is an interference experiment (cf. double slit experiment)

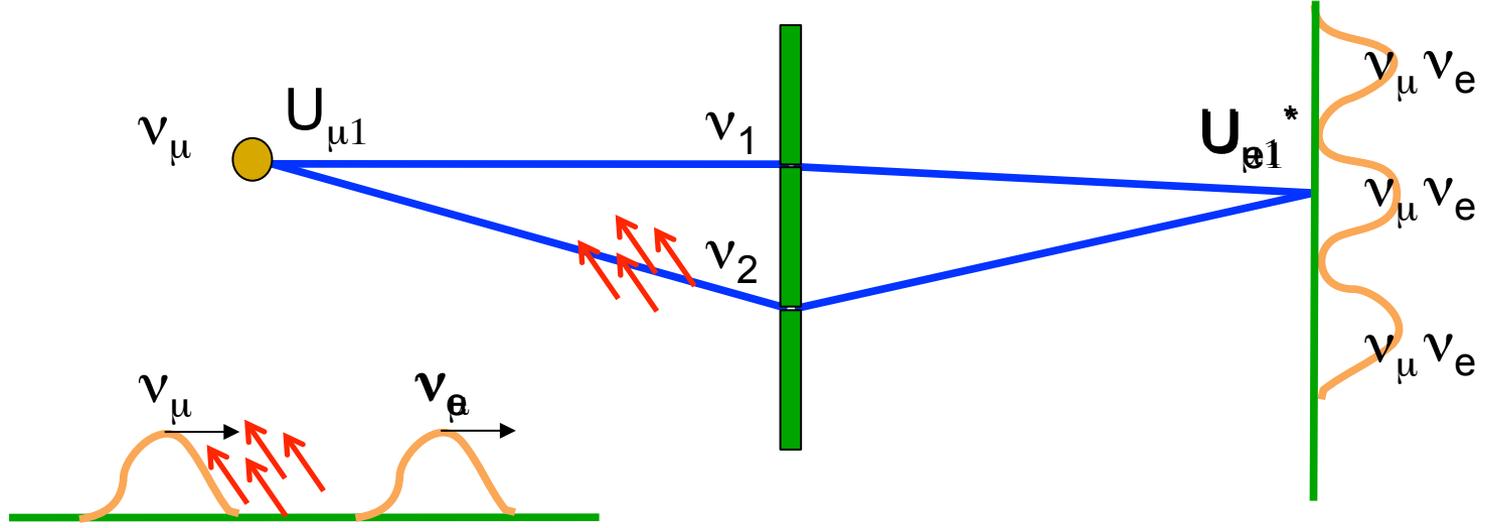


If 2 neutrino Hamiltonian eigenstates,  $\nu_1$  and  $\nu_2$ , have different phase rotation, they cause quantum interference.

If  $\nu_1$  and  $\nu_2$ , have different coupling with Lorentz violating field, interference fringe (oscillation pattern) depend on the sidereal motion.

# 4. Lorentz violation with neutrino oscillation

Neutrino oscillation is an interference experiment (cf. double slit experiment)



If 2 neutrino Hamiltonian eigenstates,  $\nu_1$  and  $\nu_2$ , have different phase rotation, they cause quantum interference.

If  $\nu_1$  and  $\nu_2$ , have different coupling with Lorentz violating field, interference fringe (oscillation pattern) depend on the sidereal motion.

The measured scale of neutrino eigenvalue difference is comparable the target scale of Lorentz violation ( $<10^{-19}\text{GeV}$ ).

## 4. Lorentz violation with neutrino oscillation

The neutrino weak eigenstate is described by neutrino Hamiltonian eigenstates,  $\nu_1$ ,  $\nu_2$ , and  $\nu_3$  and Hamiltonian mixing matrix elements.

$$|\nu_e\rangle = \sum_{i=1}^3 U_{ei} |\nu_i\rangle$$

The time evolution of neutrino weak eigenstate is written by Hamiltonian mixing matrix elements and eigenvalues of  $\nu_1$ ,  $\nu_2$ , and  $\nu_3$ .

$$|\nu_e(t)\rangle = \sum_{i=1}^3 U_{ei} e^{-i\lambda_i t} |\nu_i\rangle$$

Then the transition probability from weak eigenstate  $\nu_\mu$  to  $\nu_e$  is (assuming everything is real)

$$P_{\mu \rightarrow e}(t) = \left| \langle \nu_e(t) | \nu_\mu \rangle \right|^2 = -4 \sum_{i>j} (U_{\mu i} U_{\mu j} U_{ei} U_{ej}) \sin^2 \left( \frac{\Delta_{ij}}{2} L \right)$$

Especially, if we want to see the oscillatory shape of neutrino oscillation,

$$\frac{\Delta_{ij}(E)}{2} L \approx 1 \longrightarrow L \propto [\Delta_{ij}(E)]^{-1}$$

In the case of massive neutrino oscillation model,

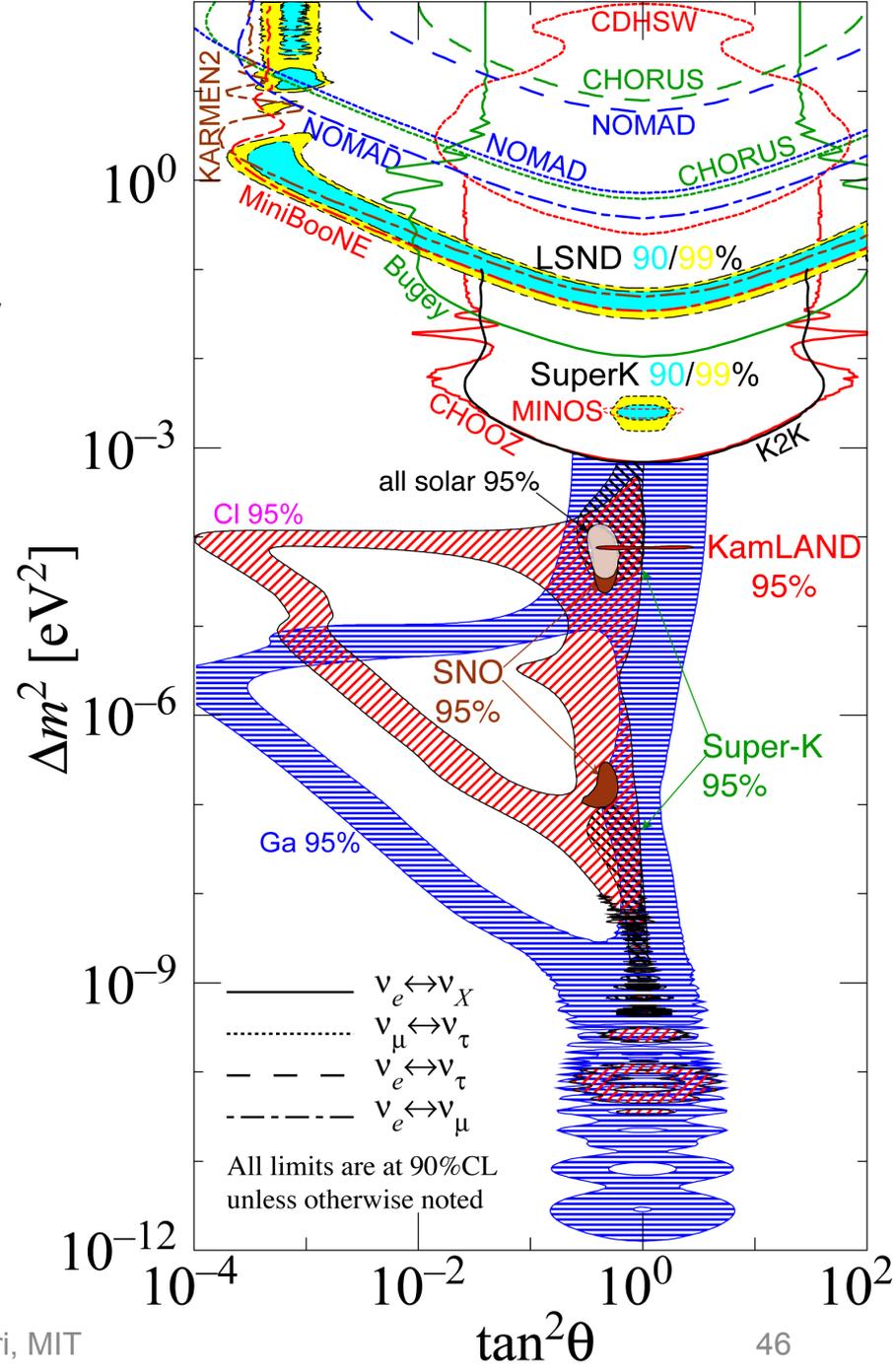
$$\frac{\Delta_{ij}(E)}{2} L \approx \frac{\Delta m^2}{4E} L \approx 1 \longrightarrow L \propto E$$

# 4. Neutrino standard Model ( $\nu$ SM)

This is the world data of neutrino oscillation, the positive oscillation signals are pinned down in very narrow region, and vast regions are rejected.

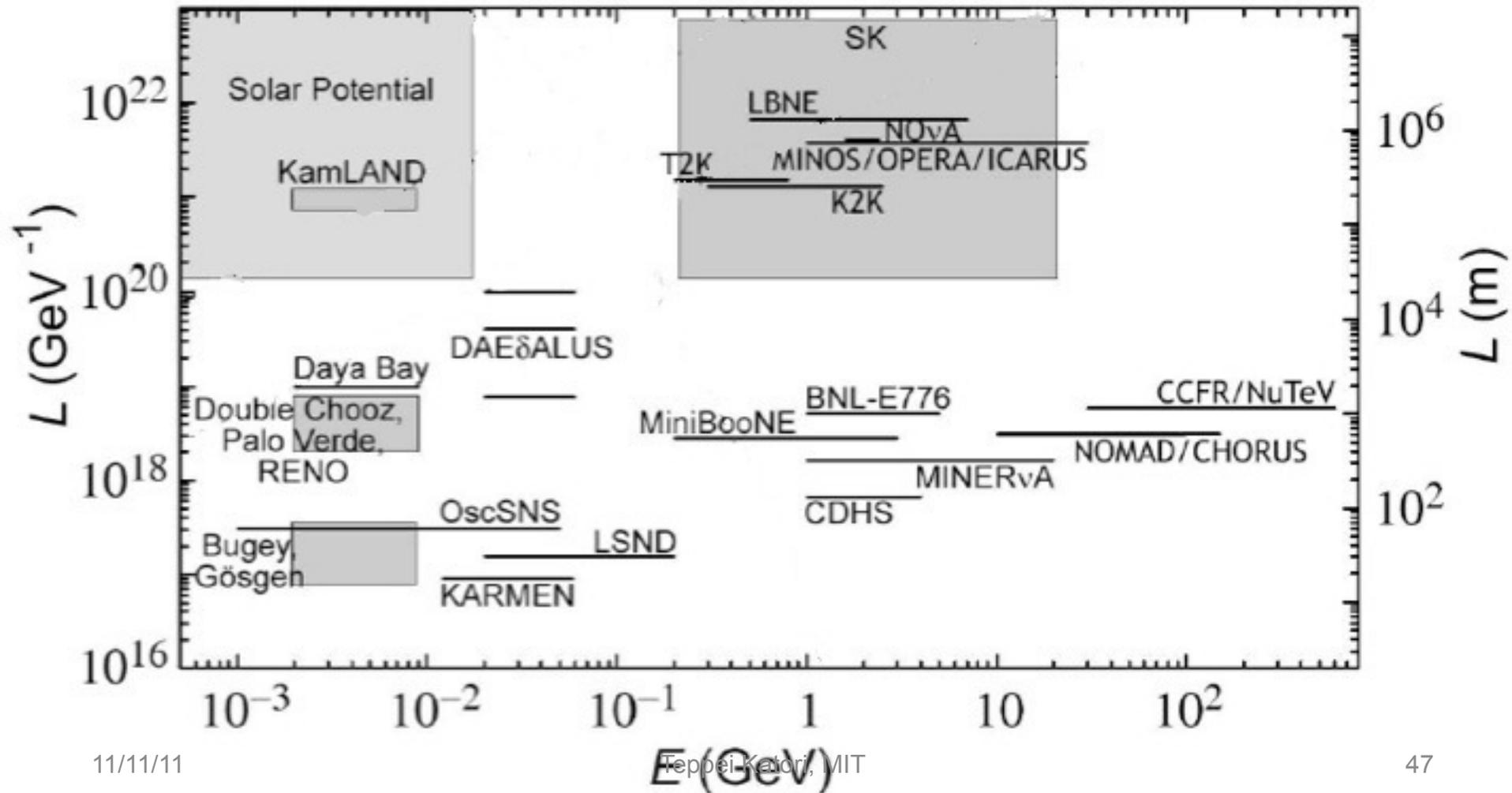
But this is model dependent diagram, because it assumes **neutrino mass as phase, and mass mixing matrix elements as amplitude of neutrino oscillations.**

What is model independent diagram look like?



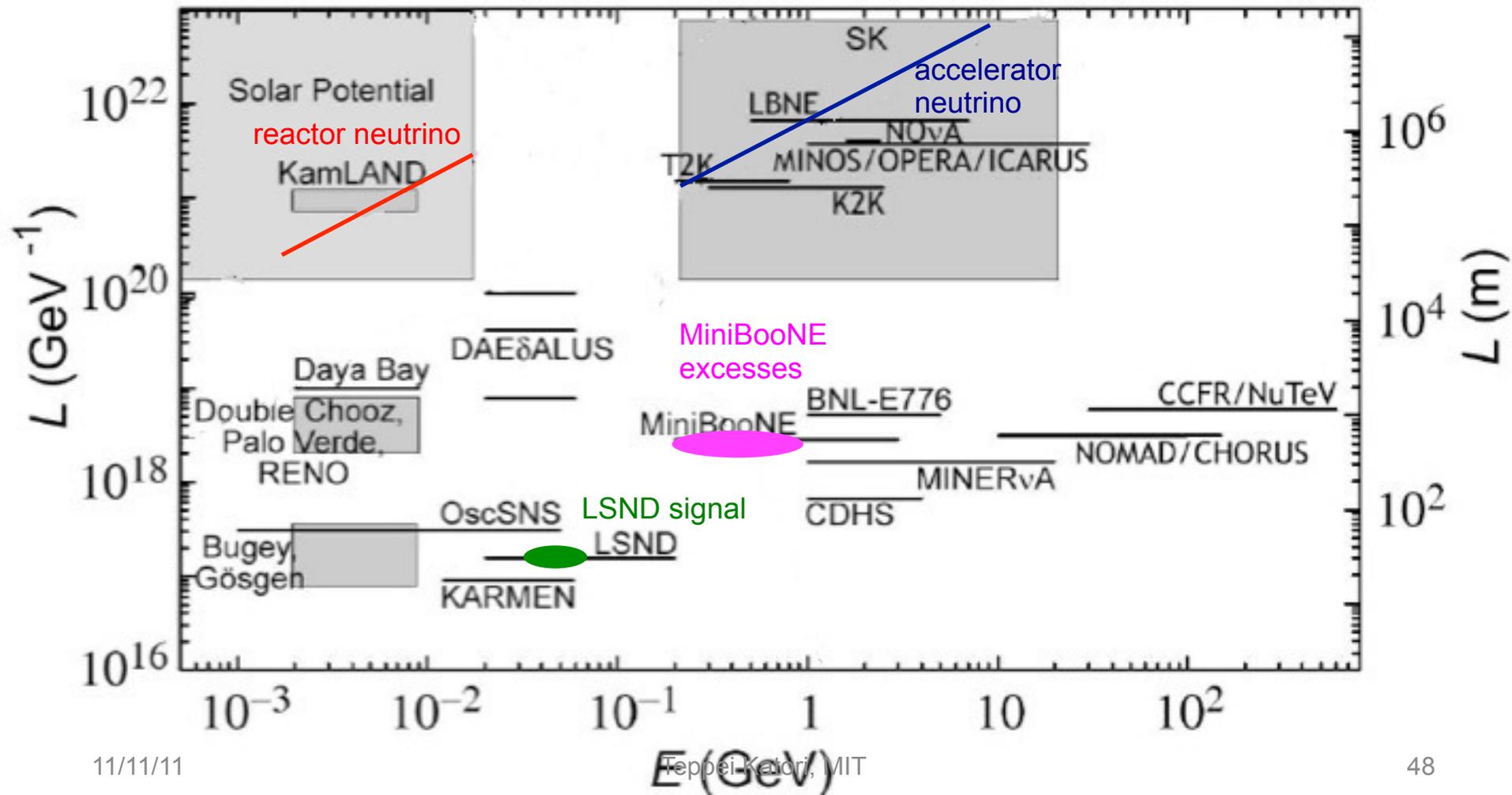
## 4. Lorentz violation with neutrino oscillation

Model independent neutrino oscillation data is the function of neutrino energy and baseline.



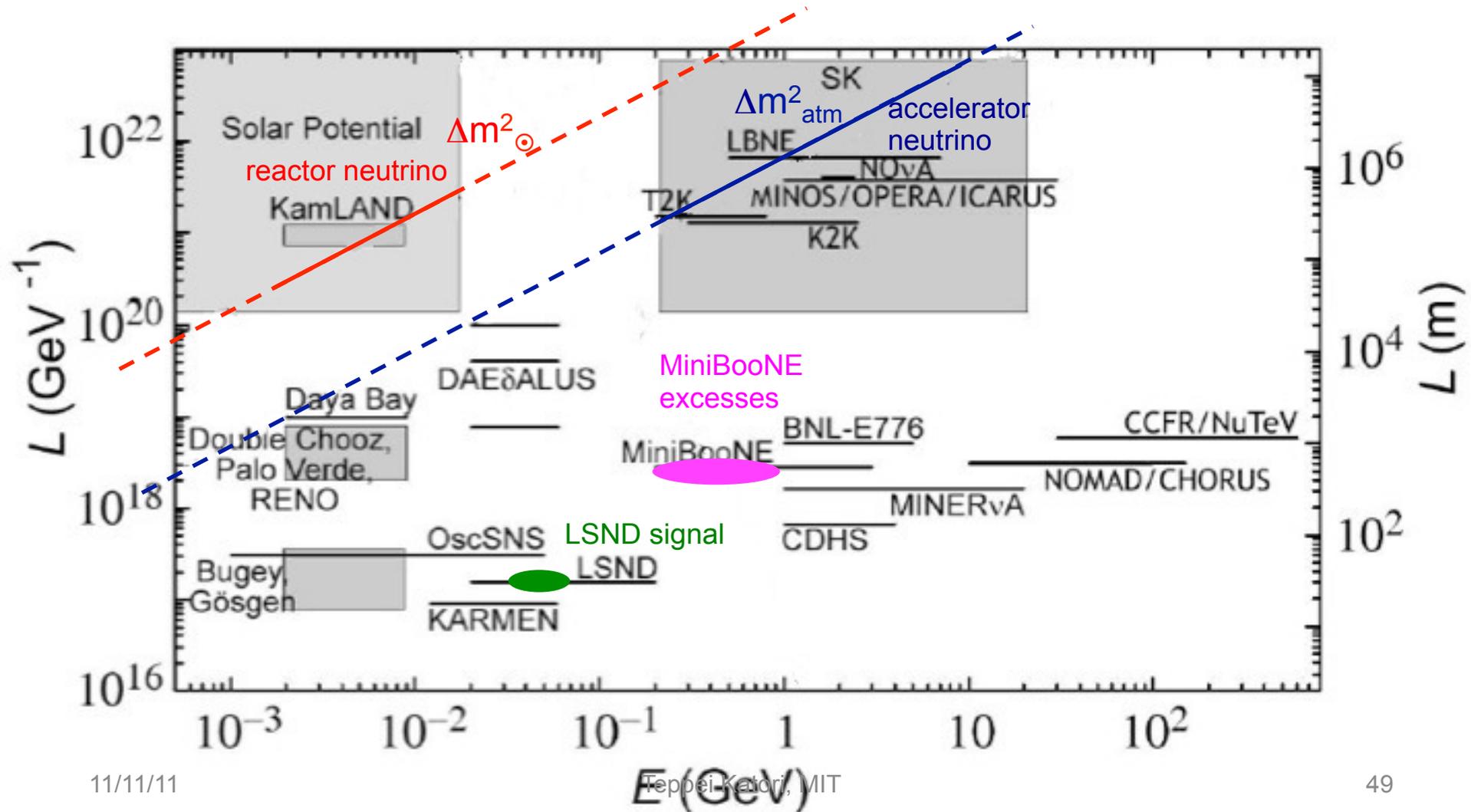
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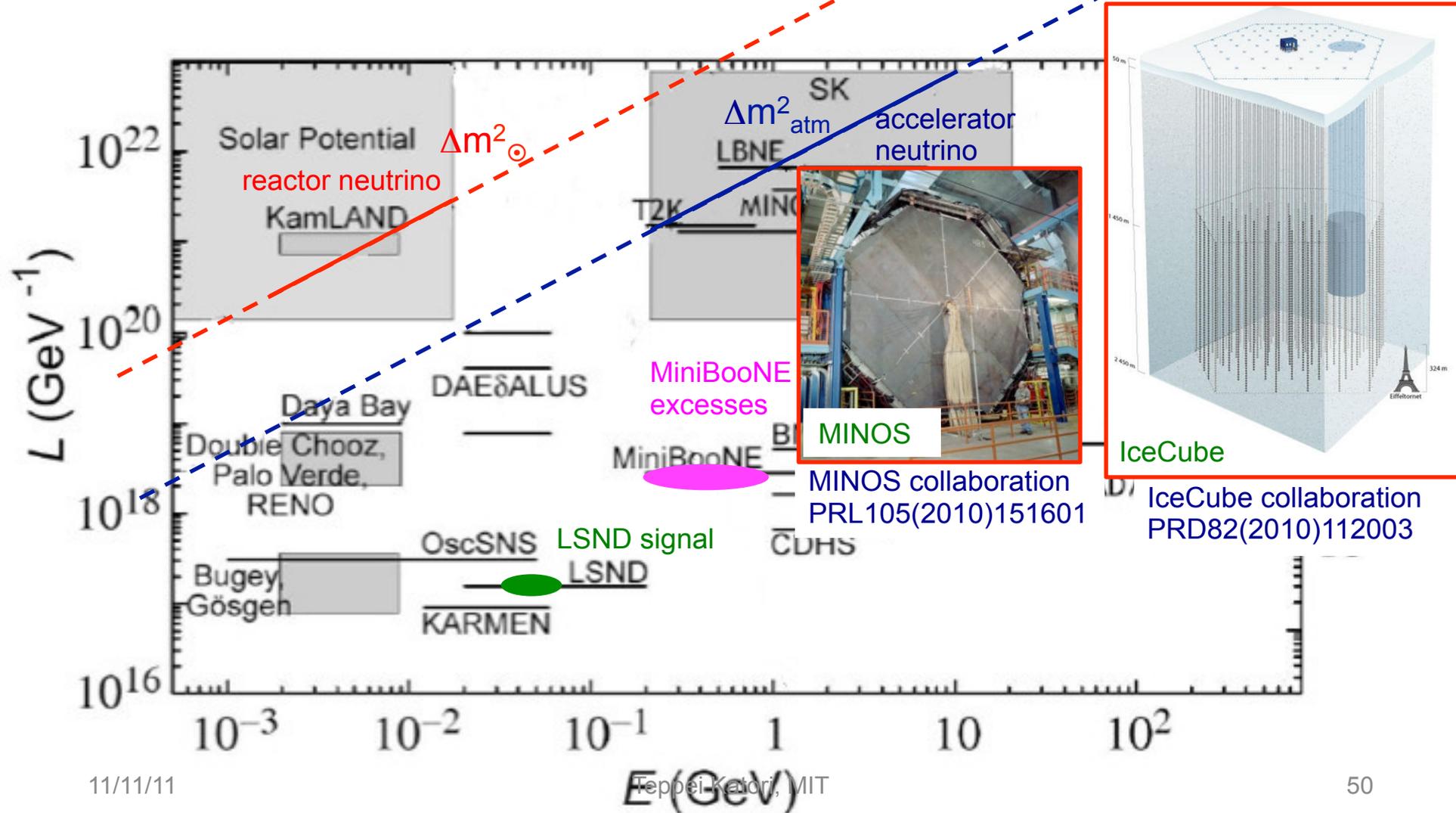
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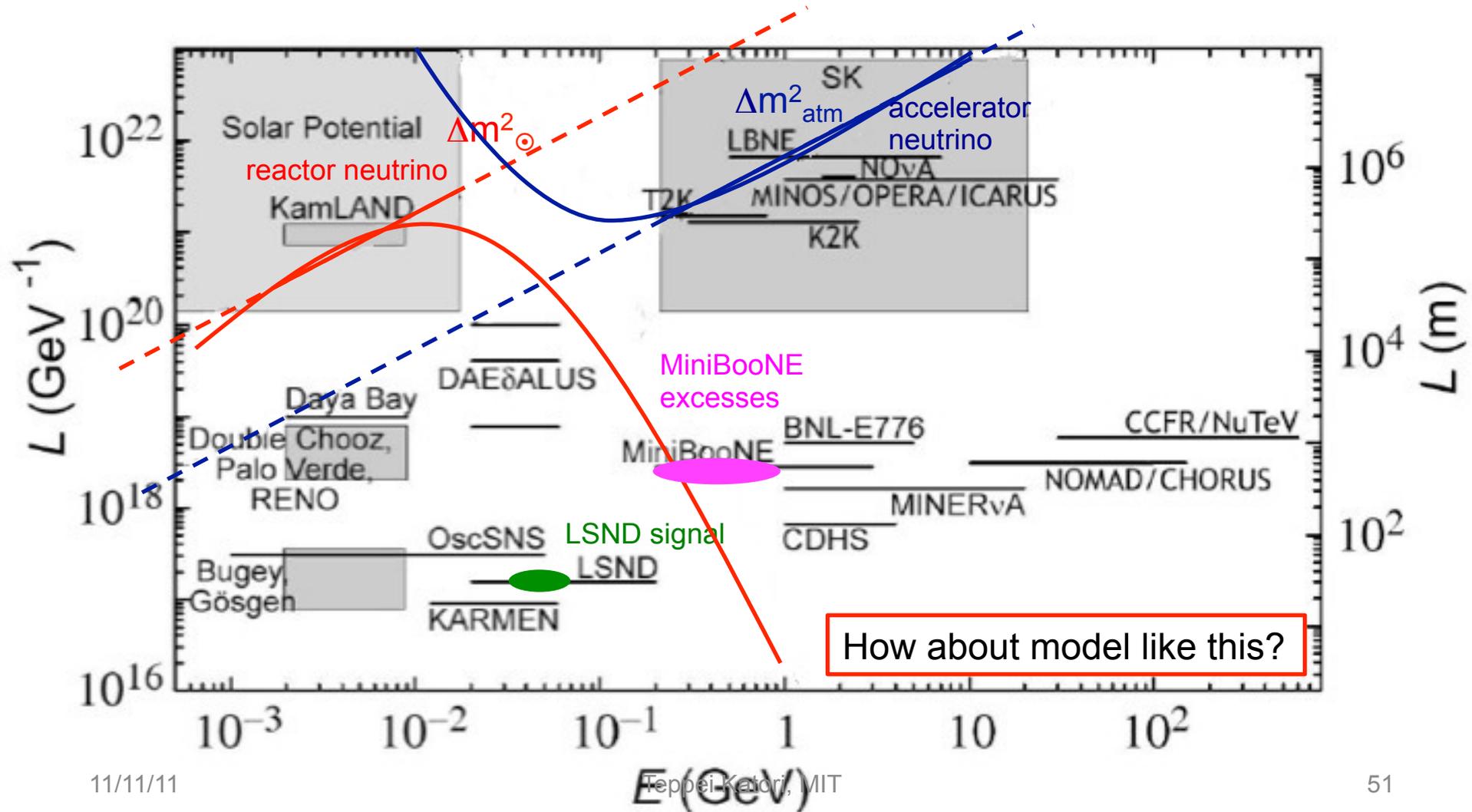
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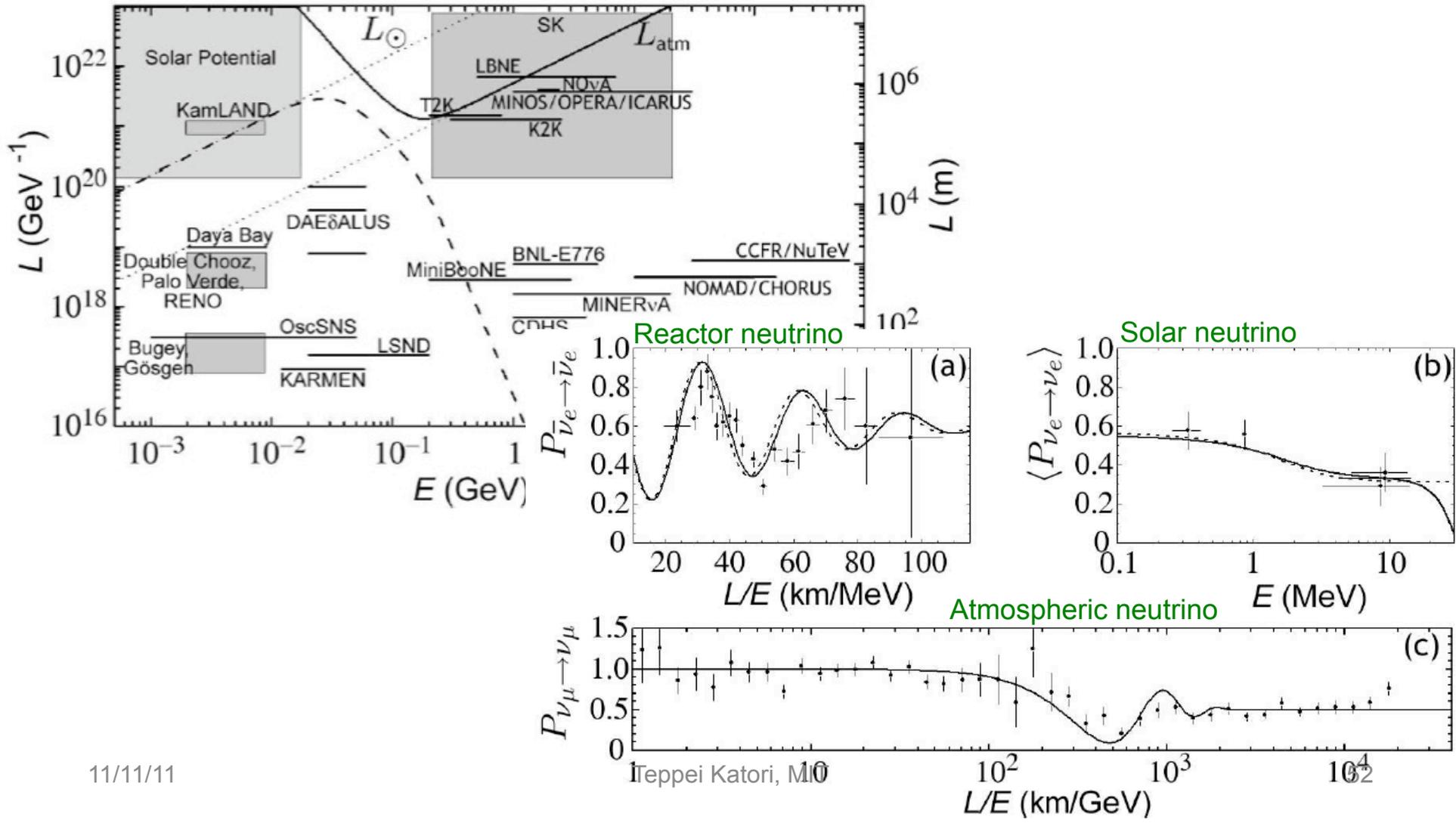
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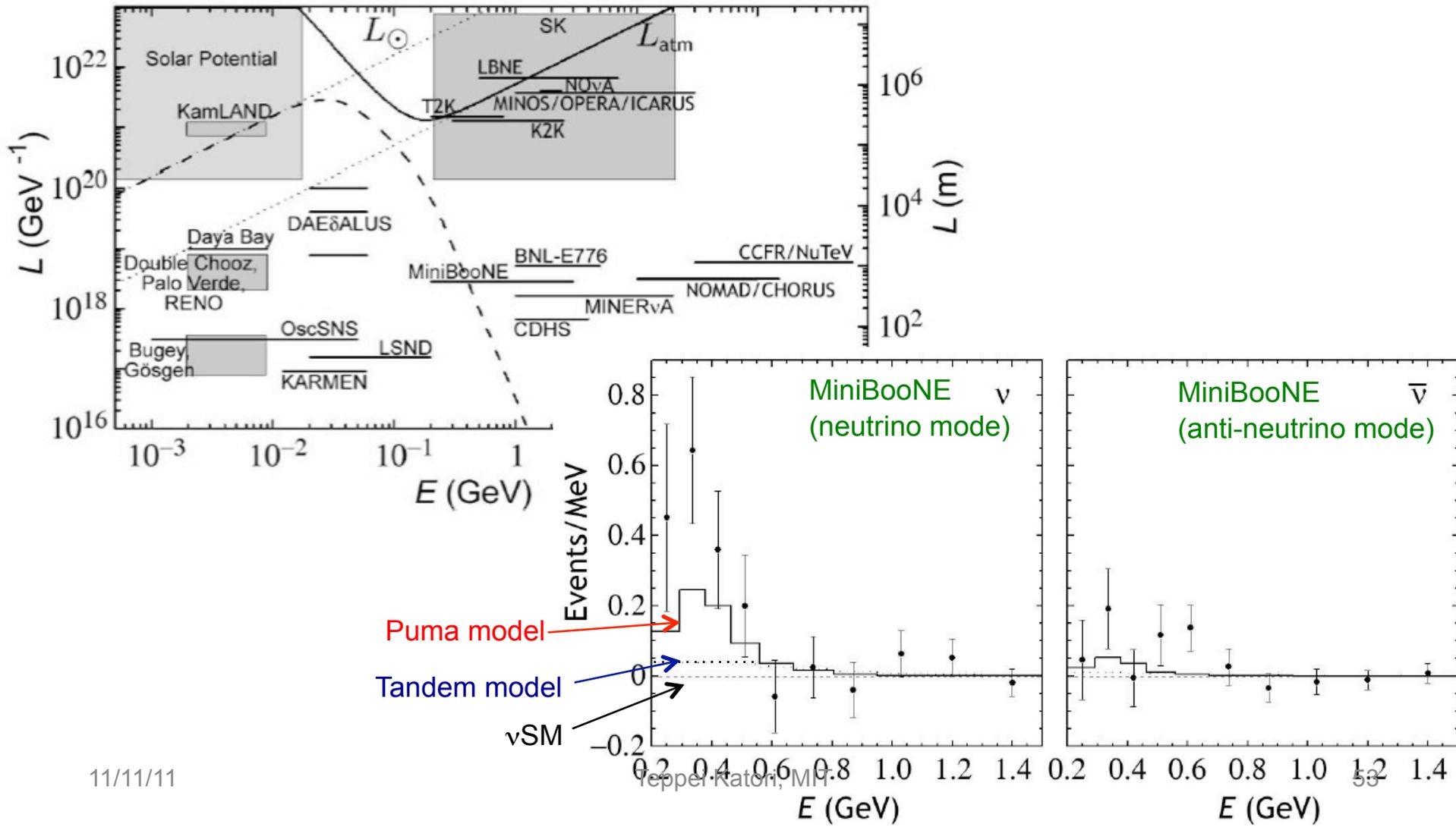
# 4. Puma model

Puma model has only 3 parameters, and perfectly describe all neutrino oscillation signal, including MiniBooNE low energy excess (neutrino mode only!)



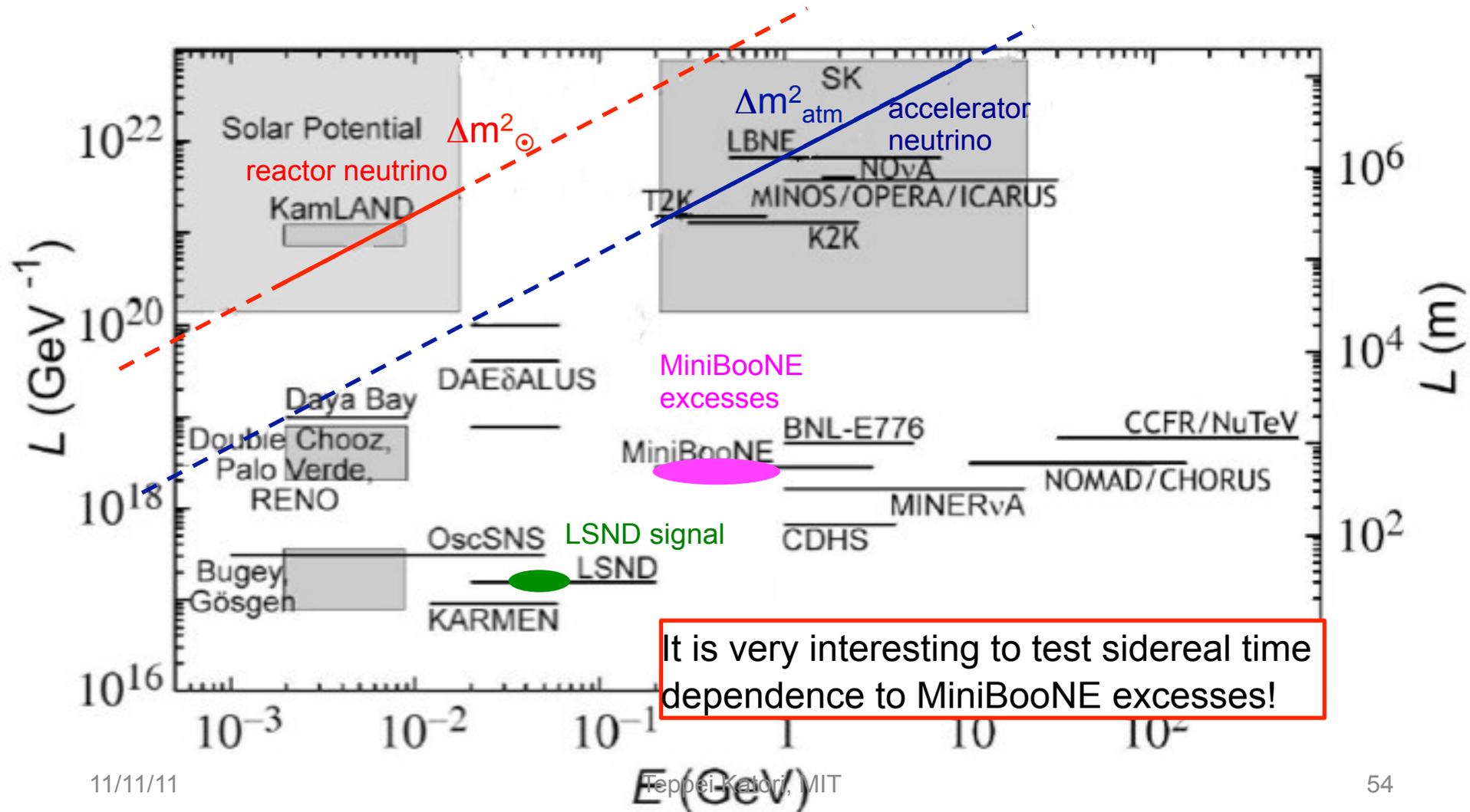
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## 4. Lorentz violation with neutrino oscillation

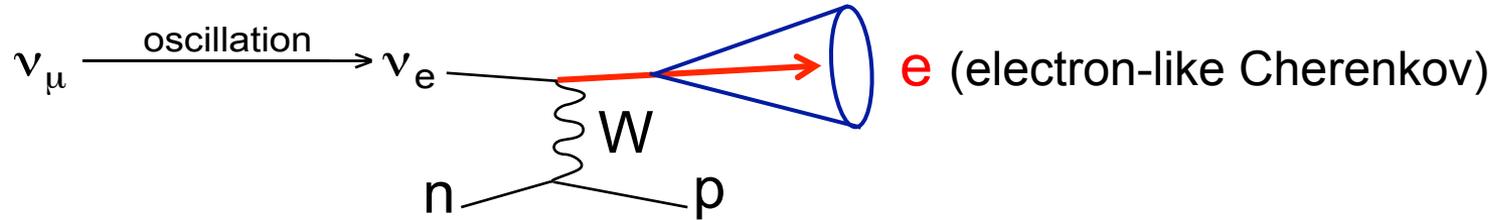
Model independent neutrino oscillation data is the function of neutrino energy and baseline.



1. Spontaneous Lorentz symmetry breaking
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6. Lorentz violation with MiniBooNE neutrino data
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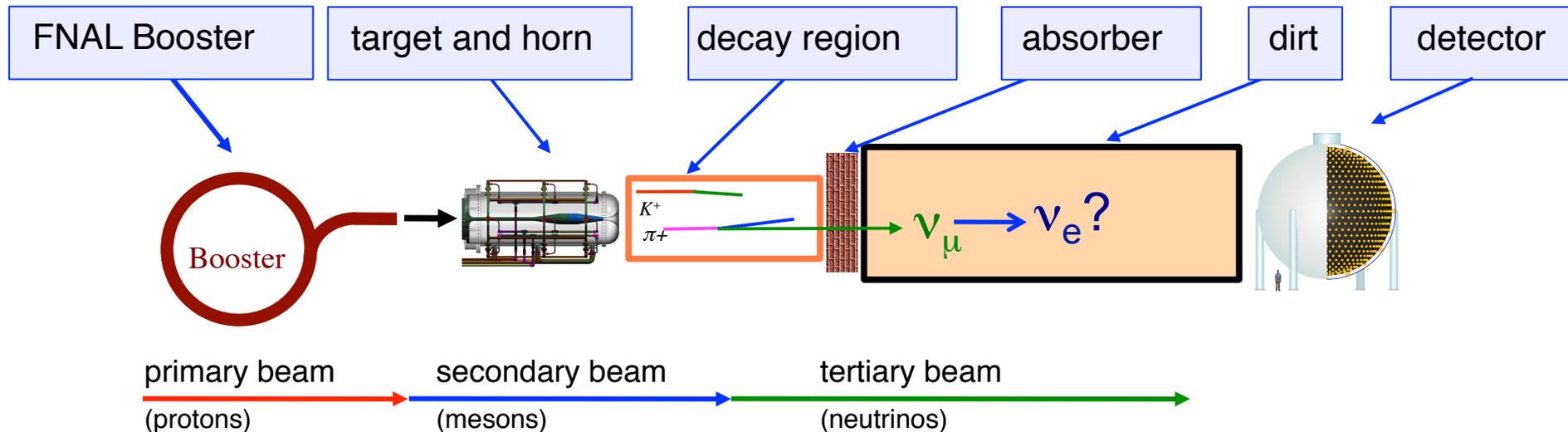
## 5. MiniBooNE experiment

MiniBooNE neutrino oscillation experiment at Fermilab is looking for  $\nu_\mu$  to  $\nu_e$  oscillation



Signature of  $\nu_e$  event is **the single isolated electron like events**

Booster Neutrino Beamline (BNB) creates  $\sim 800(600)$  MeV neutrino(anti-neutrino) by pion decay-in-flight from 8 GeV Booster protons on Be-target in the magnetic focusing horn.





# 5. MiniBooNE experiment

- **Muons**

  - **Sharp, clear rings**

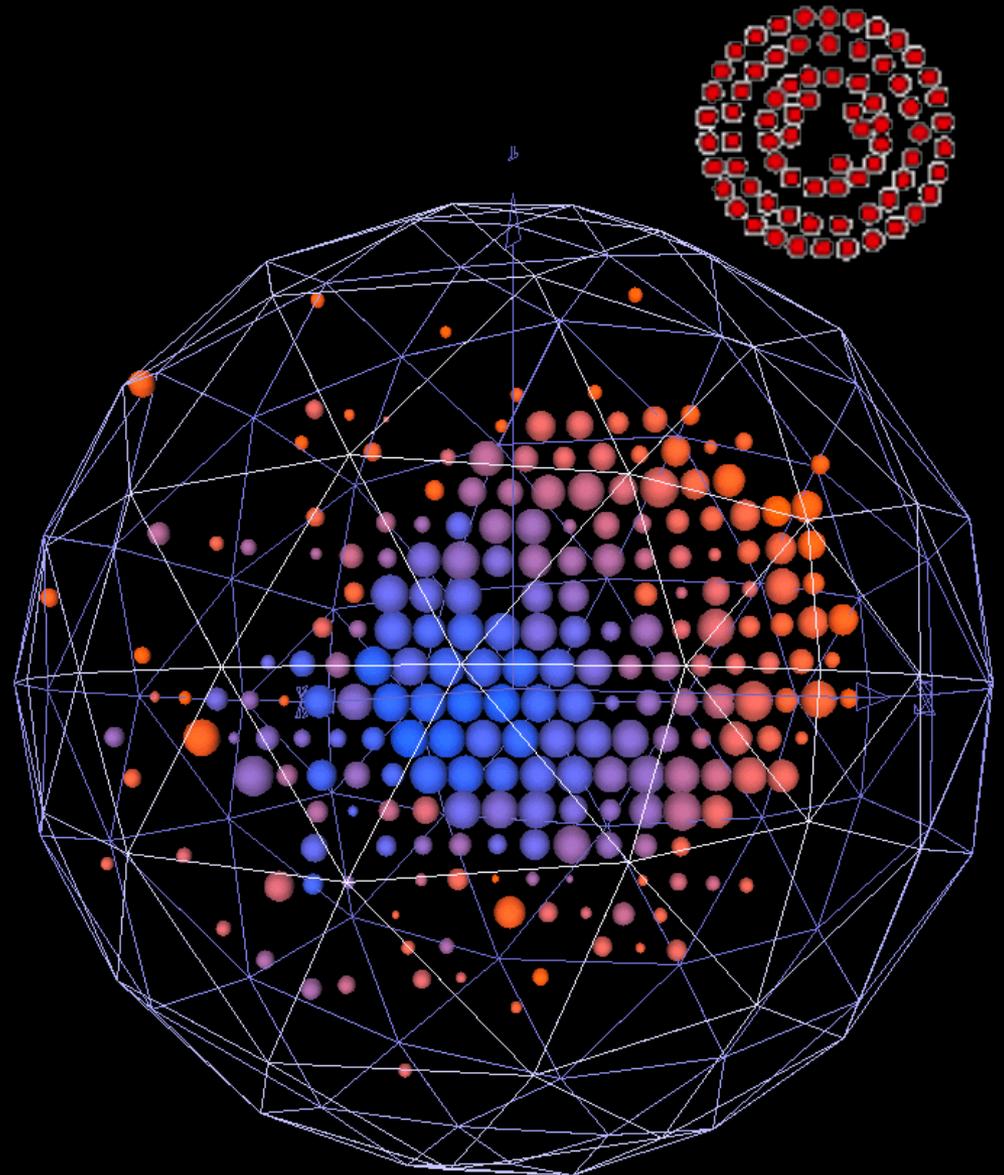
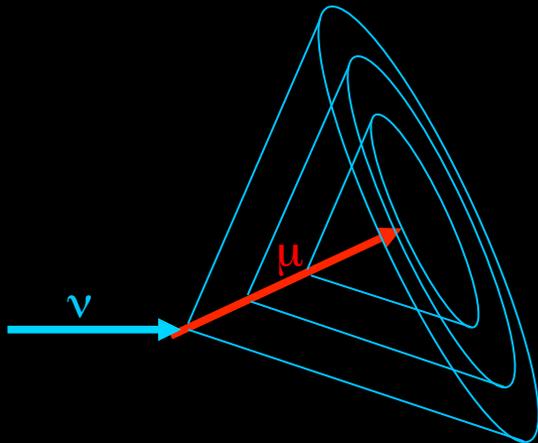
  - **Long, straight tracks**

- **Electrons**

  - **Scattered rings**

  - **Multiple scattering**

  - **Radiative processes**



# 5. MiniBooNE experiment

- Muons

  - Sharp, clear rings

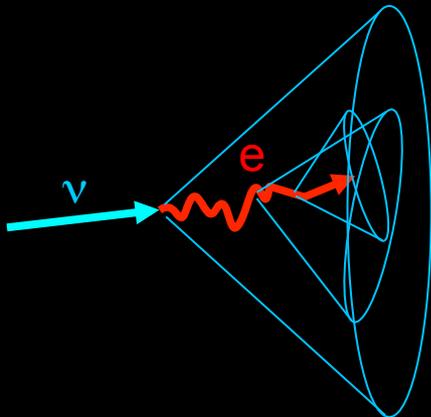
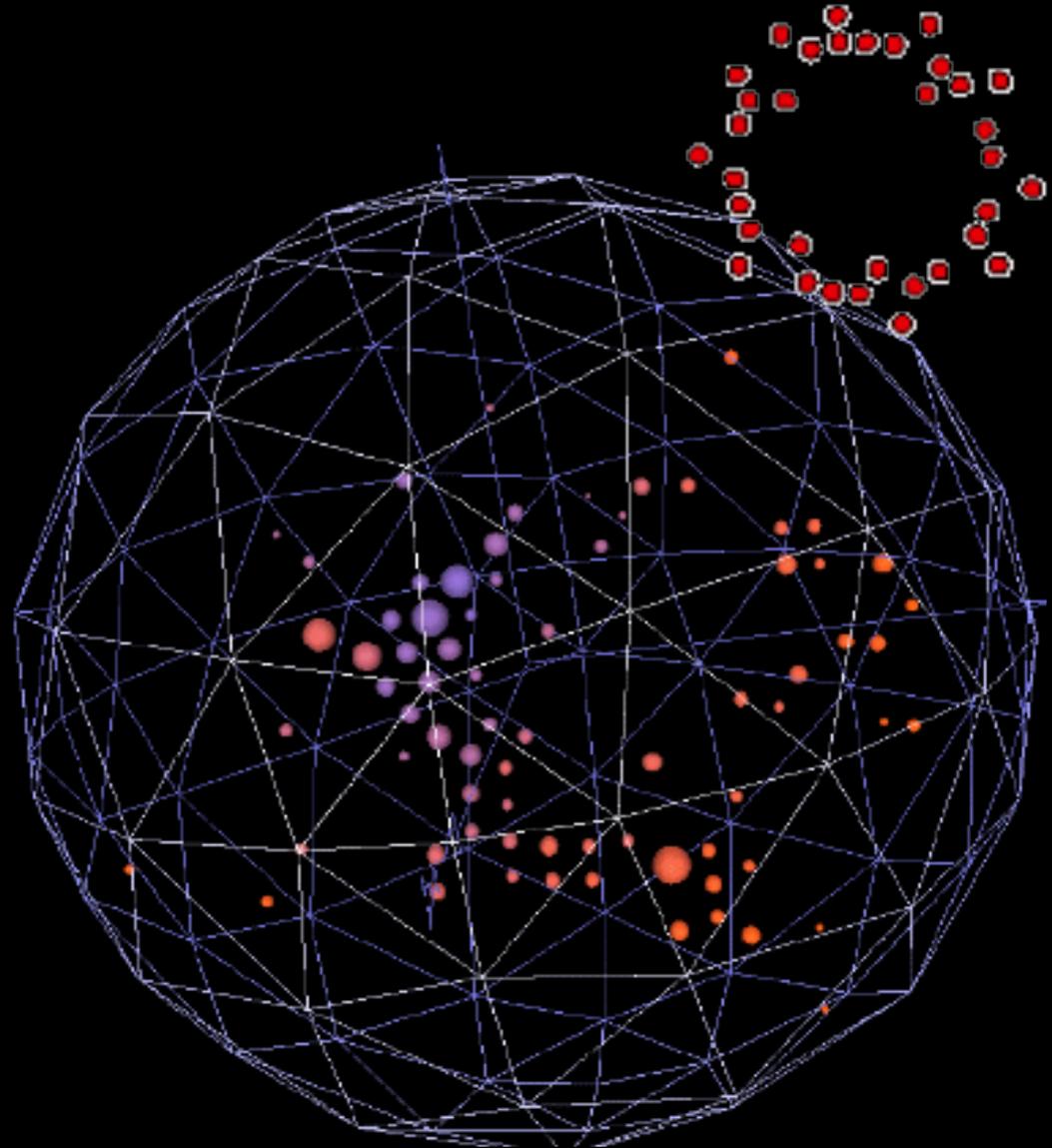
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## 6. MiniBooNE $\nu_e$ appearance candidate data

### Neutrino mode low energy excess

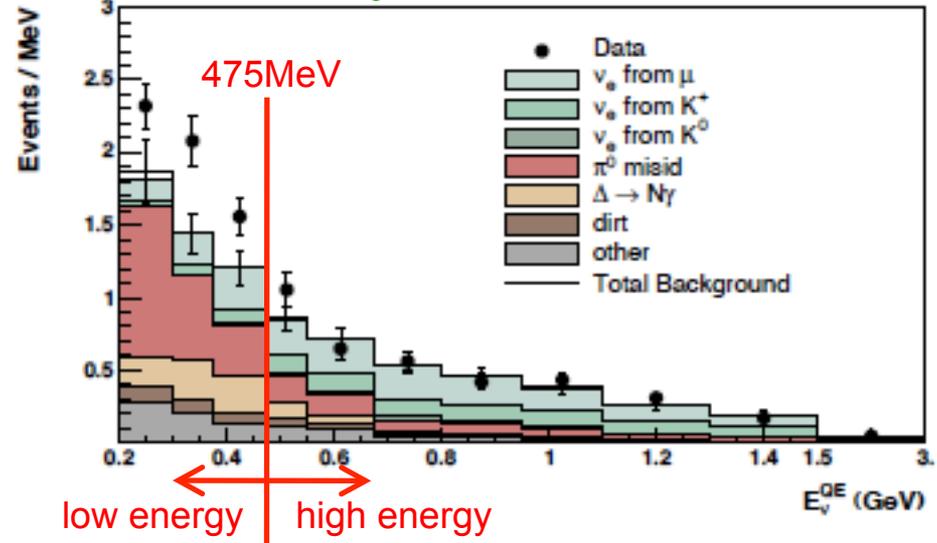
MiniBooNE didn't see the signal at the region where LSND data suggested under the assumption of standard 2 massive neutrino oscillation model, **but MiniBooNE did see the excess where neutrino standard model doesn't predict the signal.**

The energy dependence of MiniBooNE is reproducible by Lorentz violation motivated model, such as Puma model.

->

The low energy excess may have sidereal time dependence.

MiniBooNE low E  $\nu_e$  excess



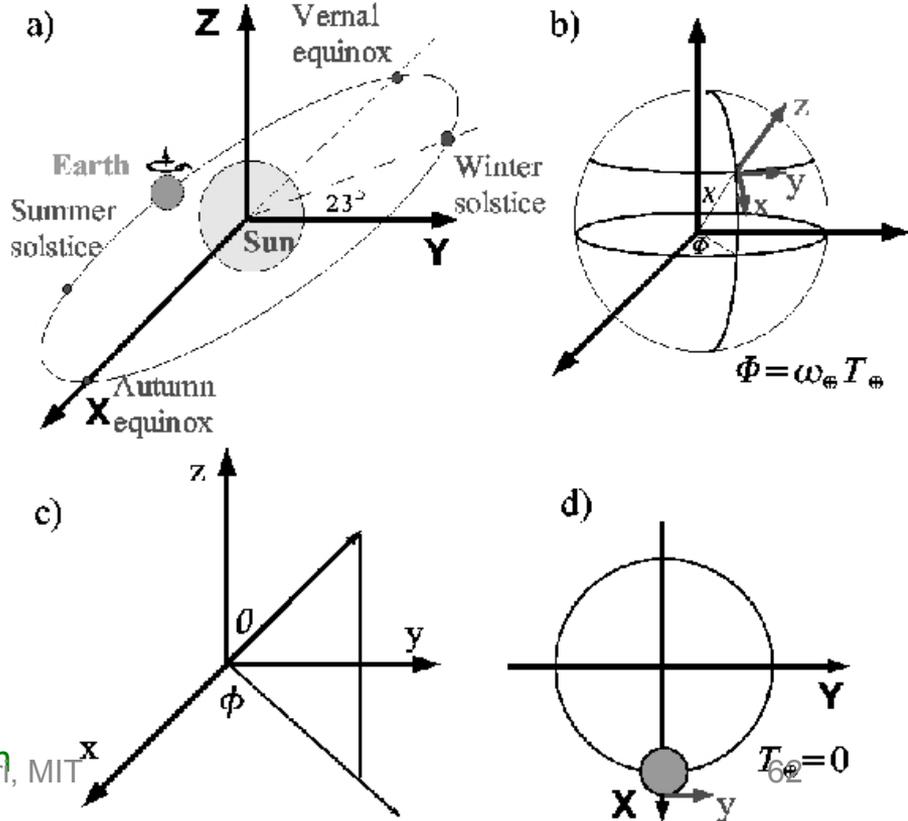
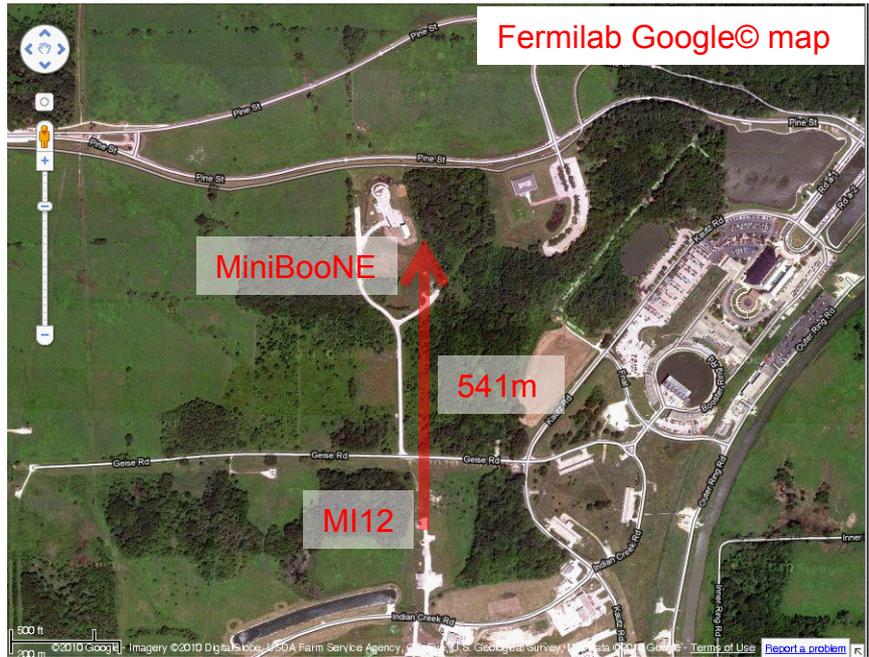
All backgrounds are measured in other data sample and their errors are constrained

# 6. Lorentz violation with MiniBooNE

Test for Lorentz violation in MiniBooNE data;

- (1) fix the coordinate system
- (2) write down Lagrangian including Lorentz violating terms under the formalism
- (3) write down the observables using this Lagrangian

- Booster neutrino beamline is described in Sun-centered coordinates



- a) Sun centred system
- b) Earth centred system
- c) FNAL local coordinate system
- d) definition of the sidereal time

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- Booster neutrino beamline is described in Sun-centered coordinates
- Standard Model Extension (SME)

### Modified Dirac Equation (MDE) of neutrinos

$$i(\Gamma_{AB}^\nu \partial_\nu - M_{AB})\nu_B = 0$$

### SME parameters

$$\Gamma_{AB}^\nu = \gamma^\nu \delta_{AB} + \mathbf{c}_{AB}^{\mu\nu} \gamma_\mu + \mathbf{d}_{AB}^{\mu\nu} \gamma_\mu \gamma_5 + \mathbf{e}_{AB}^\nu + \mathbf{if}_{AB}^\nu \gamma_5 + \frac{1}{2} \mathbf{g}_{AB}^{\lambda\mu\nu} \sigma_{\lambda\mu}$$

$$M_{AB} = m_{AB} + \mathbf{im}_{5AB} \gamma_5 + \mathbf{a}_{AB}^\mu \gamma_\mu + \mathbf{b}_{AB}^\mu \gamma_5 \gamma_\mu + \frac{1}{2} \mathbf{H}_{AB}^{\mu\nu} \sigma_{\mu\nu}$$

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$$M_{AB} = m_{AB} + im_{5AB} \gamma_5 + \boxed{a_{AB}^\mu} \gamma_\mu + \boxed{b_{AB}^\mu} \gamma_5 \gamma_\mu + \frac{1}{2} \boxed{H_{AB}^{\mu\nu}} \sigma_{\mu\nu}$$

CPT odd

CPT even

## 6. Lorentz violation with MiniBooNE

Test for Lorentz violation in MiniBooNE data;

- (1) fix the coordinate system
- (2) write down Lagrangian including Lorentz violating terms under the formalism
- (3) write down the observables using this Lagrangian

- Booster neutrino beamline is described in Sun-centered coordinates
- Standard Model Extension (SME)
- Sidereal time dependent oscillation probability

Lorentz violating oscillation probability for MiniBooNE

$$\begin{aligned}
 P_{\nu_{\mu} \rightarrow \nu_e} &\sim \frac{|(h_{\text{eff}})_{e\mu}|^2 L^2}{(\hbar c)^2} \\
 &= \left( \frac{L}{\hbar c} \right)^2 \left| (C)_{e\mu} + (A_s)_{e\mu} \sin w_{\oplus} T_{\oplus} + (A_c)_{e\mu} \cos w_{\oplus} T_{\oplus} \right. \\
 &\quad \left. + (B_s)_{e\mu} \sin 2w_{\oplus} T_{\oplus} + (B_c)_{e\mu} \cos 2w_{\oplus} T_{\oplus} \right|^2
 \end{aligned}$$

sidereal frequency	$w_{\oplus} = \frac{2\pi}{23\text{h}56\text{m}4.1\text{s}}$
sidereal time	$T_{\oplus}$

Sidereal variation analysis for MiniBooNE is 5 parameter fitting problem

## 6. Lorentz violation with MiniBooNE

Sidereal variation of neutrino oscillation probability for MiniBooNE (5 parameters)

$$P_{\nu_e \rightarrow \nu_\mu} = \left( \frac{L}{\hbar c} \right)^2 \left| (C)_{e\mu} + (A_s)_{e\mu} \sin w_{\oplus \oplus} T + (A_c)_{e\mu} \cos w_{\oplus \oplus} T + (B_s)_{e\mu} \sin 2w_{\oplus \oplus} T + (B_c)_{e\mu} \cos 2w_{\oplus \oplus} T \right|^2$$

Expression of 5 observables (14 SME parameters)

$$\begin{aligned} (C)_{e\mu} &= (\mathbf{a}_L)_{e\mu}^T - N^Z (\mathbf{a}_L)_{e\mu}^Z + E \left[ -\frac{1}{2} (3 - N^Z N^Z) (c_L)_{e\mu}^{TT} + 2N^Z (c_L)_{e\mu}^{TZ} + \frac{1}{2} (1 - 3N^Z N^Z) (c_L)_{e\mu}^{ZZ} \right] \\ (A_s)_{e\mu} &= N^Y (\mathbf{a}_L)_{e\mu}^X - N^X (\mathbf{a}_L)_{e\mu}^Y + E \left[ -2N^Y (c_L)_{e\mu}^{TX} + 2N^X (c_L)_{e\mu}^{TY} + 2N^Y N^Z (c_L)_{e\mu}^{XZ} - 2N^X N^Z (c_L)_{e\mu}^{YZ} \right] \\ (A_c)_{e\mu} &= -N^X (\mathbf{a}_L)_{e\mu}^X - N^Y (\mathbf{a}_L)_{e\mu}^Y + E \left[ 2N^X (c_L)_{e\mu}^{TX} + 2N^Y (c_L)_{e\mu}^{TY} - 2N^X N^Z (c_L)_{e\mu}^{XZ} - 2N^Y N^Z (c_L)_{e\mu}^{YZ} \right] \\ (B_s)_{e\mu} &= E \left[ N^X N^Y \left( (c_L)_{e\mu}^{XX} - (c_L)_{e\mu}^{YY} \right) - (N^X N^X - N^Y N^Y) (c_L)_{e\mu}^{XY} \right] \\ (B_c)_{e\mu} &= E \left[ -\frac{1}{2} (N^X N^X - N^Y N^Y) \left( (c_L)_{e\mu}^{XX} - (c_L)_{e\mu}^{YY} \right) - 2N^X N^Y (c_L)_{e\mu}^{XY} \right] \end{aligned}$$

$$\begin{pmatrix} N^X \\ N^Y \\ N^Z \end{pmatrix} = \begin{pmatrix} \cos \chi \sin \theta \cos \phi - \sin \chi \cos \theta \\ \sin \theta \sin \phi \\ -\sin \chi \sin \theta \cos \phi - \cos \chi \cos \theta \end{pmatrix}$$

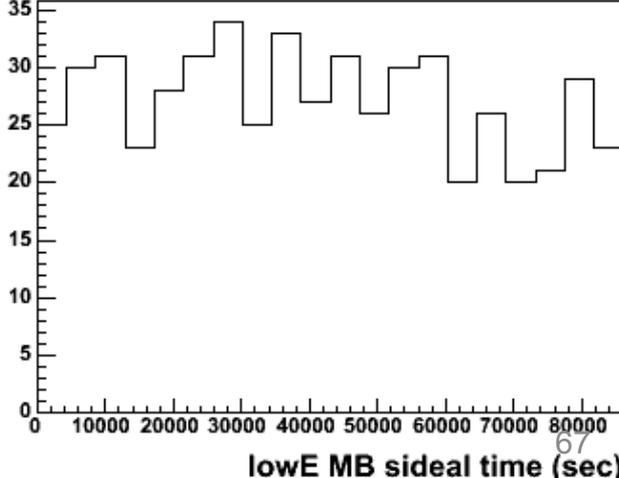
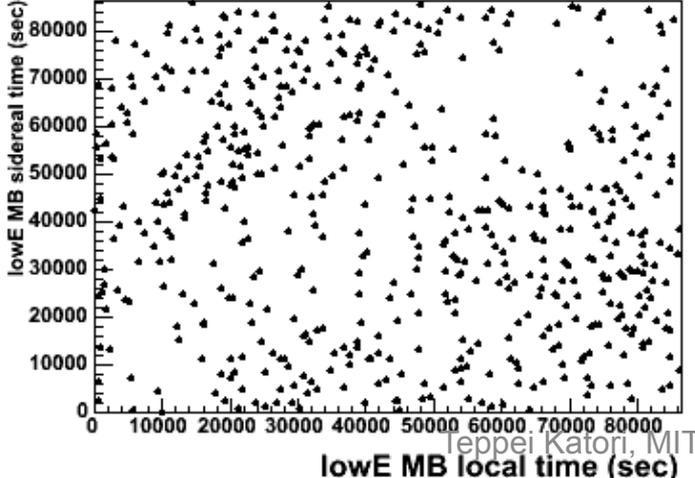
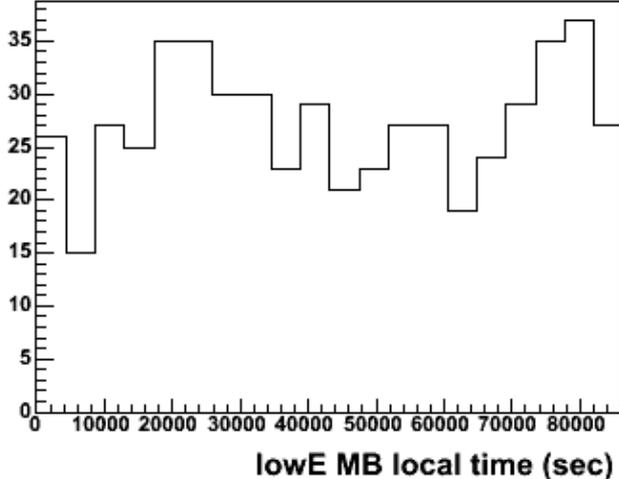
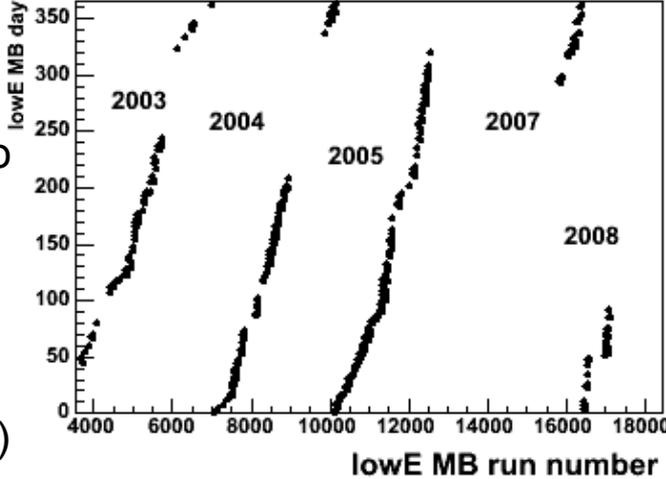
coordinate dependent direction vector  
(depends on the latitude of FNAL, location  
of BNB and MiniBooNE detector)

# 6. Lorentz violation with MiniBooNE neutrino data

## Time distribution of MiniBooNE neutrino mode low energy region

MiniBooNE data taking is reasonably uniform, so all day-night effect is likely to be washed out in sidereal time distribution.

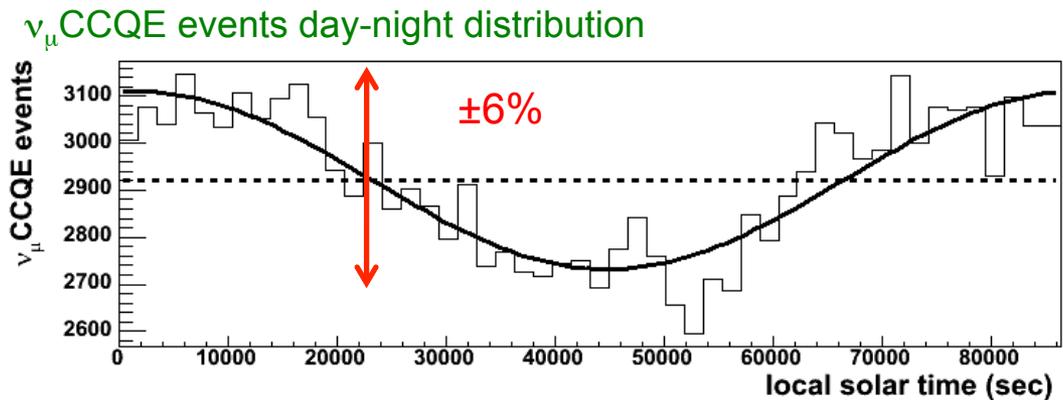
solar local time  
24h00m00s (86400s)  
sidereal time  
23h56m04s (86164s)



# 6. Lorentz violation with MiniBooNE neutrino data

## Time dependent systematics

- Beam and detector day night effect is evaluated from high statistics  $\nu_\mu$  CCQE sample
- $\nu_\mu$  CCQE events show  $\pm 6\%$  day-night variation

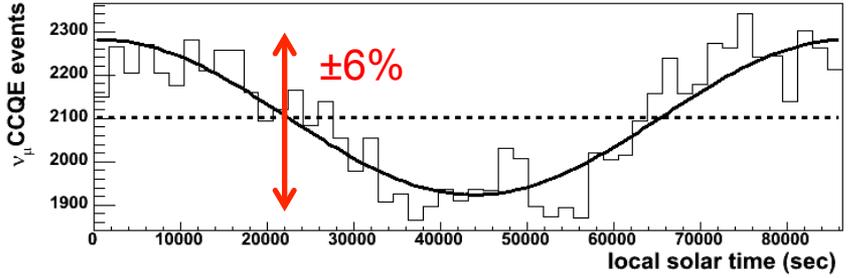


# 6. Lorentz violation with MiniBooNE neutrino data

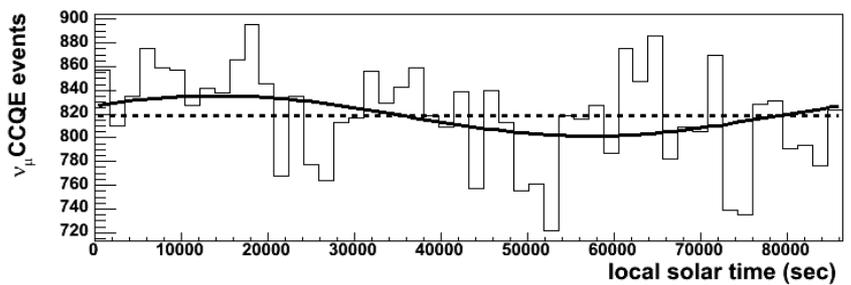
## Time dependent systematics

- Beam and detector day night effect is evaluated from high statistics  $\nu_\mu$  CCQE sample
- $\nu_\mu$  CCQE events show  $\pm 6\%$  day-night variation
- Furthermore, neutrinos know when the weekend is!

$\nu_\mu$  CCQE events distribution, Monday to Friday



$\nu_\mu$  CCQE events distribution, Saturday and Sunday

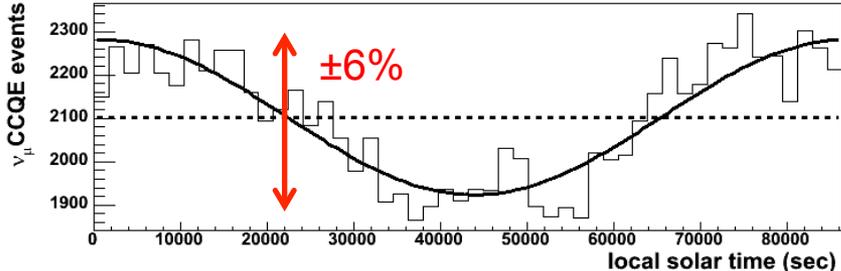


# 6. Lorentz violation with MiniBooNE neutrino data

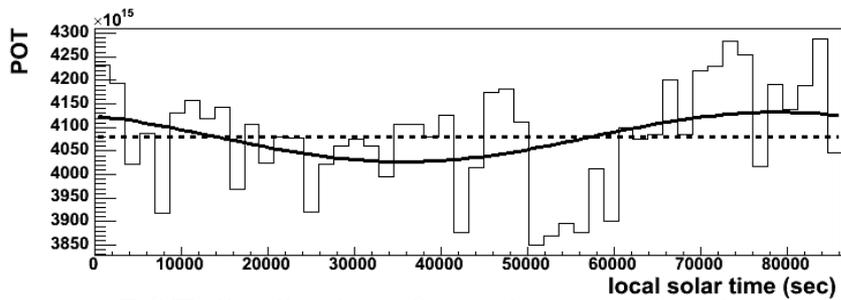
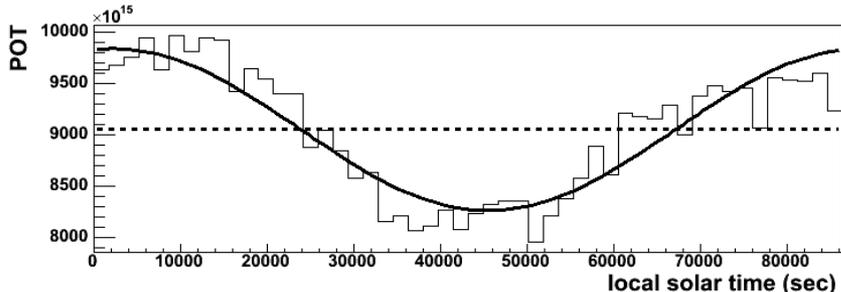
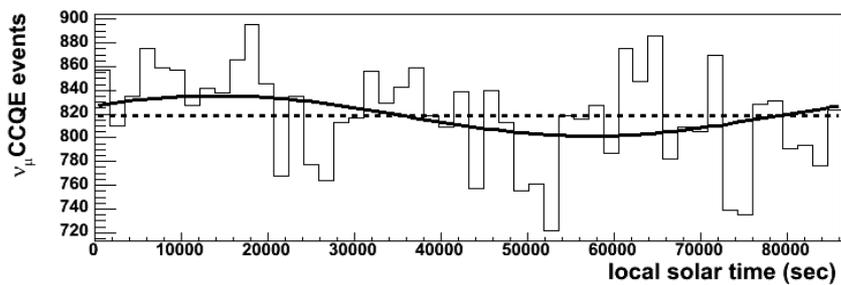
## Time dependent systematics

- Beam and detector day night effect is evaluated from high statistics  $\nu_\mu$  CCQE sample
- $\nu_\mu$  CCQE events show  $\pm 6\%$  day-night variation
- Furthermore, neutrinos know when the weekend is!
- **day-night variation of protons on target (POT)**

$\nu_\mu$  CCQE events distribution, Monday to Friday



$\nu_\mu$  CCQE events distribution, Saturday and Sunday



POT distribution, Monday to Friday

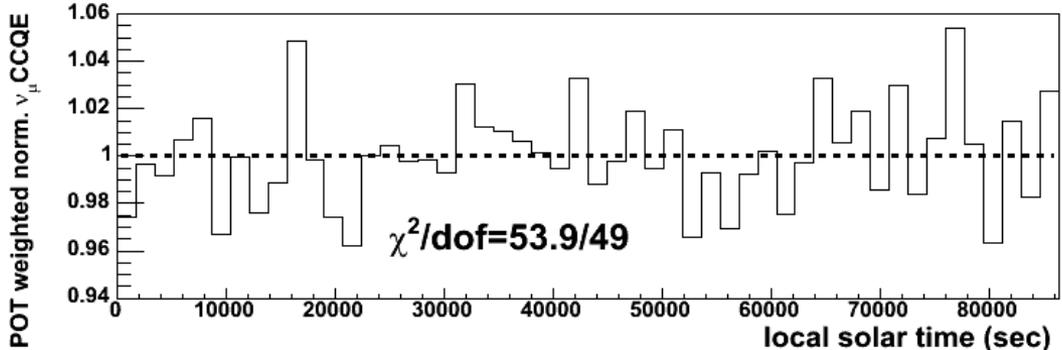
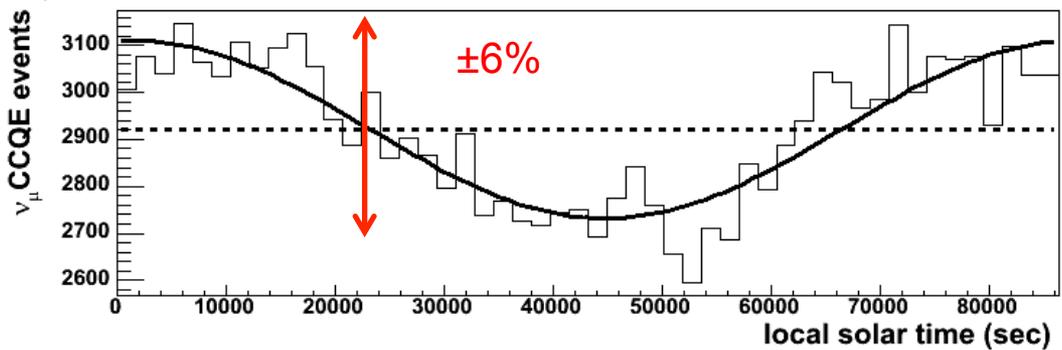
POT distribution, Saturday and Sunday

# 6. Lorentz violation with MiniBooNE neutrino data

## Time dependent systematics

- Beam and detector day night effect is evaluated from high statistics  $\nu_\mu$  CCQE sample
- $\nu_\mu$  CCQE events show  $\pm 6\%$  day-night variation
- Furthermore, neutrinos know when the weekend is!
- day-night variation of protons on target (POT)
- After correcting this,  $\nu_\mu$  CCQE events exhibit flat

$\nu_\mu$  CCQE events day-night distribution



## 6. Lorentz violation with MiniBooNE neutrino data

### Time dependent systematics

- Beam and detector day night effect is evaluated from high statistics  $\nu_\mu$  CCQE sample
- $\nu_\mu$  CCQE events show  $\pm 6\%$  day-night variation
- Furthermore, neutrinos know when the weekend is!
- day-night variation of protons on target (POT)
- After correcting this,  $\nu_\mu$  CCQE events exhibit flat.

An event weight is made to correct this from oscillation candidate sample

- however correct distributions only show negligible changes in  $\chi^2$ 
  - statistical fluctuation of oscillation candidate is bigger than 6% variation
  - day-night effect is washed out in sidereal distribution due to continuous data taking
- event weight for unbinned analysis is tricky

Therefore, we don't use an event weight to correct this in further analysis.

# 6. Lorentz violation with MiniBooNE neutrino data

## Null hypothesis test

The flatness hypothesis is tested by unbinned Kolmogorov-Smirnov test (K-S test).

K-S test has 3 advantages;

1. unbinned, so it has the maximum statistical power
2. no argument with bin choice
3. sensitive with systematic shift of the distribution (e.g., sinusoidal)

None of the tests shows any statistically significant results.

All data sets are compatible with flat hypothesis by K-S test

	low energy		high energy		combined	
	solar	sidereal	solar	sidereal	solar	sidereal
Neutrino mode						
$\langle E_\nu \rangle$	0.36 GeV		0.82 GeV		0.71 GeV	
#evt	544		420		964	
$P(KS)$	0.42	0.13	0.81	0.64	0.64	0.14

# 6. Lorentz violation with MiniBooNE neutrino data

## Unbinned extended maximum likelihood fit

- It has the maximum statistic power
- Assuming excess is Lorentz violation, extract Lorentz violation parameters (SME parameters) from unbinned likelihood fit.

likelihood function

$$\Lambda = \frac{e^{-(\mu_s + \mu_b^v)}}{N!} \prod_{i=1}^N (\mu_s \mathcal{F}_s^i + \mu_b^v \mathcal{F}_b^i) \times \frac{1}{\sqrt{2\pi\sigma_b^2}} \exp\left(-\frac{(\mu_b^v - \mu_b)^2}{2\sigma_b^2}\right) \quad (22)$$

$N$  total number of event

$\mu_s$  predicted signal event number, function of fitting parameters

$\mu_b$  predicted background event number

$\mathcal{F}_s$  probability distribution of signal, function of sidereal time and fitting parameters

$\mathcal{F}_b$  probability distribution of background, not function of sidereal time

$\sigma_b$  the  $1 - \sigma$  error of predicted the background

$\mu_b^v$  floating background event number floating within  $1 - \sigma$

# 6. Lorentz violation with MiniBooNE neutrino data

## Unbinned extended maximum loglikelihood fit

- It has the maximum statistic power
- Assuming excess is Lorentz violation, extract Lorentz violation parameters (SME parameters) from unbinned likelihood fit.
- technically, we add loglikelihood of each event to calculate loglikelihood value of each grid point in a parameter space (grid search). The maximum loglikelihood point is the best fit point, and grid of loglikelihood define 1- $\sigma$  and 2- $\sigma$  contour (degree of freedom is chosen from fake data)
- due to high correlation of parameters, 5 parameter fit cannot provide contours, so we focus on 3 parameter fit

## loglikelihood function for an event

$$\ell_i = -\frac{1}{N}(\mu_s + \mu_b^v) + \ln[\mu_s \mathcal{F}_s^i + \mu_b^v \mathcal{F}_b^i] - \frac{1}{2N} \left( \frac{\mu_b^v - \mu_b}{\sigma} \right)^2$$

## Sidereal variation of neutrino oscillation probability for MiniBooNE

$$P_{\nu_e \rightarrow \nu_\mu} = \left( \frac{L}{\hbar c} \right)^2 \left| (C)_{e\mu} + (A_s)_{e\mu} \sin w_\oplus T_\oplus + (A_c)_{e\mu} \cos w_\oplus T_\oplus \right|^2$$

sidereal frequency  $w_\oplus = \frac{2\pi}{23\text{h}56\text{m}4.1\text{s}}$

sidereal time  $T_\oplus$

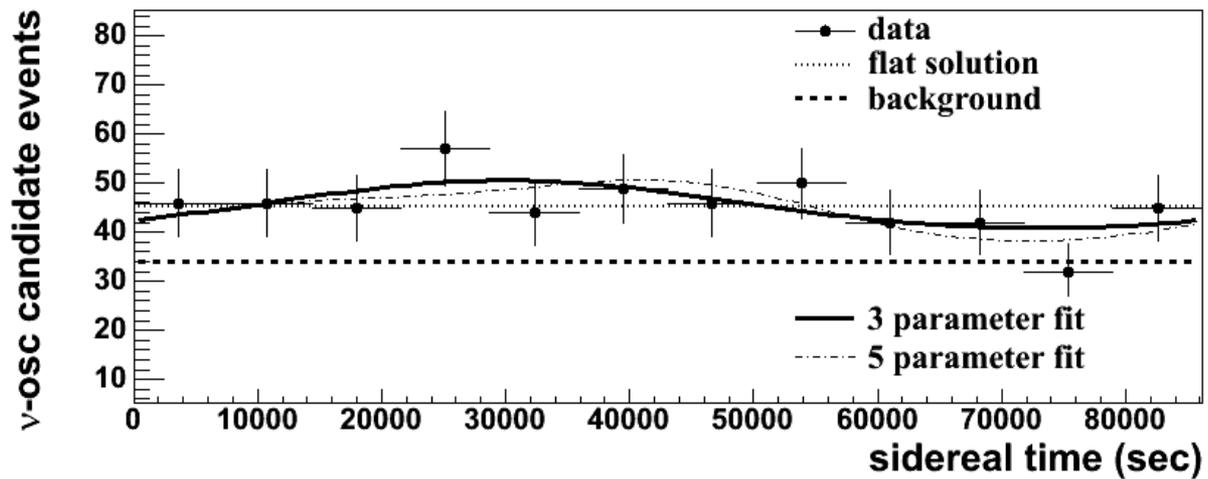
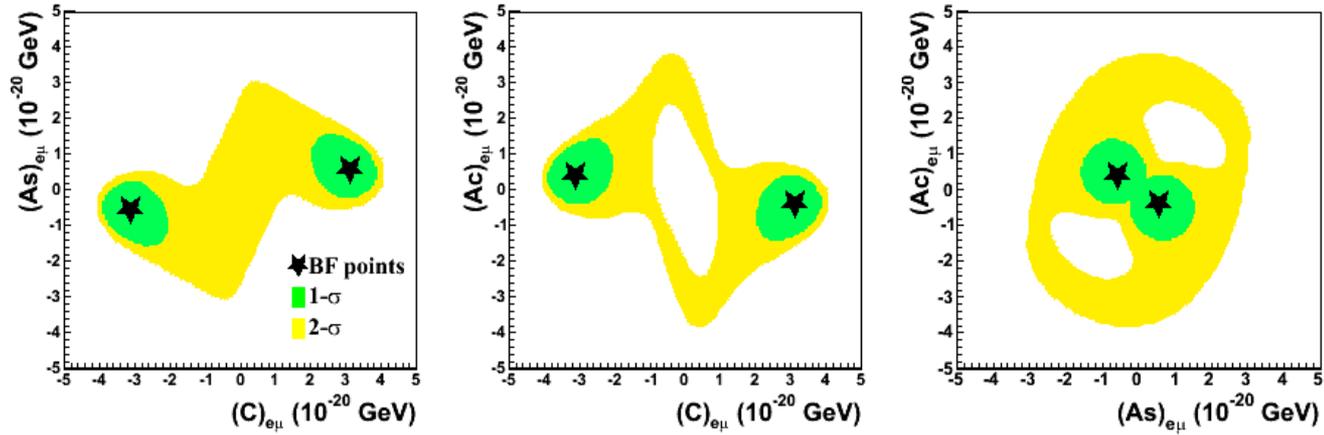
# 6. Lorentz violation with MiniBooNE neutrino data

## Neutrino mode result, low energy region

Only C-parameter is nonzero, but this is sidereal independent parameter.

26.9% of fake data based on null hypothesis have bigger  $\Delta\chi^2$  than data.

The neutrino mode low energy excess is consistent with no sidereal variation.



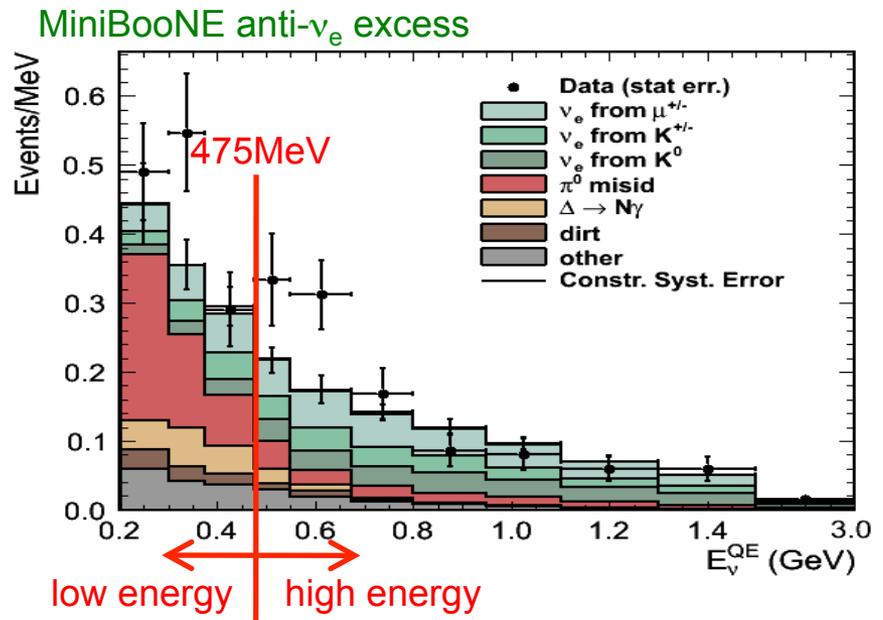
1. Spontaneous Lorentz symmetry breaking
2. What is Lorentz and CPT violation?
3. Modern tests of Lorentz and CPT violation
4. Lorentz violation with neutrino oscillation
5. MiniBooNE experiment
6. Lorentz violation with MiniBooNE neutrino data
- 7. Lorentz violation with MiniBooNE anti-neutrino data**
8. Conclusion

## 7. MiniBooNE anti- $\nu_e$ appearance candidate data

### Antineutrino mode excess

MiniBooNE did see the signal at the region where LSND data suggested under the assumption of standard two massive neutrino oscillation model

If the excess were Lorentz violation, the excess may have sidereal time dependence.



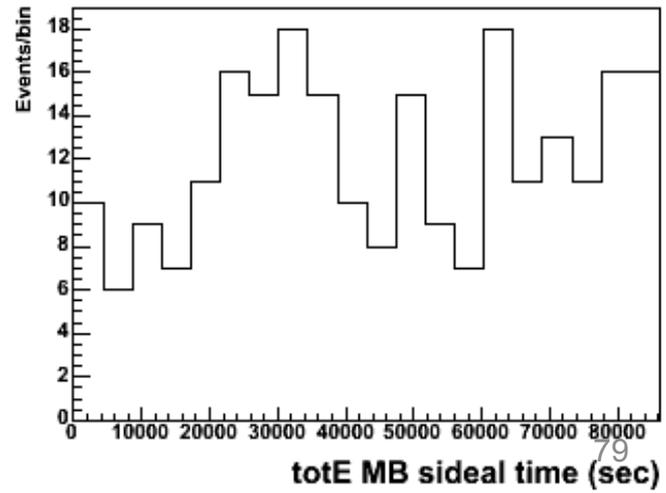
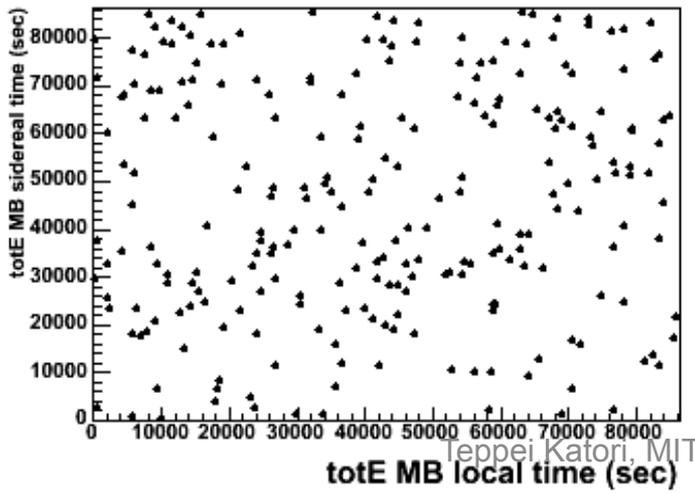
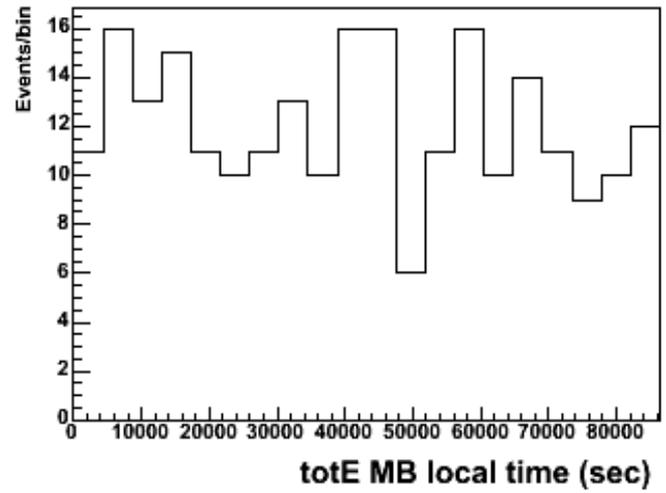
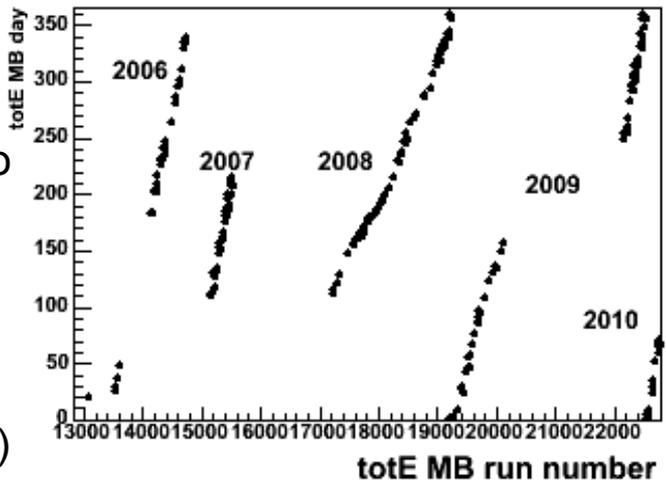
All backgrounds are measured in other data sample and their errors are constrained

# 7. Lorentz violation with MiniBooNE anti-neutrino data

## Time distribution of MiniBooNE antineutrino mode oscillation region

MiniBooNE data taking is reasonably uniform, so all day-night effect is likely to be washed out in sidereal time distribution.

solar local time  
24h00m00s (86400s)  
sidereal time  
23h56m04s (86164s)



# 7. Lorentz violation with MiniBooNE anti-neutrino data

## Null hypothesis test

The flatness hypothesis is tested by unbinned Kolmogorov-Smirnov test (K-S test).

K-S test has 3 advantages;

1. unbinned, so it has the maximum statistical power
2. no argument with bin choice
3. sensitive with systematic shift of the distribution (e.g., sinusoidal)

None of tests shows any statistically significant results.

All data sets are compatible with flat hypothesis.

	low energy		high energy		combined	
	solar	sidereal	solar	sidereal	solar	sidereal
Neutrino mode						
$\langle E_\nu \rangle$	0.36 GeV		0.82 GeV		0.71 GeV	
#evt	544		420		964	
$P(KS)$	0.42	0.13	0.81	0.64	0.64	0.14
Anti-neutrino mode						
$\langle E_{\bar{\nu}} \rangle$	0.34 GeV		0.78 GeV		0.60 GeV	
#evt	119		122		241	
$P(KS)$	0.62	0.15	0.79	0.39	0.69	0.08

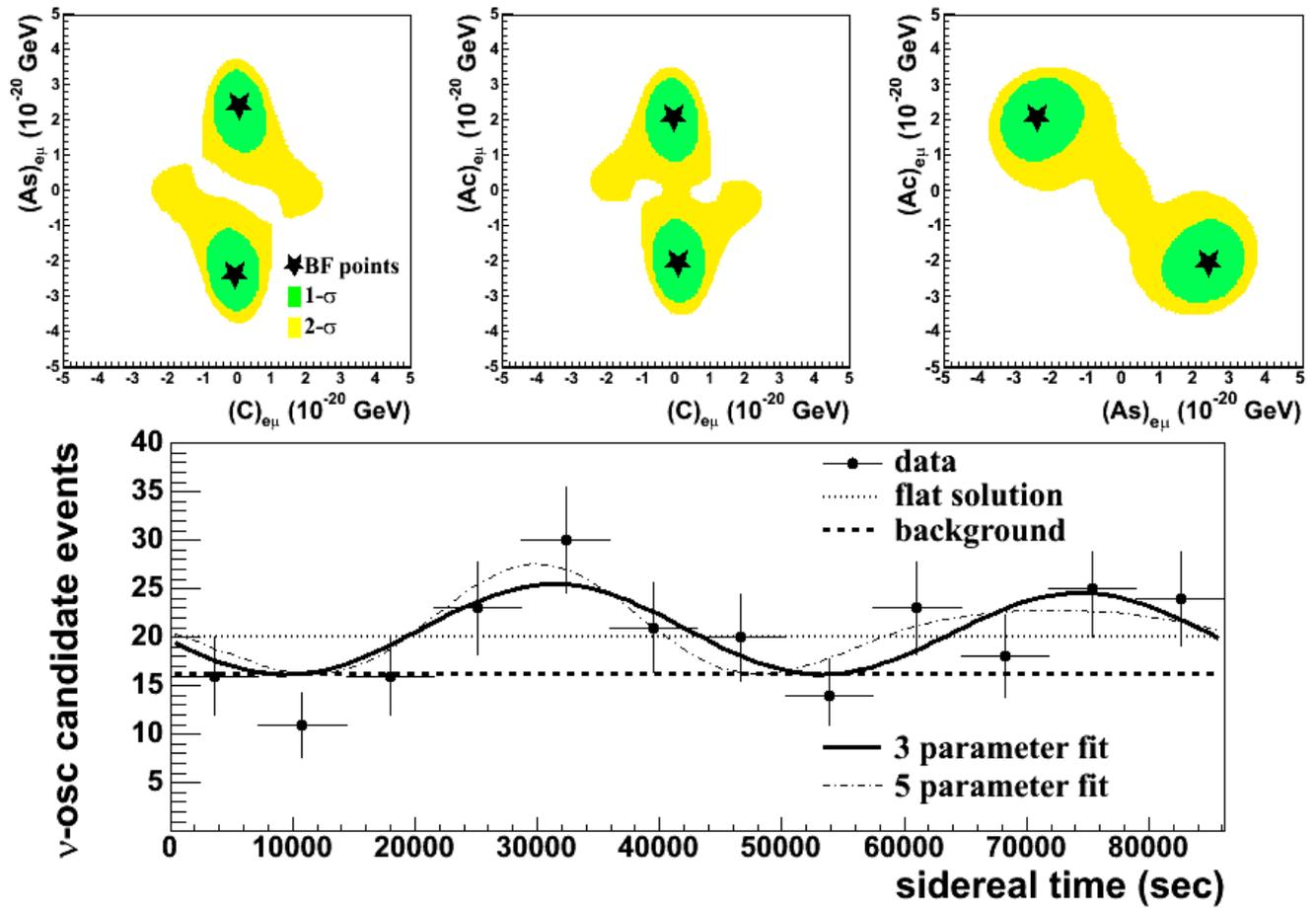
# 7. Lorentz violation with MiniBooNE anti-neutrino data

## Anti-neutrino mode result, combined energy region

As and Ac-parameters are nonzero, which are sidereal dependent parameters.

3.0% of fake data based on null hypothesis have bigger  $\Delta\chi^2$  than data.

The anti-neutrino mode combined energy region excess prefer sidereal time dependent solution, but not statistically significant level.



1. Spontaneous Lorentz symmetry breaking
2. What is Lorentz and CPT violation?
3. Modern tests of Lorentz and CPT violation
4. Lorentz violation with neutrino oscillation
5. MiniBooNE experiment
6. Lorentz violation with MiniBooNE neutrino data
7. Lorentz violation with MiniBooNE anti-neutrino data
- 8. Conclusion**

# 8. Summary of results

## Neutrino result summary

- Neutrino mode data is consistent with null hypothesis by K-S test.
- The low energy excess data fit prefer sidereal time independent solution.
- 26.9% of fake data based on null hypothesis have bigger  $\Delta\chi^2$  than data.

## Anti-neutrino result summary

- Anti-neutrino mode data is consistent with null hypothesis by K-S test.
- The fit for combined region excess data prefers sidereal time dependent solution.
- 3.0% of fake data based on null hypothesis have bigger  $\Delta\chi^2$  than data.

## SME coefficients

	$\nu$ -mode BF	$2\sigma$ limit	$\bar{\nu}$ -mode BF	$2\sigma$ limit	SME coefficients combination (unit $10^{-20}$ GeV)
$ (C)_{e\mu} $	$3.1 \pm 0.6 \pm 0.9$	$< 4.2$	$0.1 \pm 0.8 \pm 0.1$	$< 2.6$	$\pm[(a_L)_{e\mu}^T + 0.75(a_L)_{e\mu}^Z] - \langle E \rangle [1.22(c_L)_{e\mu}^{TT} + 1.50(c_L)_{e\mu}^{TZ} + 0.34(c_L)_{e\mu}^{ZZ}]$
$ (A_s)_{e\mu} $	$0.6 \pm 0.9 \pm 0.3$	$< 3.3$	$2.4 \pm 1.3 \pm 0.5$	$< 3.9$	$\pm[0.66(a_L)_{e\mu}^Y] - \langle E \rangle [1.33(c_L)_{e\mu}^{TY} + 0.99(c_L)_{e\mu}^{YZ}]$
$ (A_c)_{e\mu} $	$0.4 \pm 0.9 \pm 0.4$	$< 4.0$	$2.1 \pm 1.2 \pm 0.4$	$< 3.7$	$\pm[0.66(a_L)_{e\mu}^X] - \langle E \rangle [1.33(c_L)_{e\mu}^{TX} + 0.99(c_L)_{e\mu}^{XZ}]$

# 8. Summary of results

## SME coefficients sensitivity

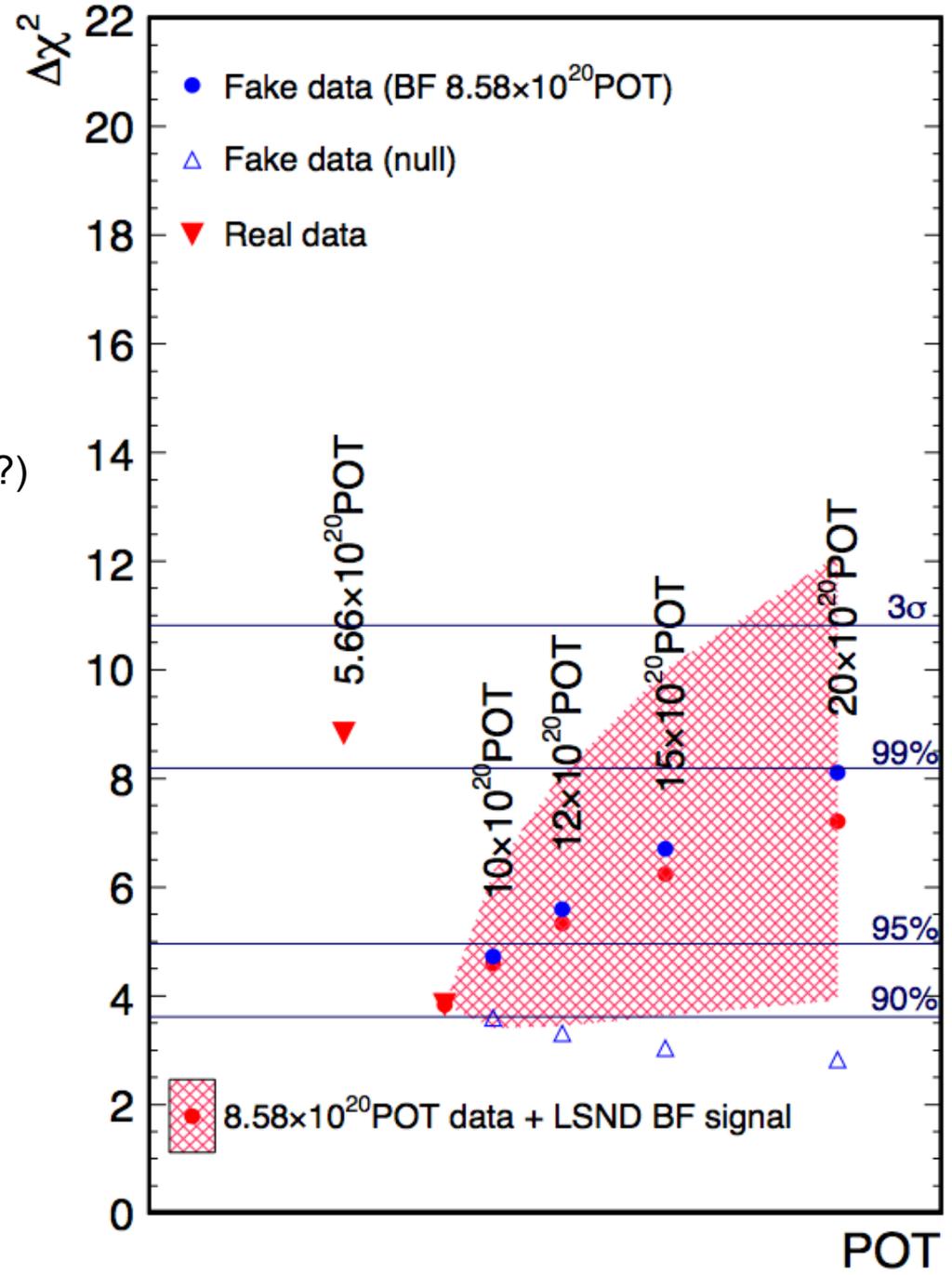
- The sensitivities are obtained by setting on one coefficient nonzero
- These result conflict with LSND (LSND signal needs  $\sim 10^{-19}$  GeV Lorentz violation), and simple Lorentz violation models leave tension between MiniBooNE and LSND
- First time constrained time independent SME coefficients for e- $\mu$  sector.

Coefficient	$e\mu$ ( $\nu$ mode low energy region)	$e\mu$ ( $\bar{\nu}$ mode combined region)
→ $\text{Re}(a_L)^T$ or $\text{Im}(a_L)^T$	$4.2 \times 10^{-20}$ GeV	$2.6 \times 10^{-20}$ GeV
$\text{Re}(a_L)^X$ or $\text{Im}(a_L)^X$	$6.0 \times 10^{-20}$ GeV	$5.6 \times 10^{-20}$ GeV
$\text{Re}(a_L)^Y$ or $\text{Im}(a_L)^Y$	$5.0 \times 10^{-20}$ GeV	$5.9 \times 10^{-20}$ GeV
→ $\text{Re}(a_L)^Z$ or $\text{Im}(a_L)^Z$	$5.6 \times 10^{-20}$ GeV	$3.5 \times 10^{-20}$ GeV
$\text{Re}(c_L)^{XY}$ or $\text{Im}(c_L)^{XY}$	—	—
$\text{Re}(c_L)^{XZ}$ or $\text{Im}(c_L)^{XZ}$	$1.1 \times 10^{-19}$	$6.2 \times 10^{-20}$
$\text{Re}(c_L)^{YZ}$ or $\text{Im}(c_L)^{YZ}$	$9.2 \times 10^{-20}$	$6.5 \times 10^{-20}$
$\text{Re}(c_L)^{XX}$ or $\text{Im}(c_L)^{XX}$	—	—
$\text{Re}(c_L)^{YY}$ or $\text{Im}(c_L)^{YY}$	—	—
→ $\text{Re}(c_L)^{ZZ}$ or $\text{Im}(c_L)^{ZZ}$	$3.4 \times 10^{-19}$	$1.3 \times 10^{-19}$
→ $\text{Re}(c_L)^{TT}$ or $\text{Im}(c_L)^{TT}$	$9.6 \times 10^{-20}$	$3.6 \times 10^{-20}$
$\text{Re}(c_L)^{TX}$ or $\text{Im}(c_L)^{TX}$	$8.4 \times 10^{-20}$	$4.6 \times 10^{-20}$
$\text{Re}(c_L)^{TY}$ or $\text{Im}(c_L)^{TY}$	$6.9 \times 10^{-20}$	$4.9 \times 10^{-20}$
→ $\text{Re}(c_L)^{TZ}$ or $\text{Im}(c_L)^{TZ}$	$7.8 \times 10^{-20}$	$2.9 \times 10^{-20}$

# 8. MiniBooNE future plan

This analysis is statistically limited.

We continue to take data until March (May?) 2012, then we will double the statistics.

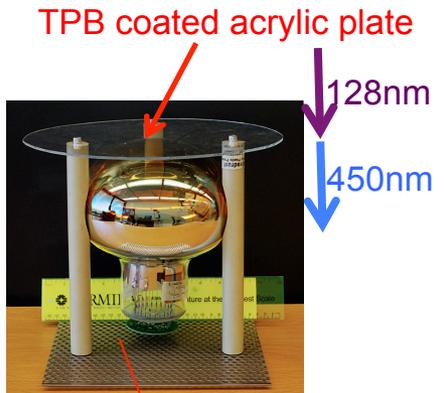
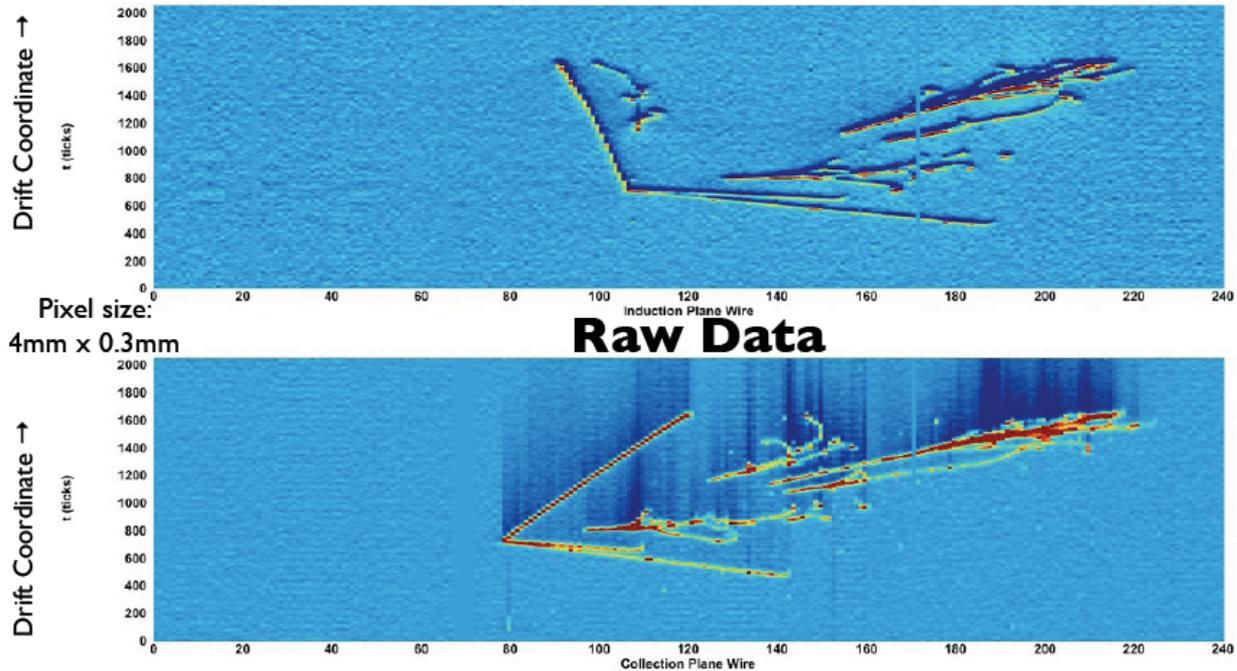


# 8. MicroBooNE

## Liquid Argon Time Projection Chamber (LArTPC) neutrino experiment at Fermilab

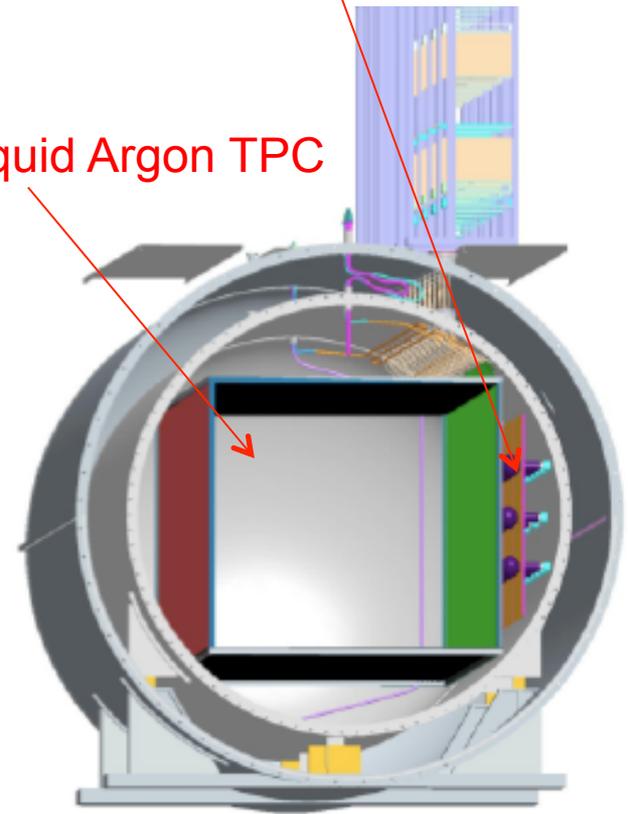
- 150 ton volume of cryostat
- R&D detector for future large LArTPC
- 3D tracker (modern bubble chamber)
- data taking will start from 2014 (passed CD2)
- dE/dx can separate single electron from gamma ray

2  $\pi^0$ s decayed to 4 gammas, then converted to 4  $e^+e^-$  pairs (ArgoNeuT experiment)



PMT system

liquid Argon TPC



# MiniBooNE collaboration

University of Alabama  
Bucknell University  
University of Cincinnati  
University of Colorado  
Columbia University  
Embry Riddle Aeronautical University  
Fermi National Accelerator Laboratory  
Indiana University  
University of Florida

Los Alamos National Laboratory  
Louisiana State University  
Massachusetts Institute of Technology  
University of Michigan  
Princeton University  
Saint Mary's University of Minnesota  
Virginia Polytechnic Institute  
Yale University



**Thank you for your attention!**

# Backup

# 1. Spontaneous Lorentz symmetry breaking

## FAQ

Q. How can Lorentz violation happen?

A. Lorentz violation has been shown to occur in Planck scale physics, especially, by **Spontaneous Symmetry Breaking**.

Q. What is the expected scale of Lorentz violation?

A. Since it is Planck scale physics, either  $>10^{19}\text{GeV}$  or  $<10^{-19}\text{GeV}$  is the interesting region.  $>10^{19}\text{GeV}$  is not achievable (LHC is  $10^4\text{GeV}$ ), but  $<10^{-19}\text{GeV}$  is possible.

ex1) Zeeman frequency change of double gas maser  $\sim 100\text{nHz} \sim 10^{-32}\text{GeV}$

ex2) measured atmospheric neutrino eigenvalue difference  $\sim \Delta m^2/E \sim 10^{-23}\text{GeV}$

## 2. What is Lorentz violation?

### FAQ

#### Q. What is Lorentz violation?

A. Lorentz violation is the violation of the **particle** Lorentz transformation, either Lorentz boost or rotation, and the **observer** Lorentz transformation is unbroken.

all observers agree with the **particle** Lorentz transformation violation phenomena through **observer** Lorentz transformation.

#### Comment - Modified dispersion relation

$$E^2 = m^2 + p^2 + f_i^{(1)} p^i + f_{ij}^{(2)} p^i p^j + \dots$$

The models usually assume isotropy (rotation invariance)

$$E^2 = m^2 + p^2 + f^{(1)} |p| + f^{(2)} |p|^2 + \dots$$

One can make such model in CMB frame.

However since we are not in CMB frame, physics in laboratory frame needs to be related by observer Lorentz transformation from CMB frame, so lab frame is always anisotropy.

## 2. Comment: Is there preferred frame?

As we see, all observers are related with observer's Lorentz transformation, so there is no special "preferred" frame (all observer's are consistent)

But there is a frame where universe looks isotropic even with a Lorentz violating vector field. You may call that is the "preferred frame", and people often speculate the frame where CMB looks isotropic is such a frame (called "CMB frame").

However, we are not on CMB frame (e.g., dipole term of WMAP is nonzero), so we can expect anisotropy by lab experiments even CMB frame is the preferred frame.

## 2. What is CPT violation?

### FAQ

Q. What is CPT theorem?

A. CPT theorem guarantees all terms in the Lagrangian are CPT-even.  
Greenberg, hep-ph/0309309 "Why is CPT fundamental?"

Q. What is CPT violation?

A. CPT violation can happen when Lagrangian has CPT-odd term. The particle mass and the antiparticle mass don't need to be different.

Q. What is the relationship of Lorentz violation and CPT violation?

A. There are 2 types of Lorentz violation,

CPT-odd Lorentz violating term (odd number Lorentz indices)

CPT-even Lorentz violating term (even number Lorentz indices)

CPT-odd term violates CPT, but CPT-even term keeps CPT symmetry. In fact, any effective CPT violation cause Lorentz violation for Feynman propagator, hence interactive quantum field theory. That is why, this is called **Lorentz and CPT violation**.

# 3. Standard Model Extension (SME)

## FAQ

Q. How to detect Lorentz violation?

A.

(1) choose the coordinate system to compare the experimental result

->

Sun centered celestial equatorial coordinate system

(2) write down Lagrangian including Lorentz violating terms under the formalism

->

SME

(3) write down the observables using this Lagrangian

Q. Do you take account the galactic motion?

A. No, the galactic motion is the fastest, but it takes ~1000 years to rotate 1 degree.

We are interested in the test of Lorentz symmetry, so translation motion is not important.

Rotation of the earth is important to test rotation symmetry, and revolution of the earth is important to test Lorentz boost.

## 5. Lorentz violation with neutrino oscillation

### FAQ

Q.why neutrino oscillation is interesting for the test of Lorentz violation ?

A. Lorentz violation is not well-tested with neutrinos. Since neutrinos only feel weak force, they can avoid all constraints come from QED, and offers new possibilities to test Lorentz violation.

Q. Is neutrino oscillation sensitive enough to Lorentz violation?

A. The measured scale of neutrino eigenvalue difference is comparable size with high precision optical test,  $\Delta m^2/E < 10^{-19} \text{GeV}$ .

Very exciting LSND and MiniBooNE data give enough motivation to test Lorentz violation in neutrino physics, because Lorentz violation is the interesting candidate solution for the neutrino oscillation (see next).

# 4. Modern tests of Lorentz violation

## Neutron/proton sector

Direct CPT test

Photon sector

Electron sector

Gravity sector

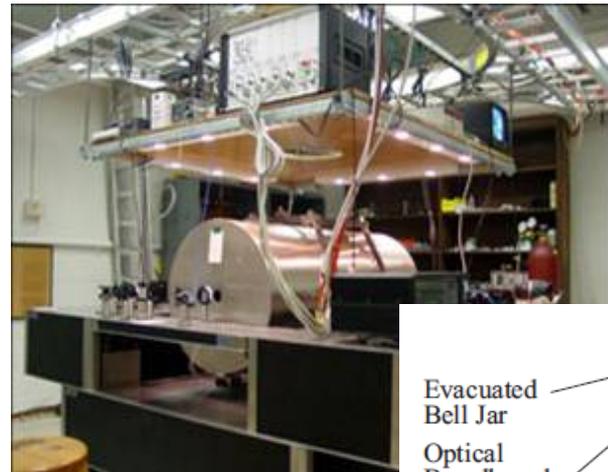
Astrophysics

Particle accelerator

Meson sector

Neutrino sector

co-magnetometer



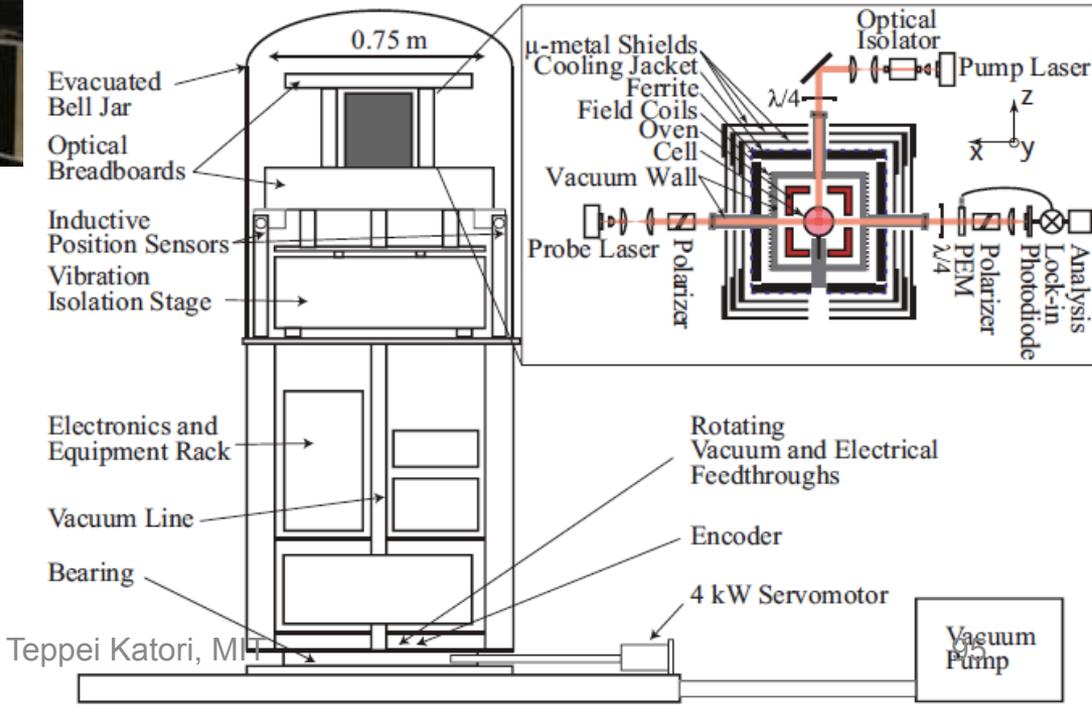
Mike Romalis (Princeton)

Ron Walsworth (Harvard-Smithsonian)



Double gas maser  
 $b_n(\text{rotation}) < 10^{-33} \text{ GeV}$   
 $b_n(\text{boost}) < 10^{-27} \text{ GeV}$

Walsworth et al. PRL93(2004)230801  
 Romalis et al. PRL105(2010)151604



# 4. Modern tests of Lorentz violation

Neutron/proton sector

Max Fujiwara (TRIUMF)

ALPHA experiment

Gerry Gabrielse (Harvard)

Alan Kostelecký (Indiana)

**Direct CPT test**

Photon sector

Electron sector

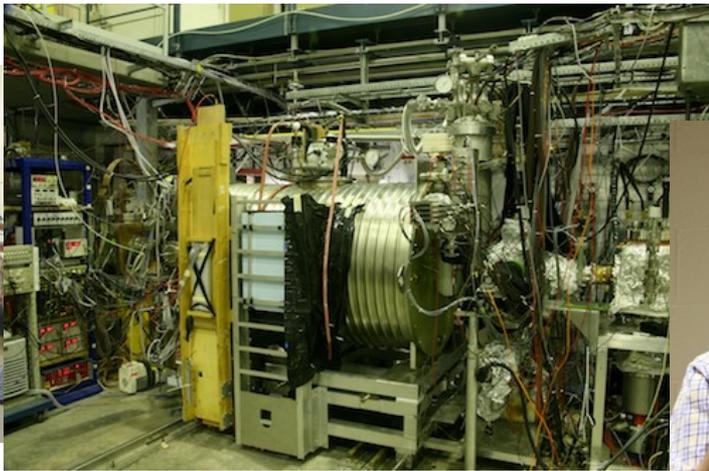
Gravity sector

Astrophysics

Particle accelerator

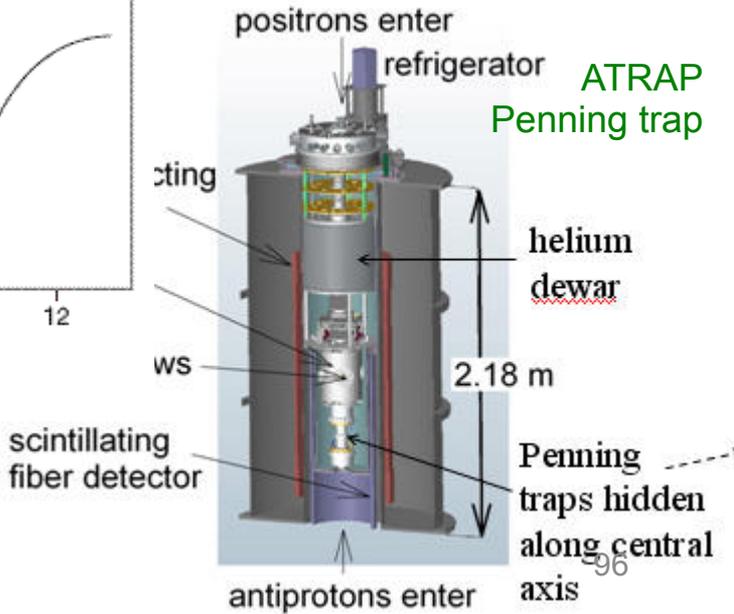
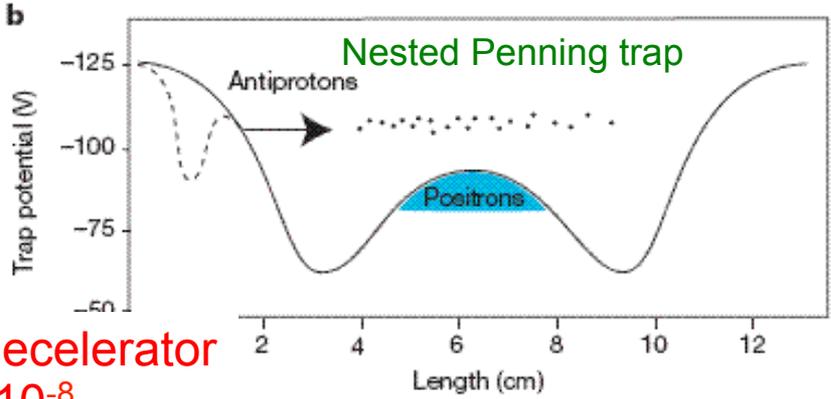
Meson sector

Neutrino sector



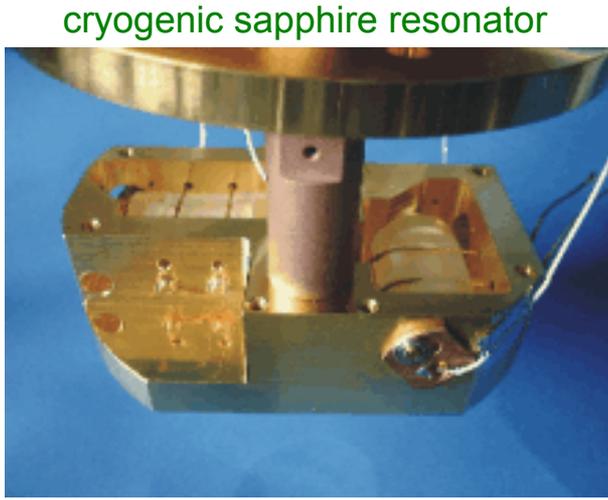
**CERN Antiproton Decelerator**  
 $(M_p - \bar{M}_p) / M_p < 10^{-8}$

ATHENA collaboration  
 Nature 419(2002)456



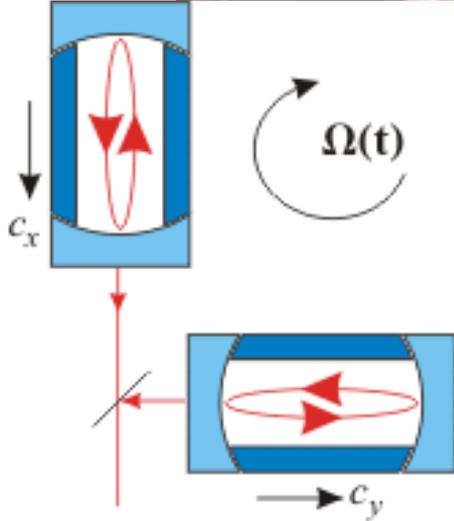
# 4. Modern tests of Lorentz violation

- Neutron/proton sector
- Direct CPT test
- Photon sector**
- Electron sector
- Gravity sector
- Astrophysics
- Particle accelerator
- Meson sector
- Neutrino sector



Cryogenic optical resonator  
 $\Delta c/c < 10^{-16}$   
 ( $\Delta c/c < 10^{-9}$  for M-M expt.)

Peters et al.  
 PRL99(2007)050401



**comparison**

# 4. Modern tests of Lorentz violation

Neutron/proton sector

Direct CPT test

Photon sector

**Electron sector**

Gravity sector

Astrophysics

Particle accelerator

Meson sector

Neutrino sector



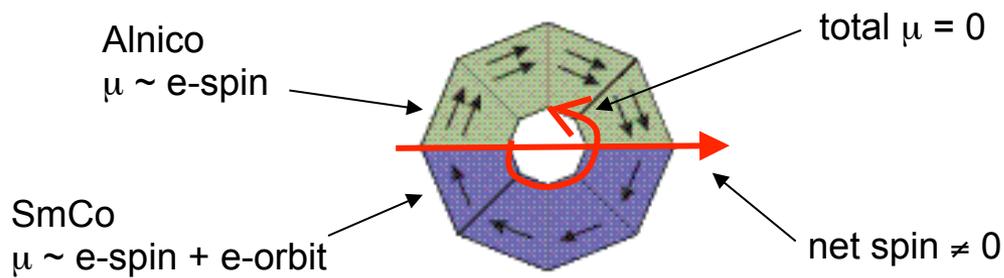
spin-pendulum



Blayne Heckel  
(Washington)

**Spin pendulum**  
 $b_e < 10^{-30}$  GeV

Heckel et al.  
PRL97(2006)021603



# 4. Modern tests of Lorentz violation

Neutron/proton sector  
IM Pegasi

Direct CPT test

Photon sector

Electron sector

Gravity sector

Astrophysics

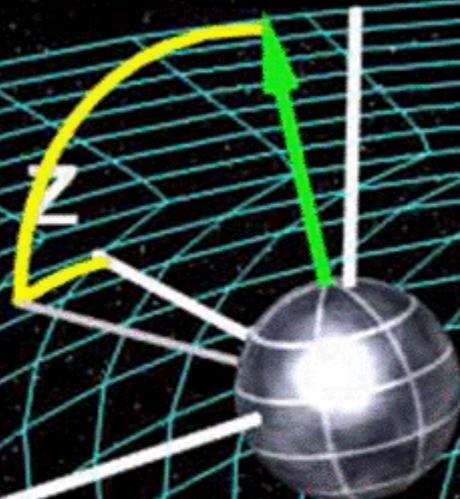
Particle accelerator

Meson sector

Neutrino sector

Geodetic effect  
6.6 arcsec/yr **X**

Frame dragging  
0.041 arcsec/yr

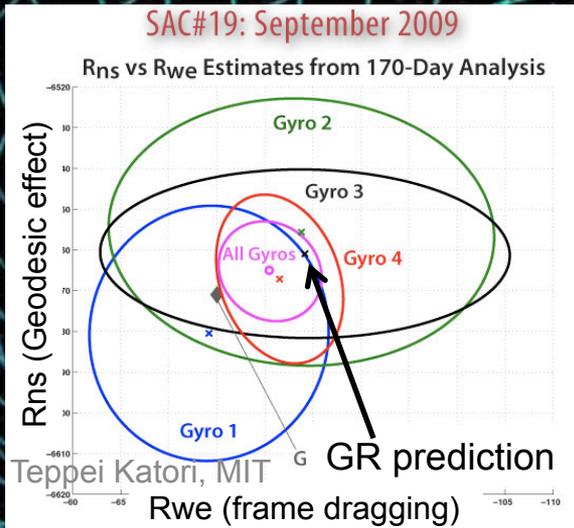


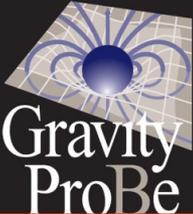
Anomalous precession  
Lunar laser ranging  
Torsion pendulum  
Free fall experiment

...

Bailey and Kostelecký  
PRD74(2006)045001

11/11 Kostelecký and Tasson  
PRL102(2009)010402





Mauro Cambiaso (UNAM)

Luis Urrutia (UNAM)

Ilya Shapiro (UFJF)

Axial vector type Lorentz violation is a source of torsion

explicit Lorentz violation conflicts with Riemann geometry (spontaneous LV is favored)

Propagating torsion is strongly restricted, but background torsion is possible...

Don't forget Cern-Simons term, which is Lorentz violating, too (and also source of torsion)

Time dependence of fine structure constant violates Lorentz invariant, too

Brett Altschul (South Carolina)

Neutrinos are the most promising particles to discover Lorentz violation

Photon may be a Nambu-Goldstone boson from spontaneous Lorentz symmetry breaking!

Numeral theoretical discussions on - top down models of LV - new type of LVs and their tests - theoretical backbones (stability, causality, renormalizability, etc)

# 4. Modern tests of Lorentz violation

Neutron/proton sector

Direct CPT test

Photon sector

Electron sector

Theorist conversations

Astrophysics

Particle accelerator

Meson sector

Neutrino sector

Dan Colladay (New College of FI)

Alan Kostelecký (Indiana)

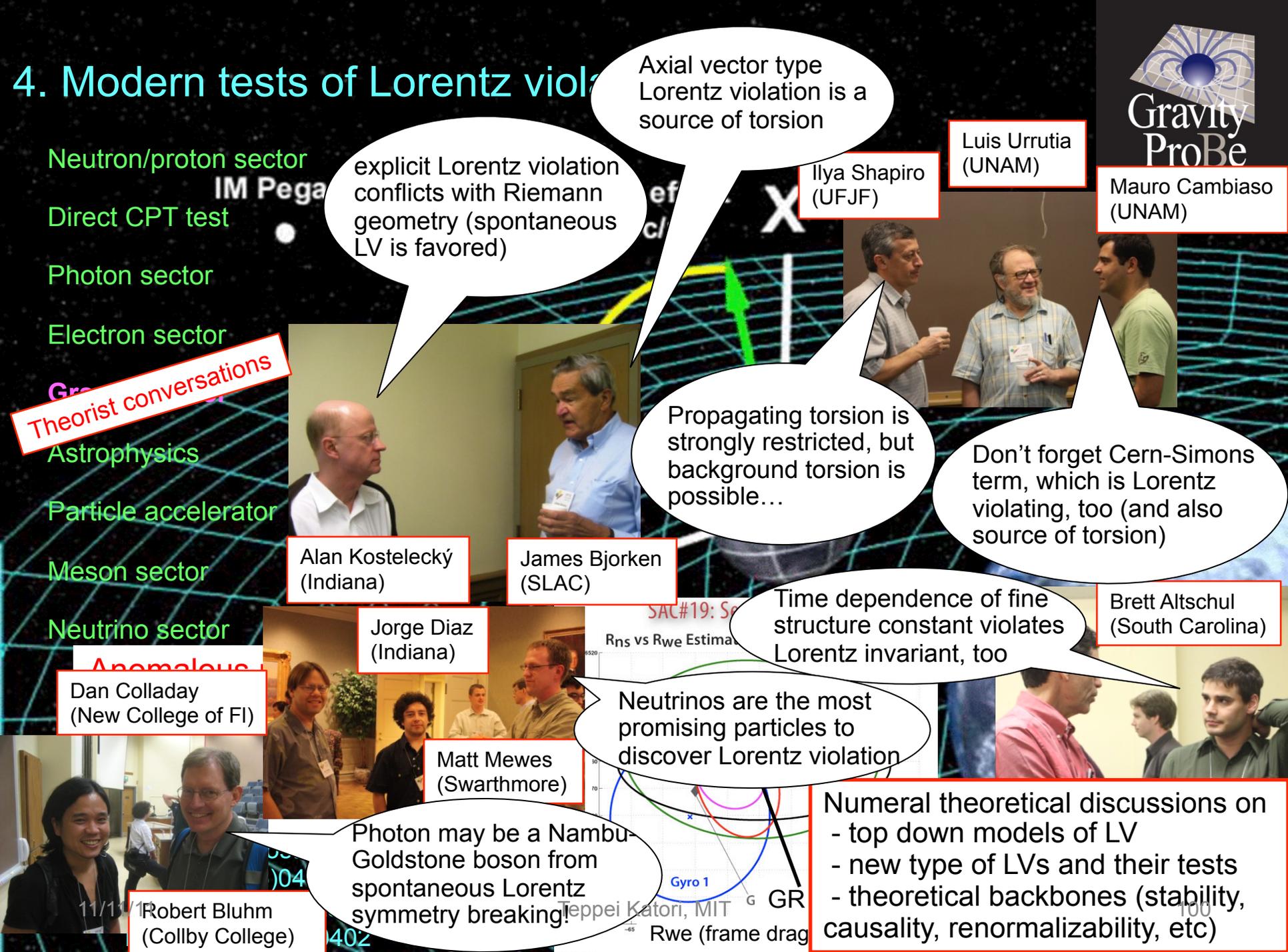
James Bjorken (SLAC)

Jorge Diaz (Indiana)

Matt Mewes (Swarthmore)

Robert Bluhm (Collby College)

Tejpei Katori, MIT



## 4. Modern tests of Lorentz violation

Neutron/proton sector

Direct CPT test

Photon sector

Electron sector

Gravity sector

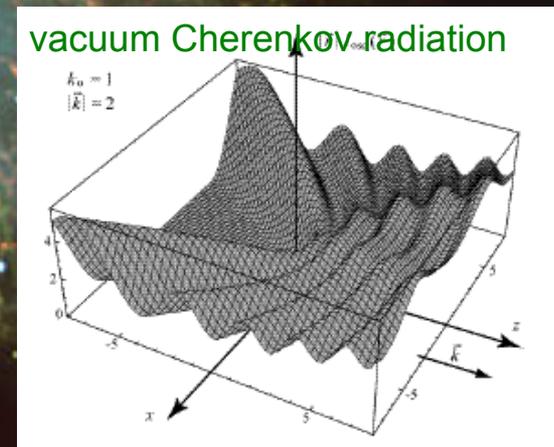
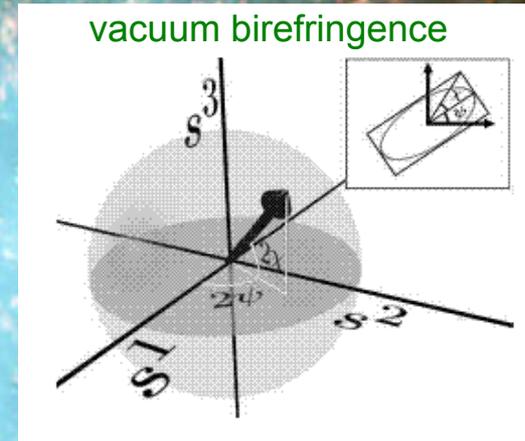
**Astrophysics**

Particle accelerator

Meson sector

Neutrino sector

GRB Lorentz violating dispersion  
 $c^{(6)} < 10^{-22} \text{ GeV}^{-2}$ ,  $c^{(8)} < 10^{-25} \text{ GeV}^{-4}$   
GRB vacuum birefringence  
 $\kappa < 10^{-37}$



# 4. Modern tests of Lorentz violation

Neutron/proton sector

Direct CPT test

Photon sector

Electron sector

Gravity sector

Astrophysics

**Particle accelerator**

Meson sector

Neutrino sector

No vacuum Cherenkov radiation from the highest energy electrons at LEP constrains upper bound

The highest photon observed at D0 detector at Tevatron constrains lower bound

$$-5.8 \times 10^{-12} < \kappa_{tr} - 4/3 c_e^{00} < 1.2 \times 10^{-11}$$

Hohensee et al.  
PRL102(2009)170402

Fermilab



# 4. Modern tests of Lorentz violation

Neutron/proton sector

Direct CPT test

Photon sector

Electron sector

Gravity sector

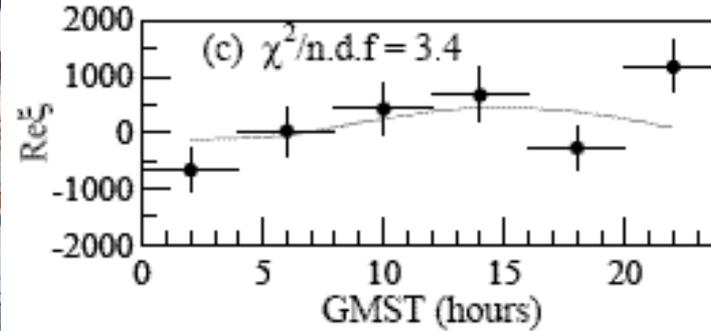
Astrophysics

Particle accelerator

**Meson sector**

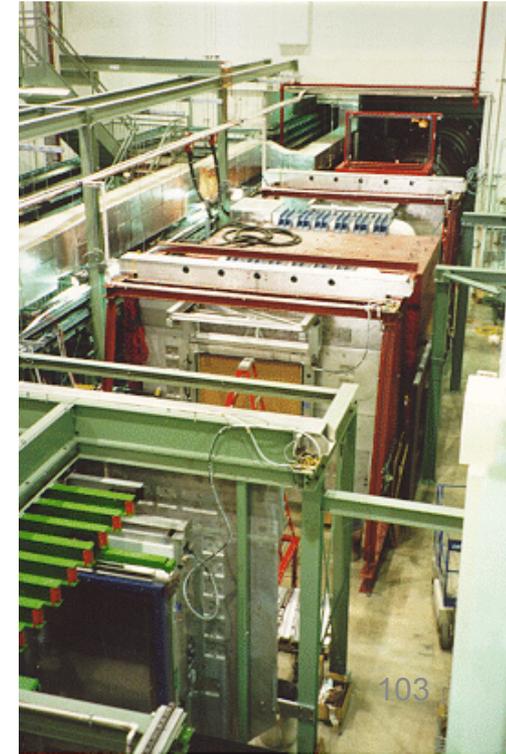
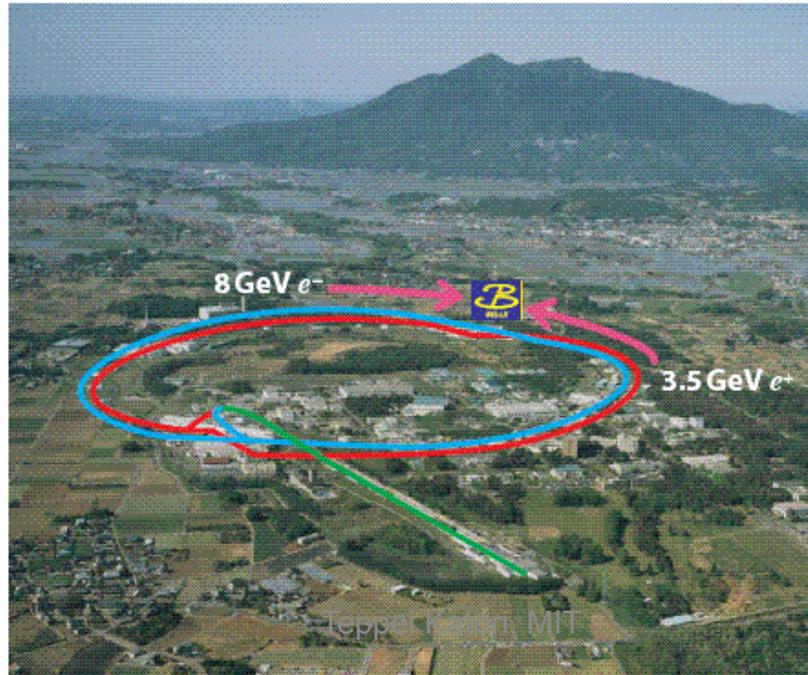
Neutrino sector

FOCUS and its data



KTeV

Belle



KTeV/KLOE (strange)

$$\Delta a_K < 10^{-22} \text{ GeV}$$

FOCUS (charm)

$$\Delta a_D < 10^{-16} \text{ GeV}$$

BaBar/Belle (bottom)

$$\Delta m_B / m_B < 10^{-14}$$

11/11/11

## 4. Modern tests of Lorentz violation

Neutron/proton sector

Direct CPT test

Photon sector

Electron sector

Gravity sector

Astrophysics

Particle accelerator

Meson sector

**Neutrino sector**

If, three neutrino massive model is correct, the deviation from standard  $\Delta m^2$  can be understood as the upper limit of Lorentz violation

In this approach, **longer baseline and higher energy neutrino experiments** have more sensitivity

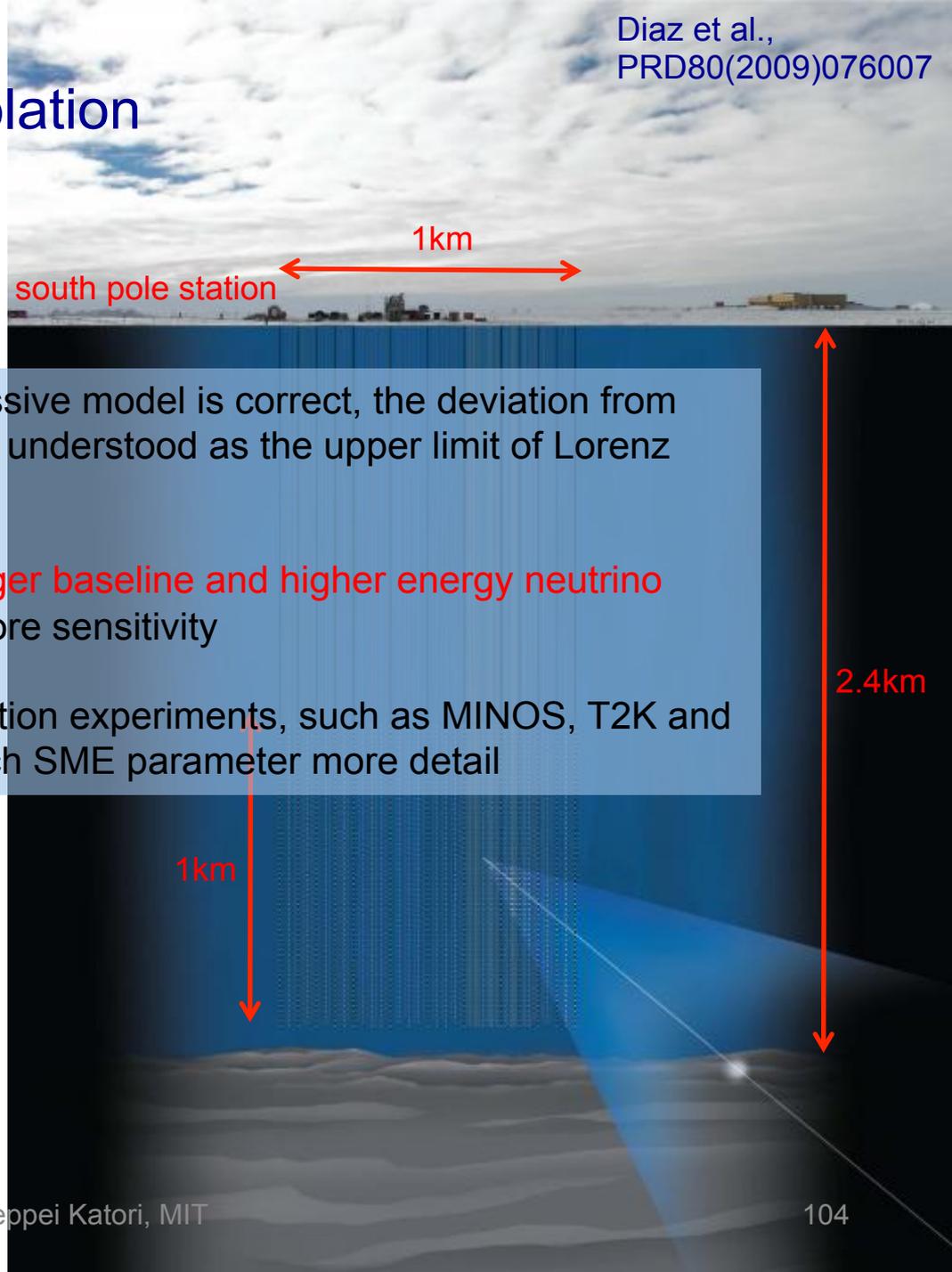
Long baseline oscillation experiments, such as MINOS, T2K and NOvA, can study each SME parameter more detail

IceCube experiment  
at south pole

IceCube collaboration  
PRD82(2010)112003

**IceCube**

$c(\text{CPT-even}) < 10^{-27} a$   
 $(\text{CPT-odd}) < 10^{-23} \text{ GeV}$





# 4. Modern tests of Lorentz violation

Neutron/proton sector

Direct CPT test

Photon sector

Electron sector

Gravity sector

Astrophysics

Particle accelerator

Meson sector

Neutrino sector

MINOS collaboration  
PRL 101(2008)151601  
PRL 105(2010)151601

If, three neutrino massive model is correct, the deviation from standard  $\Delta m^2$  can be understood as the upper limit of Lorentz violation

In this approach, longer baseline and higher energy neutrino experiments have more sensitivity

Long baseline oscillation experiments, such as MINOS, T2K and NOvA, can study each SME parameter more detail

NOvA experiment (NuMI Off-axis  $\nu_e$  Appearance)  
 $E \sim 2000 \text{ MeV}$ ,  $L \sim 800 \text{ km}$

**MINOS**  
 $c(\text{CPT-even}) < 10^{-23} \text{ a}$   
 $(\text{CPT-odd}) < 10^{-23} \text{ GeV}$

© 2007 Europa Technologies  
Image © 2007 TerraMetrics  
Image © 2007 NASA

© 2007 Google™

Streaming 100%

Eye alt 545.86 km

## 4. Modern tests of Lorentz violation

Neutron/proton sector

However, Lorentz violation could mimic neutrino masses.

Direct CPT test

We might be seeing Lorentz violation as an anomalous neutrino oscillation signal.

Photon sector

Electron sector

In this approach, it is important to test Lorentz violation for neutrino signals from precise terrestrial experiments, such as MiniBooNE, T2K, NOvA, Double Chooz etc

Gravity sector

Astrophysics

Particle accelerator

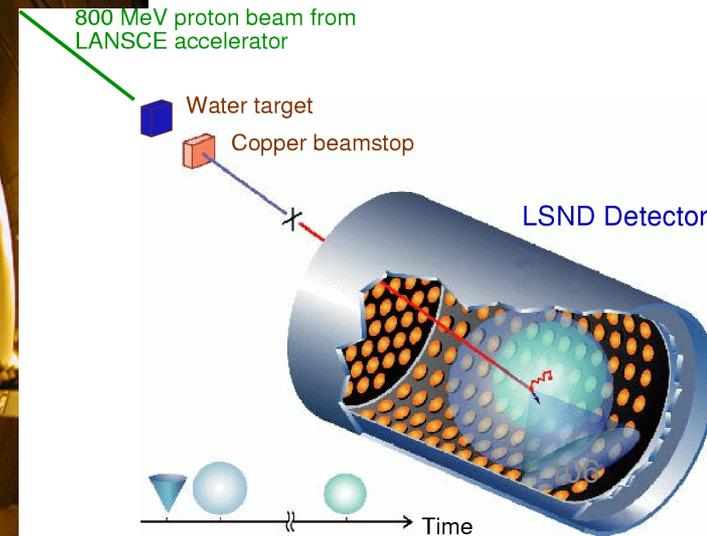
MiniBooNE

Meson sector

Neutrino sector



LSND



LSND

$a = 4.0 \pm 1.4 \times 10^{-19} \text{ GeV}$

MiniBooNE

11/11/11

??? (see next)

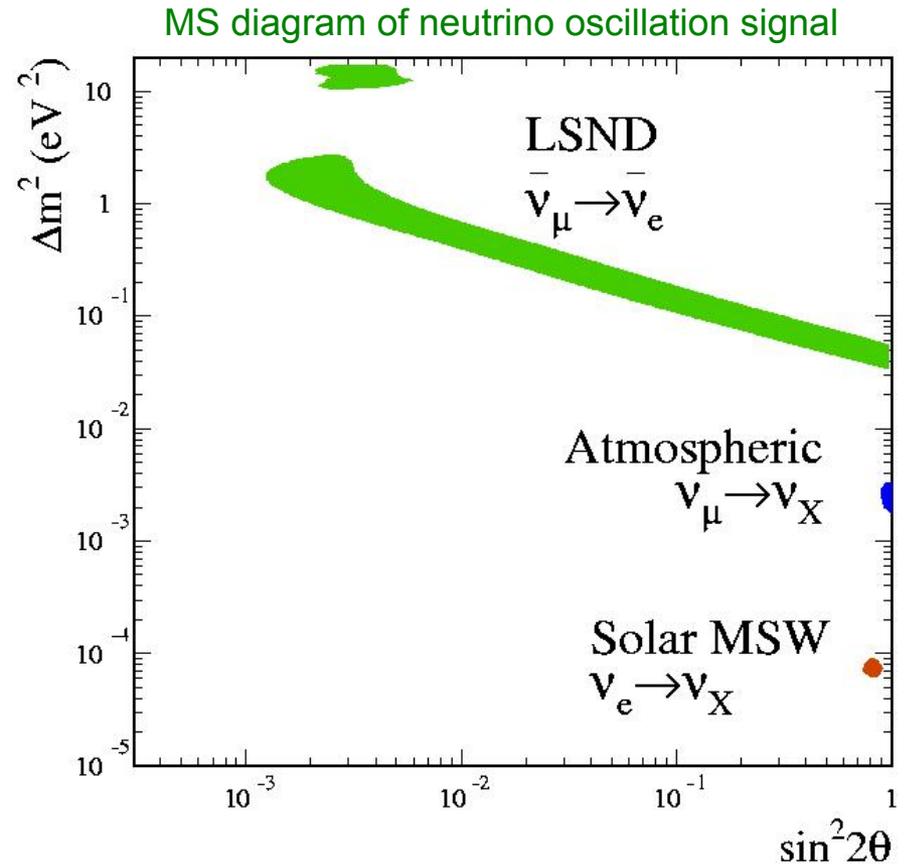
## 5. Lorentz violation with neutrino oscillation

The examples of model independent features that represent characteristic signals of Lorentz violation for neutrino oscillation

- (1) Spectral anomalies
- (2) L-E conflict
- (3) Sidereal variation
- (4) Compass asymmetries
- (5) neutrino-antineutrino mixing
- (6) classic CPT test

Any signals cannot be mapped on  $\Delta m^2$ - $\sin^2 2\theta$  plane (MS-diagram) could be Lorentz violation, since under the Lorentz violation, MS diagram is no longer useful way to classify neutrino oscillations

LSND is the example of this class of signal.



## 5. Lorentz violation with neutrino oscillation

The examples of model independent features that represent characteristic signals of Lorentz violation for neutrino oscillation

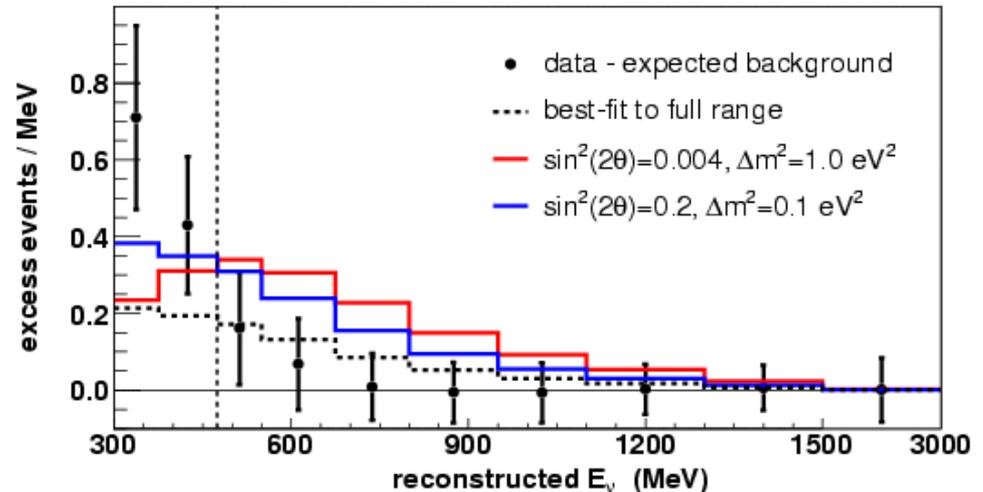
- (1) Spectral anomalies
- (2) L-E conflict
- (3) Sidereal variation
- (4) Compass asymmetries
- (5) neutrino-antineutrino mixing
- (6) classic CPT test

Any signals do not have L/E oscillatory dependence could be Lorentz violation. Lorentz violating neutrino oscillation can have various type of energy dependences.

MiniBooNE has appearance signal in the low energy region, but any naive neutrino mass models (either sterile or active) cannot make the energy dependence right.

MiniBooNE signal falls into this class.

MiniBooNE low E  $\nu_e$  excess



MiniBooNE collaboration  
PRL98(2007)231801

effective Hamiltonian  
of neutrino oscillation

usual term (3X3)

additional terms (3X3)

$$(h_{\text{eff}})_{ab} = \frac{1}{2E} (m^2)_{ab} + a_{ab} + c_{ab}E + \dots$$

## 5. Lorentz violation with neutrino oscillation

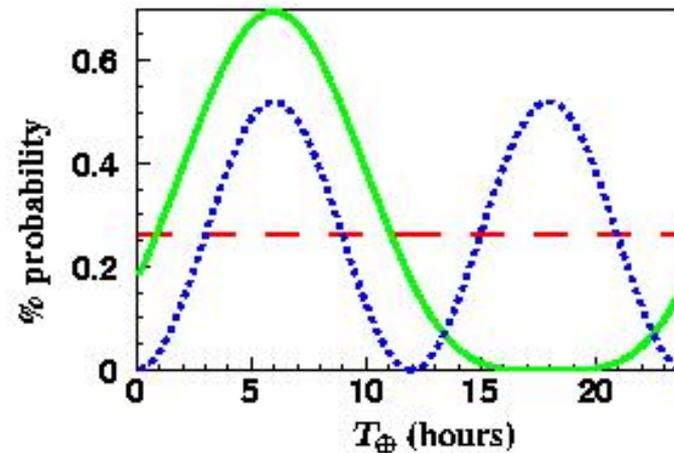
The examples of model independent features that represent characteristic signals of Lorentz violation for neutrino oscillation

- (1) Spectral anomalies
- (2) L-E conflict
- (3) **Periodic variation**
- (4) Compass asymmetries
- (5) neutrino-antineutrino mixing
- (6) classic CPT test

sidereal variation of the neutrino oscillation signal is the signal of Lorentz violation

This signal is the exclusive smoking gun of Lorentz violation.

example of sidereal variation for LSND signal



## 5. Lorentz violation with neutrino oscillation

The examples of model independent features that represent characteristic signals of Lorentz violation for neutrino oscillation

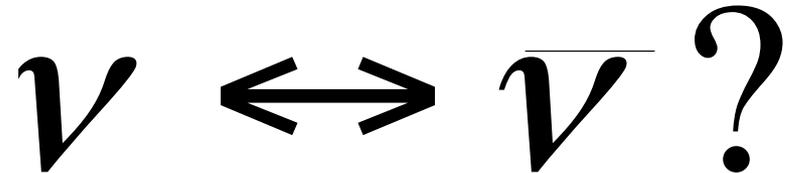
- (1) Spectral anomalies
- (2) L-E conflict
- (3) Periodic variation
- (4) **Compass asymmetries**
- (5) neutrino-antineutrino mixing
- (6) classic CPT test

Even if sidereal time dependence is erased out, effect of preferred direction may remain and it could affect neutrino oscillation signal (time independent rotation symmetry violation)

## 5. Lorentz violation with neutrino oscillation

The examples of model independent features that represent characteristic signals of Lorentz violation for neutrino oscillation

- (1) Spectral anomalies
- (2) L-E conflict
- (3) Periodic variation
- (4) Compass asymmetries
- (5) neutrino-antineutrino mixing
- (6) classic CPT test



neutrino-antineutrino oscillation is forbidden by helicity conservation. But some Lorentz violating fields violate conservation of angular momentum

formalism also contain neutrino-antineutrino oscillation

## 5. Lorentz violation with neutrino oscillation

The examples of model independent features that represent characteristic signals of Lorentz violation for neutrino oscillation

- (1) Spectral anomalies
- (2) L-E conflict
- (3) Periodic variation
- (4) Compass asymmetries
- (5) neutrino-antineutrino mixing
- (6) classic CPT test

CPT violation itself is the signal of Lorentz violation, so any difference between neutrino and anti-neutrino mode could be Lorentz violation

ex) Lorentz violating Hamiltonian for neutrino

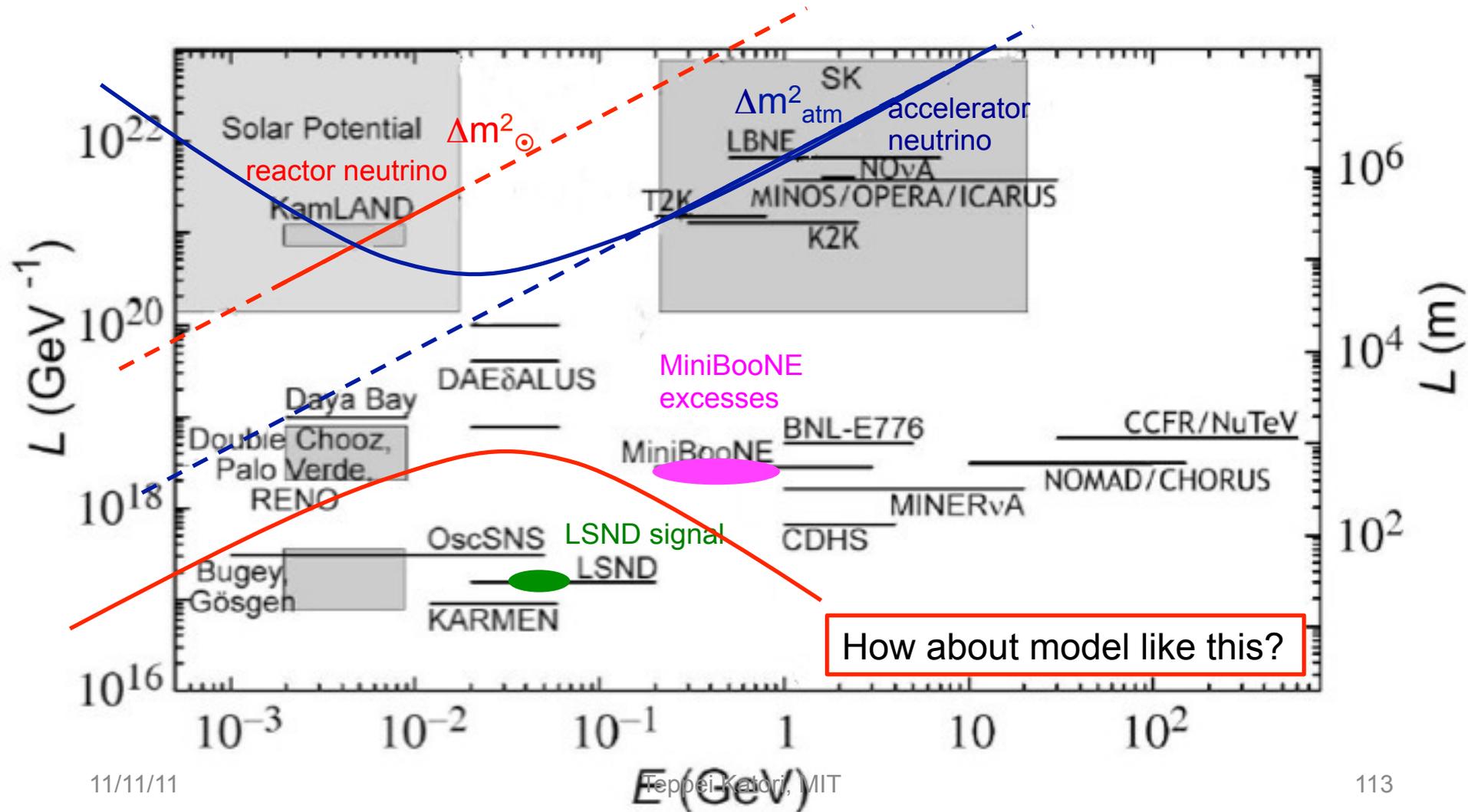
$$(h_{\text{eff}})_{ab} = |\vec{p}| \delta_{ab} + \frac{1}{2|\vec{p}|} (m^2)_{ab} + \frac{1}{|\vec{p}|} [(a_L)^\mu p_\mu - (c_L)^{\mu\nu} p_\mu p_\nu]_{ab}$$

ex) Lorentz violating Hamiltonian for anti-neutrino

$$(h_{\text{eff}})_{ab} = |\vec{p}| \delta_{ab} + \frac{1}{2|\vec{p}|} (m^2)^*_{ab} + \frac{1}{|\vec{p}|} [-(a_L^*)^\mu p_\mu - (c_L^*)^{\mu\nu} p_\mu p_\nu]_{ab}$$

# 5. Lorentz violation with neutrino oscillation

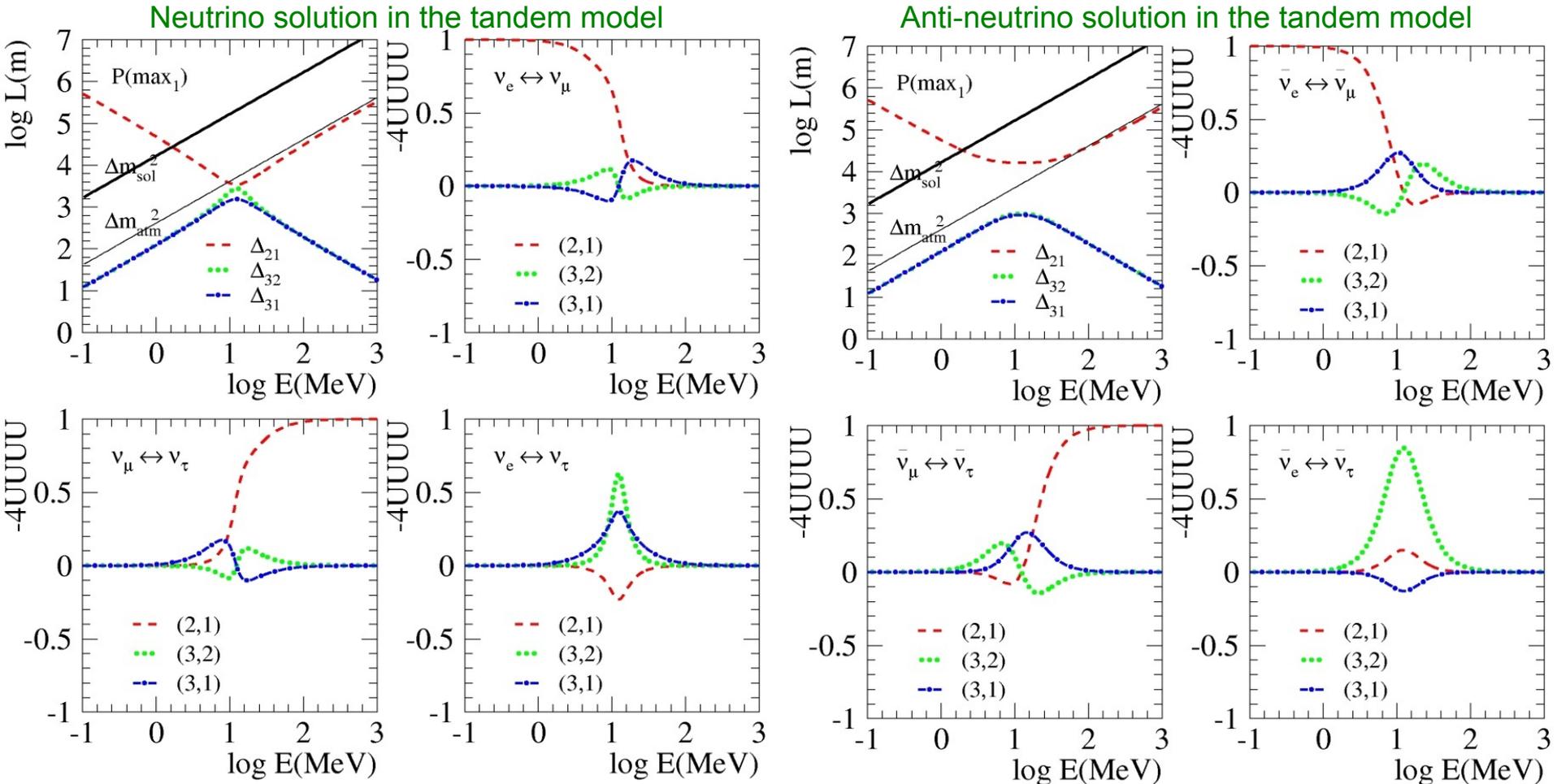
Model independent neutrino oscillation data is the function of neutrino energy and baseline.



# 5. Tandem model

## Tandem model

Tandem model has only 3 parameters, yet describes all neutrino oscillation data including LSND.

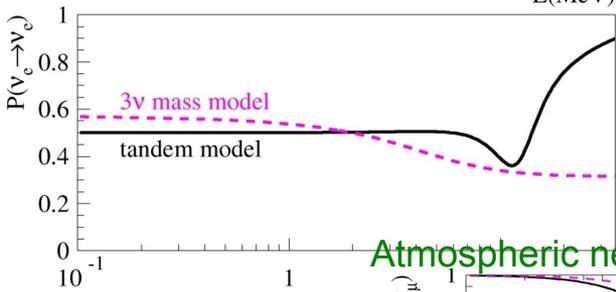
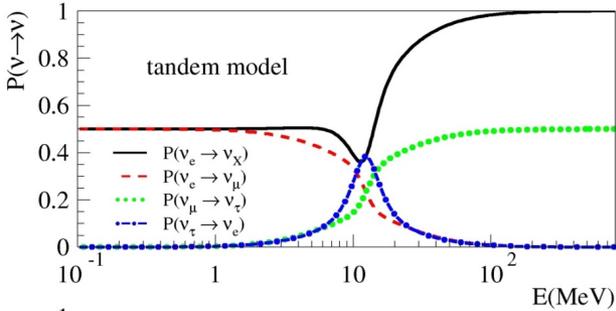


# 5. Tandem model

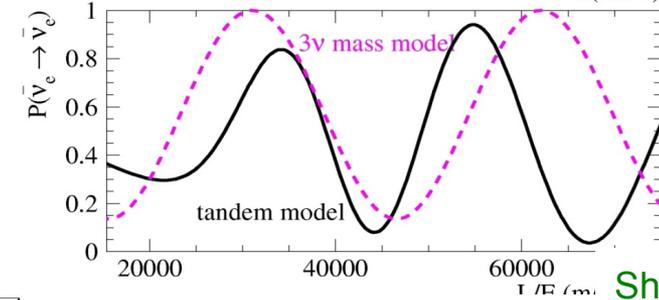
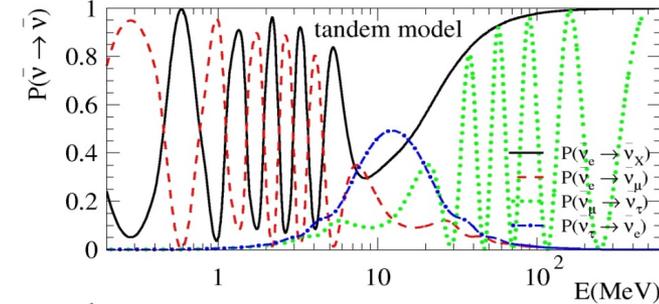
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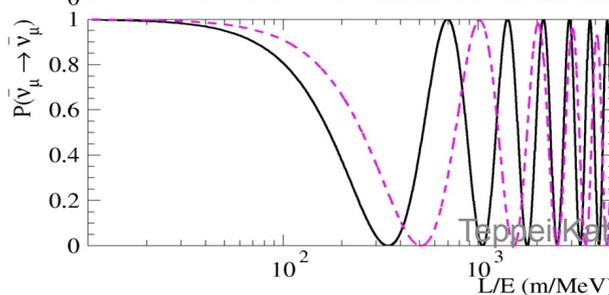
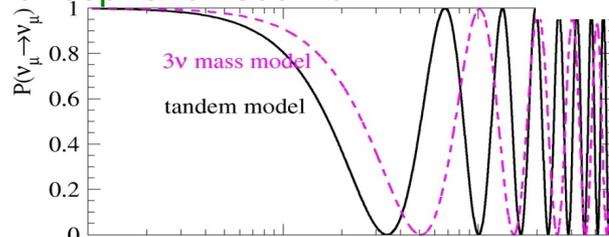
### Solar neutrino



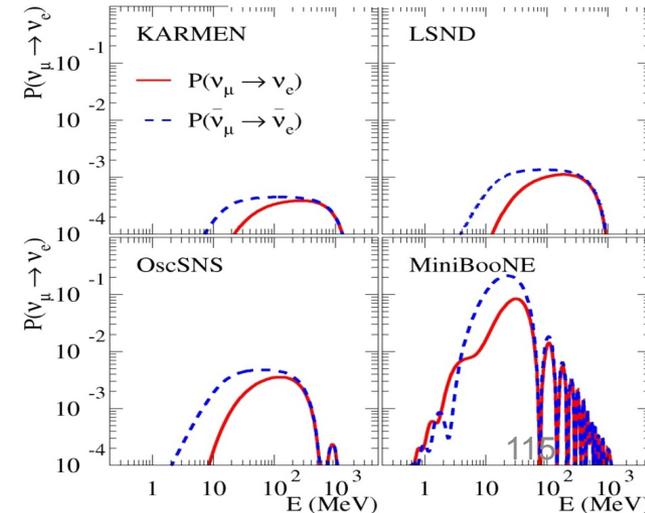
### Reactor neutrino



### Atmospheric neutrino



### Short baseline neutrinos



# 5. Oscillation analysis background summary

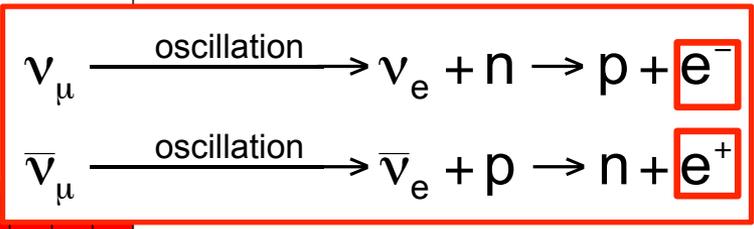
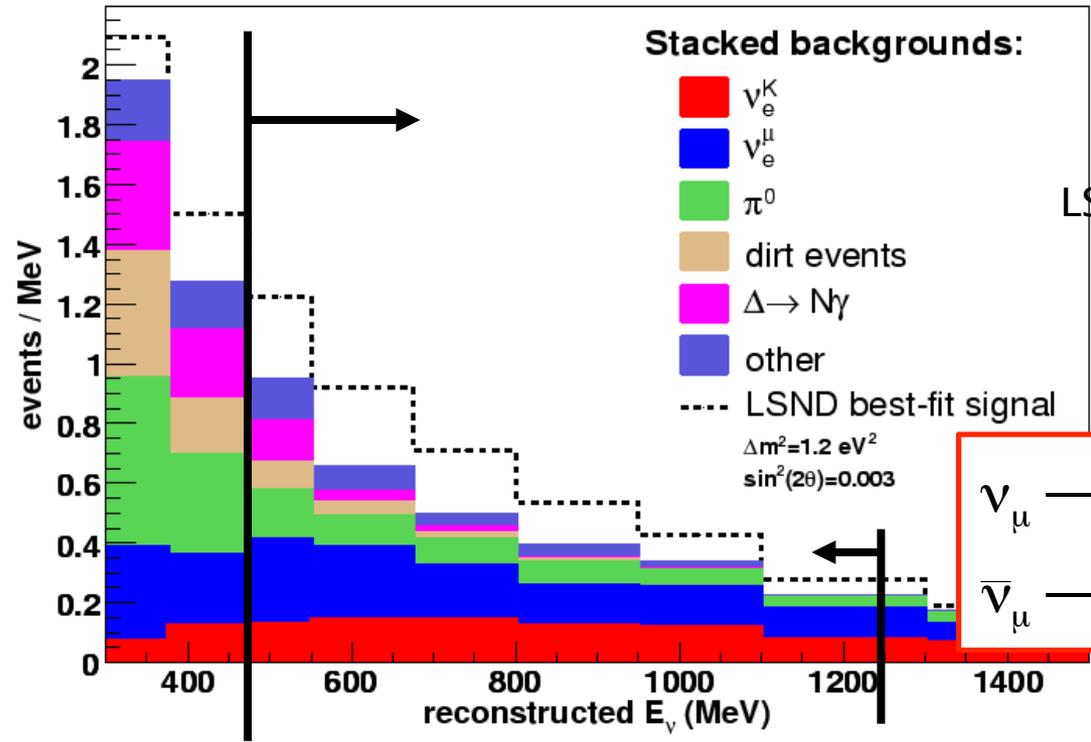
## Oscillation analysis summary

- Oscillation analysis uses  $475\text{MeV} < E < 1250\text{MeV}$

### 475 MeV - 1250 MeV

$\nu_e^K$	94
$\nu_e^\mu$	132
$\pi^0$	62
dirt	17
$\Delta \rightarrow N \gamma$	20
other	33
<b>total</b>	<b>358</b>

LSND best-fit  $\nu_\mu \rightarrow \nu_e$  126

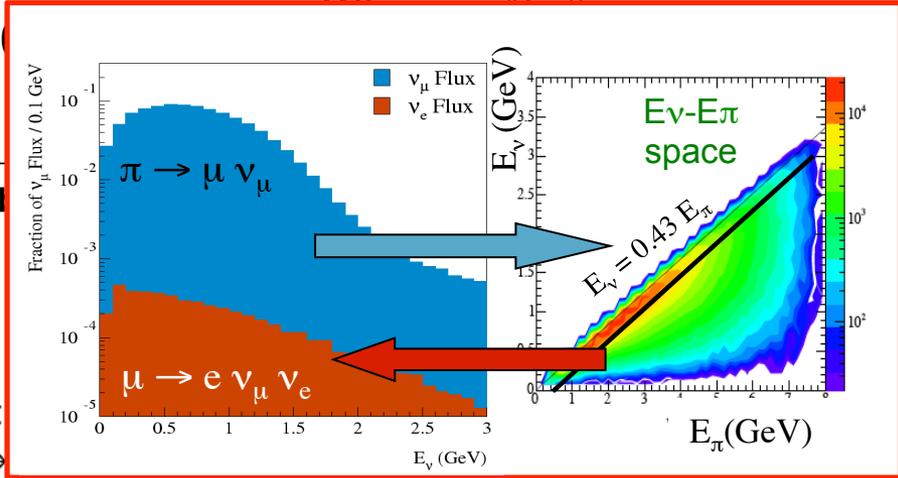
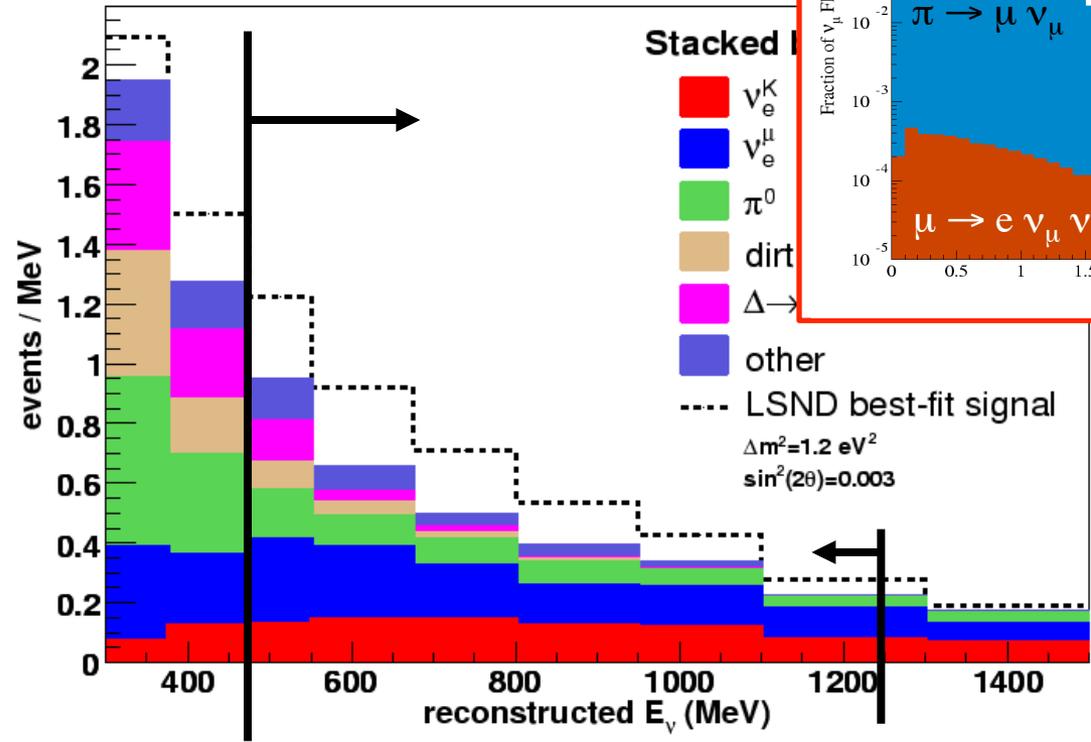


# 5. Oscillation analysis background summary

## Oscillation analysis summary

- Oscillation analysis uses  $475\text{MeV} < E < 1250$

475 MeV - 1250 MeV

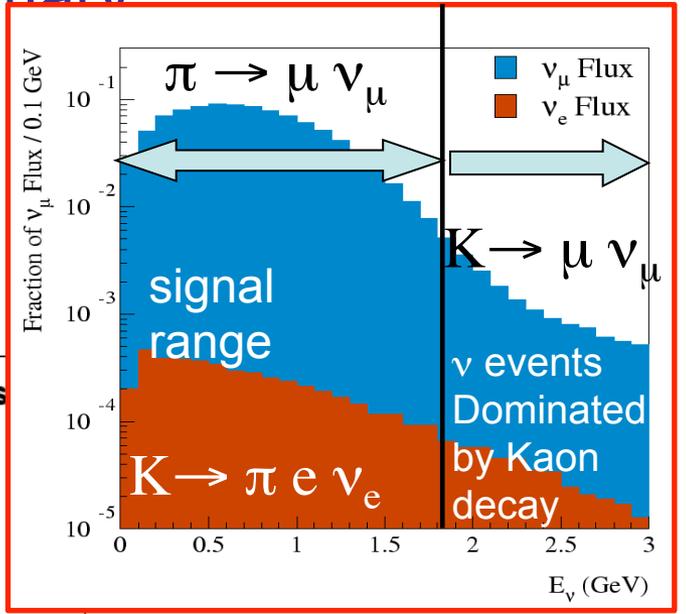
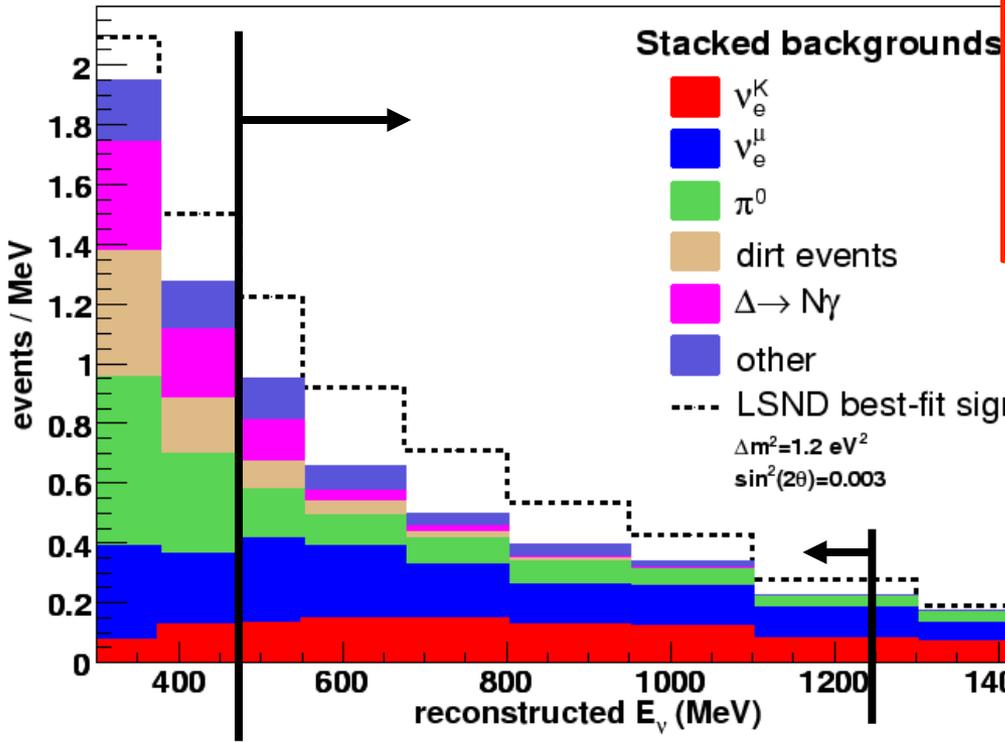


$\nu_e$  from  $\mu$  decay is constrained from  $\nu_\mu$  CCQE measurement

# 5. Oscillation analysis background summary

## Oscillation analysis summary

- Oscillation analysis uses  $475\text{MeV} < E < 1250\text{MeV}$



$\nu_e$  from  $\mu$  decay is constrained from  $\nu_\mu$  CCQE measurement

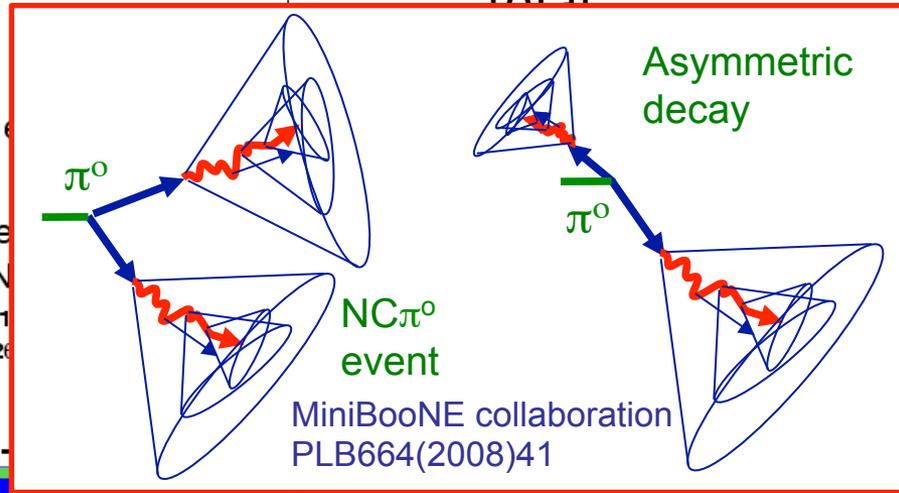
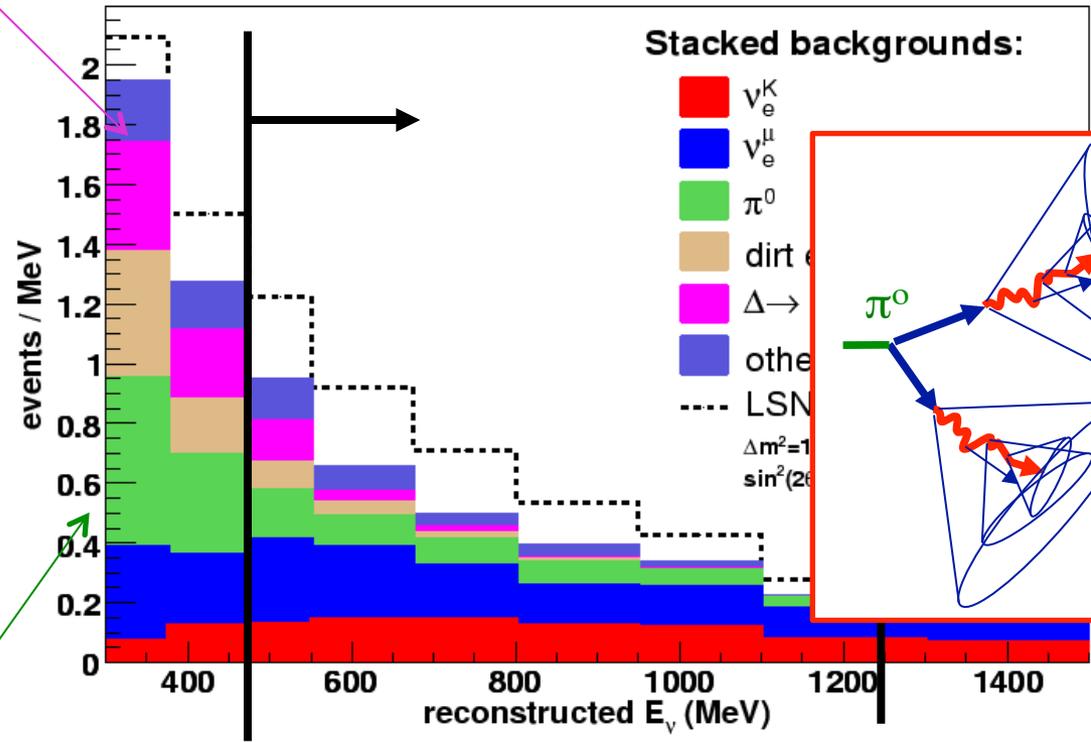
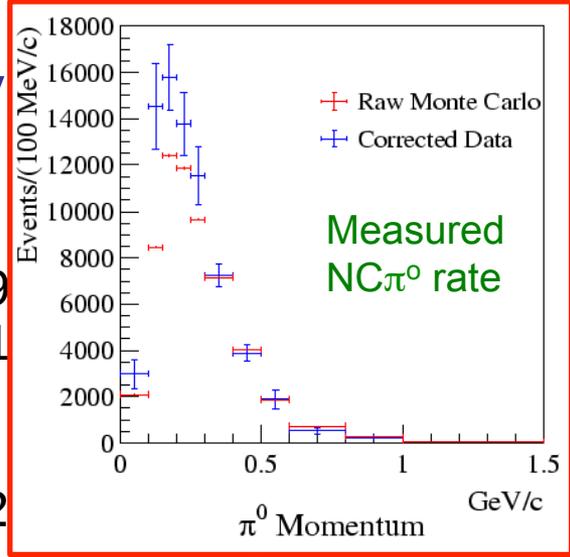
$\nu_e$  from K decay is constrained from high energy  $\nu_e$  event measurement

# 5. Oscillation analysis background summary

## Oscillation analysis summary

- Oscillation analysis uses  $475\text{MeV} < E < 1250\text{MeV}$

$\Delta$  resonance rate is constrained from measured  $\text{CC}\pi^0$  rate



Asymmetric  $\pi^0$  decay is constrained from measured  $\text{CC}\pi^0$  rate ( $\pi^0 \rightarrow \gamma$ )

$\nu_e$  from K decay is constrained from high energy  $\nu_e$  event measurement

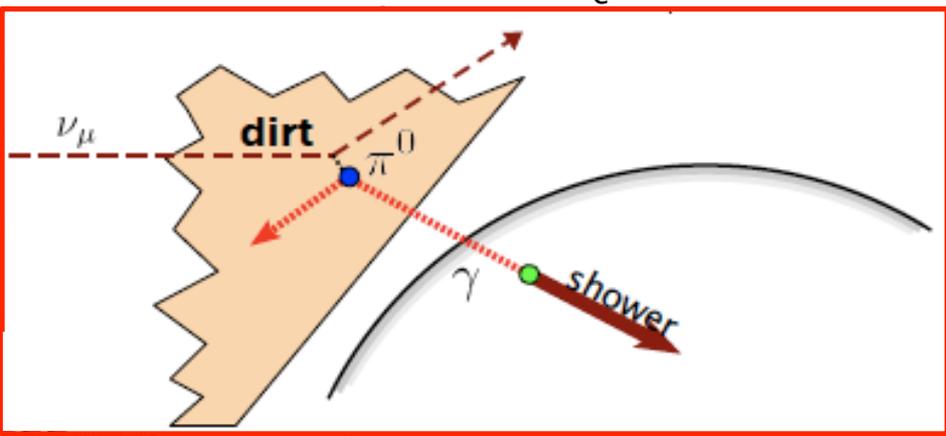
# 5. Oscillation analysis background summary

475 MeV - 1250 MeV

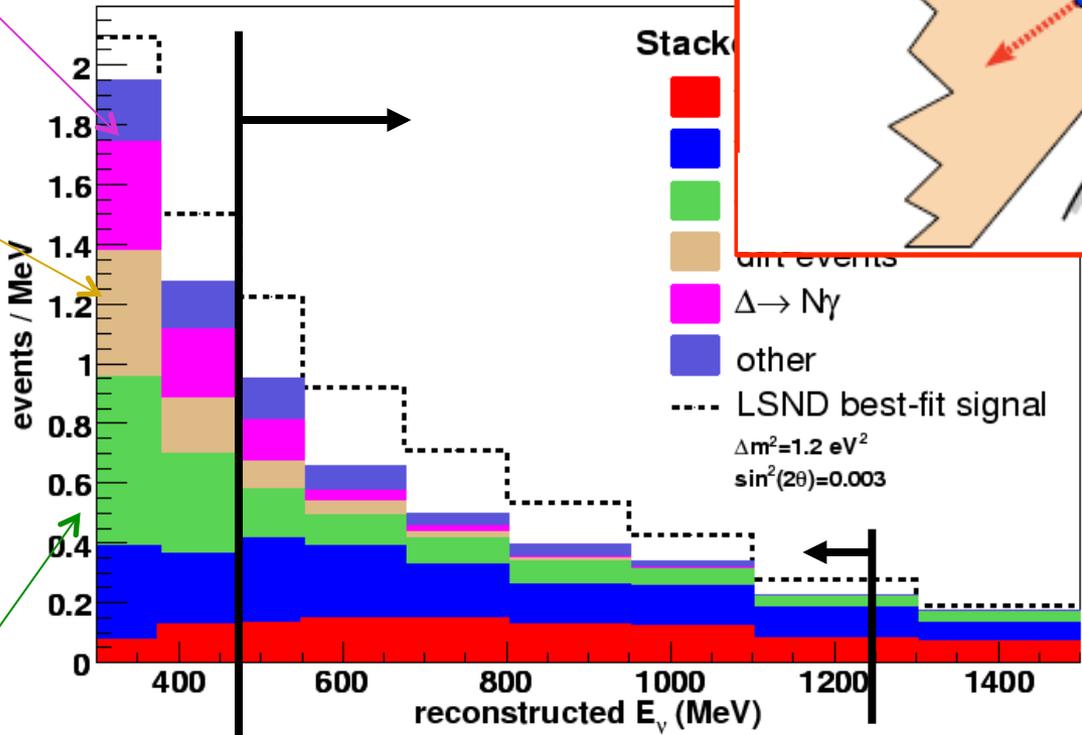
## Oscillation analysis summary

- Oscillation analysis uses  $475\text{MeV} < E < 1250\text{MeV}$

$\Delta$  resonance rate is constrained from measurement



dirt rate is measured from dirt data sample



Stacked  
 red dirt events  
 blue  $\Delta \rightarrow N\gamma$   
 green other  
 brown dirt events  
 --- LSND best-fit signal  
 $\Delta m^2 = 1.2 \text{ eV}^2$   
 $\sin^2(2\theta) = 0.003$

$\nu_e$  from  $\mu$  decay is constrained from  $\nu_\mu$  CCQE measurement

$\nu_e$  from K decay is constrained from high energy  $\nu_e$  event measurement

Asymmetric  $\pi^0$  decay is constrained from measured CC $\pi^0$  rate ( $\pi^0 \rightarrow \gamma$ )

# 5. Oscillation analysis background summary

## Oscillation analysis summary

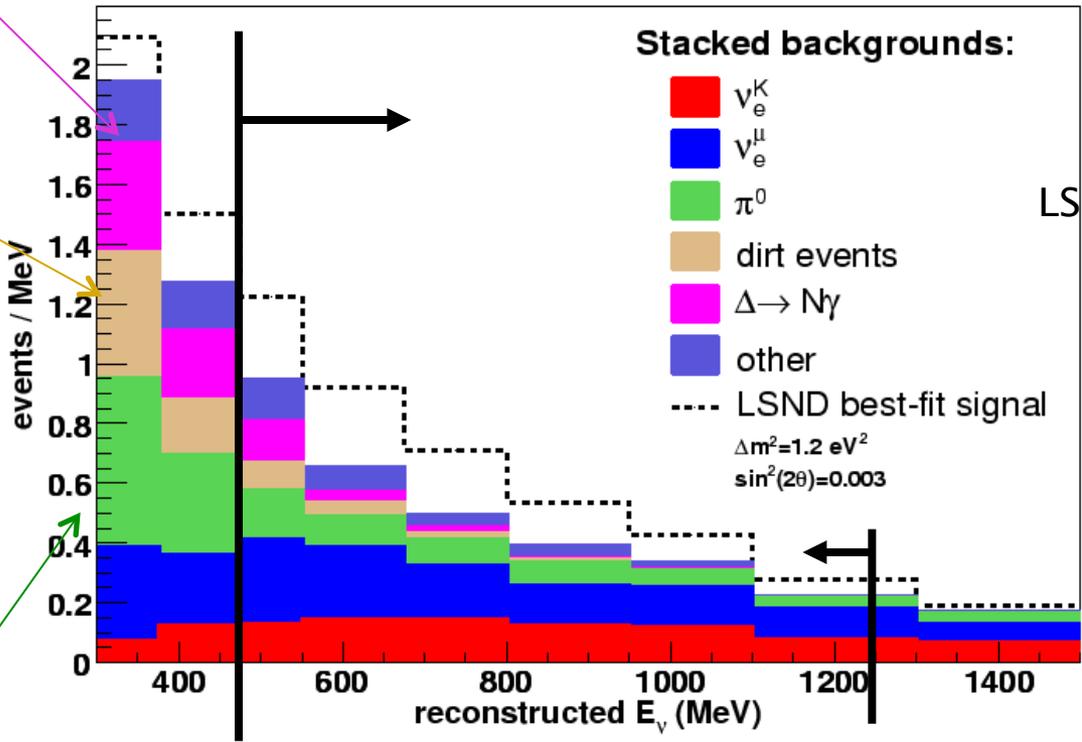
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dirt	17
$\Delta \rightarrow N \gamma$	20
other	33
<b>total</b>	<b>358</b>

$\Delta$  resonance rate is constrained from measured  $\text{CC}\pi^0$  rate

dirt rate is measured from dirt data sample



LSND best-fit  $\nu_\mu \rightarrow \nu_e$  126

$\nu_e$  from  $\mu$  decay is constrained from  $\nu_\mu$  CCQE measurement

$\nu_e$  from K decay is constrained from high energy  $\nu_e$  event measurement

Asymmetric  $\pi^0$  decay is constrained from measured  $\text{CC}\pi^0$  rate ( $\pi^0 \rightarrow \gamma$ )

All backgrounds are measured in other data sample and their errors are constrained!

# 7. Lorentz violation with MiniBooNE neutrino data

Neutrino mode result, high energy region

All parameters are consistent with zero (=no excess).

